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Miscellaneous Arithmetic :

OR A FULL

ACCOUNT of the NEW CALENDAR ;

With the several

USES of the LOGARITHMS,

AND OF

Multiplication and Division by MONY, &c.

IN SEVEN PARTS.

CONTAINING,

- I. A brief Account of the Festivals and Fasts of the *Jewish* and *Christian* Churches ; with such others as are mentioned in the present new Calendar ; very necessary for the better understanding the said Calendar.
- II. A Dissertation concerning Years, Months, &c. and the manner of their being settled in the World, for the better Computation of Time. Together with the Calculation of Scripture-Measures, Weights, and Coins : and an Observation concerning the exquisite Workmanship of the Tabernacle, &c. in the Time of *Moses*.
- III. Rules for finding the Golden Number, Epact, &c. together with the Method of calculating *Easter*, and all the other moveable Feasts throughout the Year : All which serve for a further Understanding of the present new Calendar.
- IV. The Uses of the Logarithms ; shewing how to perform that Sort of Arithmetic in all its Parts, whether in whole Numbers, or in Fractions ; with the Method of adding and subtracting Indices, both affirmative and negative.
- V. The Method of performing Multiplication and Division of Pounds, Shillings and Pence, by Pounds, Shillings and Pence, so as it may answer the Purposes of performing an Operation in the Rule of Three, where the Terms are composed of Money only ; or in Fellowship, where the Terms are composed of Money and Time, by which it appears, that this Sort of Arithmetic is very curious, and perhaps not altogether useless.
- VI. Some Observations on the Weather ; by which any Person is enabled to form to himself some Ideas of it for the Time to come ; to which is subjoined, a Taste of Enigmatical Writing, together with the Character of a good Christian, set forth in twenty Paradoxes, with their Solutions.
- VII. An Essay concerning the Education of Children, so far as relates to the several Sciences which they are to learn at School.

The Whole, being the fullest and completest of this Kind extant, is designed for the Use of Schools in *Great Britain* and *Ireland* ; and in the *English* Plantations and Colonies, as Subjects both profitable and entertaining.

By THOMAS DILWORTH,

Author of the *New Guide to the English Tongue*, *Schoolmasters Assistant*, *Young Book-keeper's Assistant*, &c. &c. and Schoolmaster in *Wapping*.

L O N D O N :

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Milnes, J. C. (1810-1880)
Account of the
Use of the
Division of
the





TO THE SEVERAL
LADIES and GENTLEMEN,

Who have been committed to the Author's
Care, and educated by him.

LADIES and GENTLEMEN !

HAVING instructed you, among other Things, in the Arts of Writing and Accompts, and am still instructing some of you in the same Arts, I hope it will not be deemed a fruitless Labour, if I furnish you with another Help, I mean that of understanding our present New Calendar, in all its Varieties : A Study as easy as it is pleasant, and equally as necessary for a Lady to be acquainted with, as a Gentleman.

Some Things in this Treatise, *viz.* the Management of Logarithms, and the Arithmetic of Mony, will not, in all Probability, become the Study of the Fair Sex, and therefore may be adjudged unnecessary for them to bend their Minds that Way ; but the Whole may be learn'd by young Gentlemen, with as much Ease as any other Part of Arithmetic.

The following Pages, carefully read over, I am sure will be both pleasing and profitable ; and therefore the making use of your *best Endeavours*

The DEDICATION.

herein, as well as in all your other Studies, will certainly turn to your Advantage, and afford such Satisfaction of Mind as cannot be purchased by careless Performances: And if a right Use be made of Numbers, it will certainly give you this Information, That all Knowledge therein (Teachers being only the Channels or Pipes of Conveyance) comes from the great Arithmetician of the Universe; whom to know and serve faithfully, will be your greatest Advantage; inasmuch as such an Obedience will, at the last, most surely bring you to the Mansions of an happy Eternity. I am,

LADIES and GENTLEMEN!

Your most humble

And most obedient Servant,

Thomas Dilworth.





T H E P R E F A C E.

*T*HE following Pages, containing (in Part) several Sorts of Arithmetic, which could not be conveniently join'd to the Schoolmasters Assistant; it was thought proper to print them by themselves: Nothing of that kind being taught in our Schools, in the ordinary Way; only among some few, the third and fourth Parts, as they lie in the Road to Navigation.

The Calendar and Logarithmetic, in every Author, I find so short, that a Pupil is hurried through them, before he rightly understands them; and the fifth Part has never yet been taught in any School at all.

As to the first Part, containing an Account of the Festivals and Fasts of the Jewish and Christian Churches; it was extracted partly from the Works of Dr. Sparke, Chaplain to King Charles the Second; partly from Mr. Nelson's Festivals and Fasts of the Church of England, but chiefly from the Works of Sir George Wharton, a Gentleman eminent for his Abilities, both in the University and in the Army, in the Time of King Charles the First; and who suffered very much, both in his Person and Fortune, for the sake of his Royal Master, by the Regicides, or their Favourers: And therefore I thought the introducing it into our Schools, in order to be read there, might contribute towards the understanding the new Calendar, as it is prefixed to our Common Prayer-Books: A Subject, though very easy and pleasant, I find many adult Persons intirely ignorant of. To which I have added, an Account of the other Festivals and Fasts, which are mentioned in the said Calendar, whereof three, viz. January 30th, May 29th, and November 5th (which being merely temporary) are observed by the Church of England only, during the Will of the Legislature; together with another on September 2d, observed in London only; and the rest, (at least some of them) by the Church of Rome, or such others as are in Communion with that Church.

THE PREFACE.

The second Part contains a Dissertation concerning Years, Months, Weeks, Days, Hours, Minutes and Seconds; and the manner of their being settled in the World, for the better Computation of Time; taken in Part from the fore-mentioned Sir George Wharton: Together with Tables of Scripture-Measures, Weights and Coins; with an Appendix, containing the Method of calculating its Measures of Surface, and reducing them to our own Measures. (A Work originally begun by the late Lord Bishop of Peterborough, and placed in our large Quarto Bibles) in several Places of which Appendix, are placed the Arithmetic of those Calculations, as a further Explanation of that Appendix; to which is subjoin'd, an Observation concerning the exquisite Workmanship of the Tabernacle, the Ark of the Testimony, Mercy-Seat, &c. in the Time of Moses; all which were directed by God Almighty himself, and shewn to Moses while he was with God on the Mount. Intended to be read by the Youth of both Sexes at their Schools, in order to give them some Ideas of those Measures both of Surface and Capacity, and to exclude contemptible Thoughts of the divine Workmanship.

The third Part, which contains Rules and Tables for a further understanding the new Calendar, is the fullest and compleatest of any thing of that Kind hitherto published for Scholastic Uses; and to make it turn to any Advantage, the Pupil should be taught how to make the Table for finding the Golden Numbers, Epacts, Dominical or Sunday Letters; and also the moveable Feasts dependant on Easter; together with the other Tables of the Moon, containing her Change, Full, Age and Southing; and what Year, Month, Day and Hour, these will happen on.

*The fourth Part contains the Use of the Logarithms; a Sort of Arithmetic first invented by Lord Napier, Baron of Merchiston in Scotland, and is of such Use for the facilitating of Calculations in several Parts of the Mathematics, that it is very well worth the while to be perfectly acquainted with them. And here the Learner will find the largest Instructions that he can possibly desire, or that are any where to be found. If Sherwin's Tables (which I would recommend for ordinary Use before any other) were
join'd*

THE PREFACE.

join'd to this Part of the Pupil's Study, I believe it would be found very agreeable. The Addition and Subtraction of Indices, I never saw in Print before; but as they are used both affirmatively and negatively before Logarithms, I thought it might not be amiss, first to consider them in the Light they are there placed, though they may otherwise be looked on as the Coefficients in Algebra. One thing I must beg Leave to observe, that whereas I have found some Authors make use of one Sort of Negative Indices, and some, another Sort, that is, their Complements to 10, I have in this Treatise shewn the Uses of them both; so that the Pupil may hereafter use either of them, as he likes best; and also to prevent his being surpris'd, when he should at any Time meet with an Author that treats of them one Way, when himself has learned them another Way.

The fifth Part is a Sort of Arithmetic, which is nowhere taught that I know of, except in a few idle Questions, too often given by Way of Trial of a Boy's Abilities, but have no Foundation in Reason; and it was owing to Propositions of this Kind, which set me at work to try how far this Way of managing broken Numbers could be carried. That it is curious, I think none can deny; how far it is really useful, I shall leave others to determin. That it holds most certainly good, is obvious enough from the several Operations wrought at Length in the Rule of Three, and proved both by Whole Numbers, Vulgar Fractions, and Decimals: Not that I am a Friend to what is called Multiplication of Money by Money, exclusive of Division going along with it: For where the Rule of Three is not concern'd, it is idle to the last Degree; but where it is concern'd, both Multiplication and Division must be first learned, that the fourth Proportional may be found: And the Multiplication of any two Terms of different Names in the Rule of Three of Whole Numbers, would make as bad a blunder, were not the Product divided by the other Term.

And as Examples make up one of the best Methods of conveying Instructions to, and confirming them in the Pupil, he will here meet with such a competent Number of them,

The P R E F A C E.

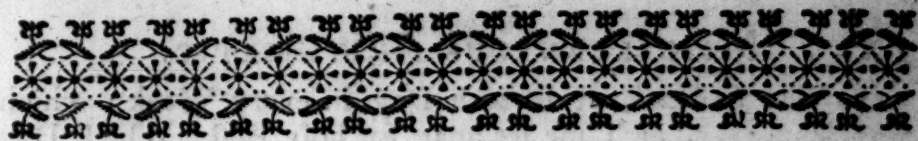
throughout all the Parts, as cannot fail of answering the End expected, and of which most other Treatises are extremely defective.

The sixth Part contains, First, some Observations on the Weather, very necessary for a Boy of some Genius to be acquainted with, which lately made its Appearance in the World in a very unjust Manner, by which it appears as if this was copied from that unfair Performance, but in Fact it was stolen from my Papers, while they were in Manuscript. Secondly, A Taste of Ænigmatical Writing, containing thirty-three dark, obscure and intricate Questions and Rebusses, with their Solutions. And Thirdly, the Character of a good Christian, set forth in twenty Paradoxes, each Paradox being solved in so clear a Light, that a Youth of middling Understanding may be able to comprehend them: All which serve as so many Touch-Stones to whet the Genius of those, who are not inclined to be idle; and to help those, who are inquisitive after Knowledge. And as Studies of these Kinds are not to be entered on till the Pupil's Ideas are enlarged by a due Share of reading and studying Numbers, I thought it would not be amiss to give them a Place here, for the Benefit of such industrious young Ladies and Gentlemen. To which are subjoined a few Questions, some Arithmetical, and others of Pleasantry.

The seventh and last Part contains, as the Title-Page expresses it, An Essay concerning the Education of Children, so far as relates to the several Sciences, which they are to learn at School; with a Word or two concerning good Manners in Children, the Circumstances of their Parents, and School-Prayer. If the Whole of this Part is read with the same Candour that it was wrote, it will never give Offense, but on the Contrary have its desired Success.

Upon the Whole: If any Instructor of Youth has Courage enough to use this Treatise in his School, as the Schoolmasters Assistant is used; it will save him an infinite deal of Trouble, and at the same Time will give his Scholars an Opportunity of making four times the Improvement, by having Business always ready cut out for them; in all which both Teachers and Scholars will undoubtedly find their Advantage.

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Miscellaneous Arithmetic :

OR A FULL

ACCOUNT of the NEW CALENDAR, &c.

PART I.

A short ACCOUNT of the
FESTIVALS and FASTS
OF BOTH THE
JEW S and CHRISTIAN S,
WITH THE
Original and End of their INSTITUTION.

*** I ***
T cannot well be denied, but that as God, by his extraordinary Presence, hath hallowed and sanctified certain Places ; so by his extraordinary Works, he hath worthily advanced certain Times ; for which Reason they ought to be esteemed, with all Men, more holy than other Days.

The Times so advanced, are the Festivals and Fasts of the *Jews and Christians.*

I. Of the FESTIVALS and FASTS of the JEWS.

These were of two Sorts, viz. First, Those instituted by divine Authority. And

Secondly, Those which were instituted by the Appointment of Men.

First, Of the *Jewish* Festivals and Fasts,* instituted by divine Authority. These also were of several Sorts,

A 5

1. The

* Note, It does not appear any where in Sacred Writ, that God Almighty appointed any Fasts ; but that the Jewish Fasts were purely of human Institution.

1. The *Sabbath*, or seventh Day in every Week; which signifies a Day, or Time set apart for holy Rest: Which Day God consecrated to his Worship, because thereon he rested from his Work of Creation, as may be seen at large, *Ex. xx. 9, 10. 11.* The Ends whereof, were

(1.) *Ecclesiastical*, for the Worship of God, and Meditation upon his divine Works.

(2.) *Civil and Oeconomical*, for the Ease and Refreshment of their Bodies, whose Strength had been exhausted by Labour. *Six Days thou shalt do thy Work; and on the seventh Day thou shalt rest; that thine Ox, and thine Ass may rest, and the Son of thine Handmaid, and the Stranger may be refreshed. Exod. xxiii. 12. and Lev. xxiii. 3.*

(3.) *Spiritual* (1.) As being a Type of that spiritual Rest, whereby we should cease from the Works of the World, and the Flesh, that God might work in us by his Word and Spirit. And (2.) As shadowing unto us that endless Rest, which all of us hope to enjoy with God in the World to come.

2. The *Neomeniæ*, or Feasts of New Moons, celebrated the first Day of every Month, beginning with the new Moon; *Numb. xxviii. 11.* which were instituted in Memory of the Light created by God.

(1.) That his People, by this Means might be alienated from the Superstitions and Idolatries of the *Ethnics* (who subjected the Months to the Planets, Stars, and Celestial Signs) and know that God is the only Lord, Governor, and Moderator of the Stars and Signs themselves, and consequently of the Months and Years, and Time in general; and therefore give unto God the greater Thanks, who ordained all these Things for the Use and Benefit of Men.

(2.) To typify Man's Renovation by the Illumination of the Holy Spirit, which is still required of all the Faithful. *Except a Man be born of Water and of the Spirit, he cannot see the Kingdom of God. John iii. 5.*

3. The *Pascha*, or *Passover*, which signifies a Passage or Leap. This was instituted *Anno Mundi 2513*, at the Departure of the *Israelites* from the Land of *Egypt*; and afterwards during their Abode in the Wilderness, celebrated from the fifteenth Day of the first Month *Abib* (called afterwards *Nisan*) to the twenty-first Day of the same Month, inclusively; that is, for seven Days together: Yet so, as that the first and last thereof, *viz.* the fifteenth and twenty-first, were held more festiuous, and sacred than the rest. These seven Days were likewise called the Feast of *Azyms*: and the first of them

them the *Pascha*, because that thereon the *Paschal* Lamb was eaten —

(1.) To call to mind, and as it were, consecrate to Eternity, God's miraculous Deliverance of the *Israelites* from their Bondage in *Egypt*, by the destroying Angel's smiting the *Egyptians*, and passing over the Houses of the *Israelites*.

(2.) For a sure Testimony of the perpetual Mercy and Power he would shew to his People. And,

(3.) To typify Christ Jesus, and our Deliverance perfected by him.

4. The Feast of *Pentecost*, so called from the Greek Πεντηκοστή, called also by the Hebrews, *Exod.* xxxiv. 22, and *Deut.* xvi. 10, the *Feast of Weeks*. But it truly signifies the fiftieth (solemn and festival) Day from the second of the *Azymes*, in which Sense St. Luke takes it, *Acts* ii. 1, And when the Day of *Pentecost* was fully come; and *Acts* xx. 16. speaking of St. Paul, For he hastened, if it were possible for him, to be at Jerusalem the Day of *Pentecost*. By this Name also are meant all those fifty Days, betwixt the second of *Azymes*, and the fiftieth festival Day. It is also called *Festum Primitiarum*, the Feast of the first Fruits, from the first Fruits, or the Bread offered which was made of the first Fruits. *Exod.* xxiii. 16.

This Feast was instituted,

(1.) In Memory of the Law given by God on Mount *Sinai*, the fiftieth Day after the *Israelites* departed out of *Egypt*.

(2.) That by the ceremonial Oblation of two Loaves made of the new Fruits, to the Lord, Men might be admonished they received all Fruits, and so all things else for the Preservation of Life, from the bountiful Hands of God, and be also excited to beseech God, not only for a Blessing thereupon, but also to make a sanctified Use thereof.

(3.) To typify that *Pentecost*, wherein Christ, after his Ascension, proclaimed the Law (not that which was written in Tables of Stone, but) in the Heart and Mind, the Law of the new Covenant; that happy Day, on which the first Fruits of the Holy Spirit were miraculously poured down on the Apostles.

5. The Feast of *Trumpets*; because on the first Day of the seventh Month ecclesiastical, or first political, the sound or Noise of Trumpets or Cornets, were every where heard by the Command of God, *Levit.* xxiii. 24, In the seventh Month, in the first Day of the Month, shall ye have a Sabbath, a Memorial of blowing of Trumpets, an holy Convocation. Hence, some of the Jewish Rabbins believed it was ordained in Memory of

Isaac's

Isaac's Deliverance from being sacrificed : And that God commanded a Noise should be then made by the Trumpet or Horn of a Ram, because a Ram was caught by his Horns in a Thicket or Bush, *Gen. xxii. 13.* and sacrificed in his stead. Others have thought it very unlikely, that so public and solemn a Feast should be instituted for the Deliverance of a single Person, but rather to commemorate those grievous Wars which the *Israelites* undertook, first against the *Amalakites*, and afterwards the *Ethnics*, to the End they might be admonished that this human Life of ours is nothing but a perpetual Warfare upon Earth.

6. Next to the foregoing, and in the tenth Day of the same Month, was the Feast of *Expiation* or *Atonement* celebrated ; *Levit. xvi. 29,* and *xxiii. 27.* In which annual Solemnity, an universal expiatory or propitiatory Sacrifice was perform'd for the Sins of the People : Whereby the whole Passion and Fruits of our Saviour's Death, were yearly shadowed out, by the whole Church. Yet the *Jews* say, it was instituted in Memory of God's Favour to them, in forgiving their Sin of Idolatry, committed by their making a Calf in the Desert.

7. The Feast of *Tabernacles*, celebrated next after the two former, *viz.* from the fifteenth Day of the Month *Thifri*, to the twenty-first Day inclusively, that is, for seven Days together ; yet so, as that the first and last Days were more solemn and festiuous than the rest. *Levit. xxiii. 34, &c.* The End of which Feast, is contained in these Words, *That your Generations may know that I made the Children of Israel to dwell in Booths, when I brought them out of the Land of Egypt. Levit. xxiii. 43.*

8. Next to this did immediately follow the Feast of the *Congregation*, or great and solemn Assembly, celebrated the twenty-second Day of the seventh Month, and called by the Hebrews *Hatifph*, also *Azereth*, that is, an Assembly or Collection : Or secondly, a Retention and Prohibition ; because that when the seven Days of the Feast of *Tabernacles* were expired, the People were obliged to hold it one Day longer : Or thirdly, because upon that Day they were prohibited the doing any Work : Or fourthly, because the People were obliged to contribute Mony for the Use of the Sacrifices : Or fifthly, because it shadowed out a Collection of all Nations : Or sixthly, a Gathering together of the Elect in the Kingdom of Heaven : Or lastly, from the Collection of Fruits, because on the Close of this Day, were offered the *Primitia*
of

of the *Serotine* Fruits, or first Fruits of the Evening, and that Thanks were therefore given unto God. Howbeit, it was an Appendix to the Feast of Tabernacles, as may be seen, *Levit. xxiii. 36, 39, and Numb. xxix. 35.*

But here Note, that *Jeroboam*, who revolted with the ten Tribes from *Rehoboam*, the Son of *Solomon*, commanded the precedent Solemnity of *Tabernacles* (which the *Jews* were commanded by God, in the Law, to celebrate in the seventh Month) to be kept in the fifteenth Day of the eighth Month; that so by little and little, he might wean the Sons of *Israel* from the Rites and Customs of their Fathers, as in *1 Kings, xii. 32.*

9. The next Feast instituted by God, was the *Septennial*, or *Sabbatical* Year, which took Beginning from the tenth Day of the seventh Month. For as the *Jews* every seventh Day, so their Land every seventh Year kept a Sabbath: The Observation whereof consisted in these two things especially, *viz.*

(1.) That the Ground should lie untilled.

(2.) That Debts should be remitted.

And therefore *Moses* (*Deut. xv. 1, 9.*) called this Year the Year of *Release*; because that both Agriculture or Tillage, and Debts were this Year commanded by God to be forborn and remitted. *Deut. xv. 1, 2, and xxxi. 10.*

The Causes of this Feast, were partly Civil, partly Mystical. *First* Civil, to teach them,

(1.) That they were not by continual Exercise to draw out the Strength of the Earth, and thereby make it barren; for, as all other Creatures, so likewise the Earth, hath need of Intermision and Rest.

(2.) Gratitude to God for the Fruits of the Earth, and Mercy to the Poor, whereof a principal Regard is had in this Law. And

Secondly Mystical,

(1.) To remind them of *Adam's* first Estate, wherein only the voluntary Fruits of the Earth were fed upon.

(2.) To shadow out unto them an eternal Sabbath, that is, a blessed Life, in which all the Labours and Miseries of the present Life, together with Exactions of Creditors, shall have an End, and the Sins of Believers be remitted.

10. The tenth and last of the Feasts instituted by the Command of God, is the Year of *Jubile*, that is, a Year of Rejoicing, or of Remission, celebrated every fiftieth Year; for so it is commanded, *Levit. xxv. 8. And thou shalt number seven Sabbaths of Years unto thee, seven times seven Years; and the*

the Space of seven Sabbaths of Years, shall be unto thee forty and nine Years. Therefore the Year following this, was the fiftieth Year, and wholly Sabbatical: From whence, if you account exclusively to another Year of Jubile, you have only forty and nine Years, and so it is numbered in the latter Part of the Verse last cited; but if inclusively, that is, if you account both the former and the latter, you shall have fifty Years, as at Verse the 10th of the last mentioned Chapter; which manner of Account is often used by us at this Day. For thus a Week is said to have eight Days, counting both the *Sundays*; but one of them being excluded, there remains but a true Week, consisting of seven Days.

In this Year, not only the Bondmen of *Israel* were set free from their Masters, and the Prison Doors thrown open, but all Debts were likewise remitted; and the Grounds, Vineyards, Houses, and other Possessions return'd to their first Owners. For it was not permitted any Man to sell his Grounds or Houses to another, by a perpetual Contract; but only the Use and Fruits thereof till the Year of Jubile; which may be read at large in the forementioned 25th Chapter of *Leviticus*.

The End of this Feast, like the former, was partly *Civil* and partly *Mystical*.

First, *Civil*.

(1.) Because God therein so ordained things, that the Families of the *Israelites* should not be destroyed, but more especially that Family, out of which the Messiah was to come.

(2.) To shew unto us what a special Regard he had, and still has, for the Poor, to put them in Hope of a better Condition for the future, and also lay down a Way to brotherly Communion, so far forth as the Condition of this Life will permit.

(3.) As the *Olympiads* were in Use among the *Greeks*, the *Lustra* among the ancient *Romans*, and the *Indictions* among the later *Romans*, whereby they supputated Time; so also the *Hebrews* should be accustomed to number their Times by Jubiles, so soon as possessed of the holy Land.

Secondly, *Mystical*, To shadow out to them, by this public Jubile and solemn Joy, the Lord *Jesus*, and the whole Business of their Salvation: and this himself alluded to, *Luke iv. 19*, where he saith, *To preach the acceptable Year of the Lord.*

Secondly, Of the *Jewish* Fasts and Festivals, done by the Appointment of Men.

1. The *Jejunia Quatuor*, or four solemn Days of Fasting, mentioned in *Zechariah* viii. 19.

(1.) The Fast of *Jerusalem besieged*, which (notwithstanding it to be the last, according to the Order of the Months, yet it) is the first in respect of the Order of the Thing done. This was celebrated the tenth Day of the tenth Month, on which Day *Nebuchadnezzar* first pitched his Tents before, and besieged *Jerusalem*, 2 *Kings*, xxv. 1.

(2.) The Fast of *Jerusalem taken by Nebuchadnezzar*, celebrated the ninth Day of the fourth Month, v. 3.

(3.) The Fast of *Jerusalem forsaken*, or made desolate, celebrated the ninth Day of the fifth Month, because that on this Day in this Month, the City and Temple were set on fire; first by *Nebuzaradan*, Captain of the Guard belonging to *Nebuchadnezzar*, King of *Babylon*, v. 9. and after that by *Titus*.

(4.) The Fast of *Gedaliah*, who was left in *Judea* by *Nebuzaradan*, and slain by the Treachery of *Ismael*, celebrated the third Day of the seventh Month. *Jer.* xli. 2.

Note, *The foregoing four solemn Fast-Days, were, by the divine Order, appointed to be Days of Feasting at the Restoration of Jerusalem, Zech. viii. 19.*

2. To the foregoing four Fasts (during the Captivity of the *Jews* in *Babylon*) was annexed the solemn Fast of *Queen Esther*, instituted in Memory of the three Days Fast she commanded, when about to apply herself to King *Ahasuerus*, on behalf of the *Jews*, *Esther* iv. 16, and celebrated the thirteenth Day of the twelfth ecclesiastical Month *Adar*, whereon all the *Jews* throughout the Kingdom of *Persia*, should have been slain by the Persuasion of *Haman*, *Esth.* iii. 9. Afterwards this Day became more celebrated for the signal Victory of *Judas Maccabeus*, who overthrew the Army of *Antiochus*, with *Nicanor* the Captain of it. 2 *Mac.* chap. ult.

3. The *Jews* likewise celebrated of old, the Fast of the *Tables of the Law broken* (which *Moses*, when descending from Mount *Sinai*, dashed against the Ground, and broke in Pieces, as being offended at their Idolatry of worshiping the Calf) the seventeenth Day of the fourth Month *Tamuz*.

4. The Days of *Purim*, or Feast of *Lots*, so called, because *Haman* had cast the Life and Death, as it were, of the *Jews*, upon the Hazard of a *Lot*; which Feast was first celebrated by *Mordecai* and *Esther*, the fourteenth and fifteenth Days of the last Month *Adar*, in Memory of the Lord's most wonderful Protection, when *Haman* had laid his inevitable Plot, to Man's thinking, for the utter Extirpation of the *Jews*, even in one Day. *Esth.* iii. 13.

5. The

5. The Feast of *Comportion of Wood*, mentioned by *Josephus*, Book 2, of the Wars of the *Jews*, Chap. 17, celebrated in the fifth ecclesiastical Month *Ab*, in Memory of the Wood comported, or brought for perpetual Nourishment of the Holy Fire in the Temple of *Jerusalem*, according to the Law of God. *Nebem. x. 34.*

6. The *Encænia*, or Feast of Dedication, or Consecration and Renovation of the Temple, instituted by *Judas Maccabeus*. For when *Antiochus Epiphanes* came out of *Egypt* into the Holy Land, and so to the Temple, he reduced both the City and Temple; everted the true Worship of God; carried away the Vessels of the Temple, and therein placed the Idol of *Jupiter Olympius*, as you may read *1 Mac. i.* But *Judas Maccabeus*, having undertaken a War against the Captains of *Antiochus*, overthrown their Armies, and recovered the City; purged the Temple, threw down and burnt the Idol, and again dedicated both the Altar and Temple to the Worship of God, in Memory of which this Feast was celebrated.

He also ordained, that the Dedication of the Temple, which was made at the first in eight Days, should be renewed and celebrated by Anniversary Holy-Days, for eight Days together, with Rejoicing and Gladness, beginning from the twenty-fifth of *Cisleu*, *1 Mac. iv.* And this is the Feast whereof *St. John* the Evangelist makes mention, and whereat our Saviour *Christ* himself was present. *Luke v. 1.*

7. The Solemnity of the Expiation of the Tower of *Jerusalem*, instituted by *Simon Asmonæus*, Brother to *Judas Maccabeus*, on the twenty-third Day of the Month *Ijar*. For having by Famine taken the Tower of *Jerusalem*, which a Garrison of *Antiochus* had, until then defended, he celebrated the same as on this Day, by a solemn Rite, to the great Rejoicing of the whole City, and commanded it to be, every Year, celebrated by Posterity, with festival Joy and Gladness. *1 Mac. 13.*

8. And lastly, The *Marriage Festivities*, observed by the Space of seven Days, *Gen. xxix. 22*, and *Judg. xiv. 10*, which are honourably mentioned by *Christ* in his Parables, and vouchsafed his Presence and first Miracle, *John ii. 8.*

And these are the *Feasts* and Solemnities celebrated by the antient *Jews*, whereof so frequent Mention is made in Scripture.

For the rest, instituted after their Destruction and Repudiation, and observed by the modern *Jews*, in all Places where-soever they are dispersed; as the Feast of the new Year; the Feast of Reconciliation; the Feast of Gladness, or Joy of the Law;

Law; the Feast Days of the Equinoxes and Solstices, &c., none of which are mentioned in the Old Testament, I shall forbear saying any thing about them; putting here a Period to the *Festivals* and *Fasts* of the *Jews*.

II. Of the FESTIVALS and FASTS of the CHRISTIANS.

Concerning the Solemnities of the *Christians*, we find not any one certainly declared in all the New Testament; neither is any Man bound to the strict Observation of those which were used of old by the *Jews*: Yet, because the Exercise of Godliness may be oft times interrupted, through the Infirmities of the Flesh, and Cares of the World, and that nothing is more convenient, nothing more necessary to the Confirmation and Increase of Faith, and the Exercise of the Christian Religion, than that Men should have certain Days, whereon frequently to meet in the public Assembly, and to hear the Word of God, seeing that Faith cometh by hearing thereof; therefore hath the *Christian Church* very worthily set apart certain Festivals, Holy Days, or Solemnities, and commanded the same to be religiously observed in the public Congregation, that so all daily Labours, and politic Affairs, being laid aside, we might thereon entirely apply ourselves to the public Service of God, to reading, and holy Meditation, with Joy and Gladness, as well of Mind as of Body.

The first of which is derived from the *Saxons*, commonly called *Sunday*, or the weekly Feast of the *Resurrection* of *Christ*, and thence called the *Lord's-Day*, instituted by the Apostles of *Christ*, in the room of the rejected *Jewish Sabbath*: to the End

1. That *Christians* might not seem to be tied and obliged to *Judaism*, and the Ceremonies of the *Jews*, but testify the Abrogation of the Mosaical Feasts, and manifest the Liberty received by *Christ*.

2. That as the *Jewish Sabbath* did continually bring to Mind the former World, finished by Creation, so the *Lord's Day* might keep us in perpetual Remembrance of a far better World, begun by him, who came to restore all things, and to make both Heaven and Earth new: for which Cause *they* honoured the last Day, *we* the first in every seven Days throughout the Year.

3. Because that *Christ* on this Day rose from the Dead; perfected the Work of Man's Redemption, and so entered into the Glory of the New Testament.

4. That

4. That (if Creatures be admitted) we can by no other Creature more congruously apprehend the Majesty of the mighty and supereminent Christ, the Son of Righteousness, than by the glorious Light of the Sun, the once supposed Ruler of this Day.

The other Holy-Days are divided into General, *i. e.* such as are generally celebrated by all Men, and termed Solemnities; as the *Nativity* and *Circumcision* of our Saviour, *Epiphany*, *Purification*, *Annunciation*, *Resurrection*, *Ascension*, *Pentecost*, *Trinity*, &c. And Particular, *i. e.* such as are kept by some particular Church, or of some whole Country or Community, as the Fast-Days for averting some public Calamity, and the Festivals for obtaining some public Deliverance; or else by some one Bishop's See, Parish, or Town, called the proper Holy-Days of the Place, as the Days of some particular Persons, Donors, or Benefactors: All which, whether they be general or particular, for the whole Day, or at least in the Time of the Morning, are ever esteemed holy; Divine Service being generally performed on such Days.

They are again divided (in respect of the Days whereon they fall in the Calendar) into moveable, and fixed or immoveable.

I. Of the MOVEABLE FEASTS.

The *moveable Feasts* are those, which howsoever they are celebrated on the same Week-Day, have got no fixed Seat in the Calendar, but in divers Years, fall upon sundry Days of the Month. Such are all the Lord's Days throughout the Year, and so indeed the interjected Days, which are fixed to certain Weeks. Whereof

1. The Lord's Day (when any happens) betwixt the Feast of *Circumcision* and *Epiphany*, hath no certain Name assigned to it, save only the first or second *Sunday* (whichsoever it is) after *Christmas-Day*. But the Lord's-Days that follow after the *Epiphany*, are denominated according to the numeral Order, by which Means they succeed the same; as the first *Sunday* after it, is called the first *Sunday* after *Epiphany*; the next the second, &c. Whereof there are in some Years four, in others more or fewer, according to the greater or lesser Quantity of the *Intervallum majus*, or Distance of Time between the *Epiphany* and *Easter*; for that is what I conceive Sir George Wharton means by the *Intervallum majus*, that being the greater Interval compared with the lesser one between the
Epiphany

Epiphany and *Septuagesima Sunday*. Howbeit, the *Sunday* next preceding that of *Septuagesima*, is always the last of the *Sundays* after the *Epiphany*; and the *Monday* next after the *Epiphany*, is called *Plough-Monday*; because the poorer Sort of People draw a Plough through the Streets, in the northern Parts of *England*, in order to excite the Charity of such People as are able and willing to bestow it upon them.

The next four Lord's-Days are thus nominated, viz. *Septuagesima*, *Sexagesima*, *Quinquagesima* and *Quadragesima*; the first three whereof had their Names from their Order by which they precede *Quadragesima*, as *Quinquagesima* is so called, because the next anteceding *Quadragesima*, and so of the rest.

For the better understanding the Nature of these three *Sundays*, viz. *Septuagesima*, *Sexagesima*, and *Quinquagesima*, I shall proceed in a retrograde Order, and begin with that of *Quinquagesima*.

1. Concerning *Quinquagesima*: Forasmuch as the Church hath commanded a Fast consisting of forty Days before *Easter*, called *Quadragesima*, or the holy Time of *Lent*, wherein there are but thirty-six Days, besides the Lord's-Days, on which she fasteth not; in regard of her Joy for his Resurrection: Therefore to supply this Defect, there were four Days (viz. *Asb-Wednesday*, and the three following Days) of the preceding Week, added to the *Quadragesimal* Fast. After which it was (first by *Telephorus*, Bishop of *Rome*, and Martyr, who flourished *Anno Christi* 141, and since that by *Gregory* the great) decreed, that all Priests should begin their Fasts two Days sooner, viz. the *Monday* and *Tuesday* before the four so added; to the End, that as they preceded the People in Dignity, so they might also precede them in Sanctity. Wherefore to the Week of *Quadragesima* was this other added, named *Quinquagesima*. It is also called *Shrove-Sunday*, because it is the *Sunday* immediately preceding and nearest to *Shrove-Tuesday*.

2. Touching *Sexagesima*, it is to be observed, that *Melchisedech*, Bishop of *Rome*, and Martyr (who flourished *Anno Christi* 311) instituted, that none should fast upon *Friday*, because of the Lord's Supper and Ascension, as upon that Day; so neither on the *Sunday*, which being the first Day of the Week solemnizeth the Resurrection, thereby to put a Difference between the *Christians* and the *Gentiles*. Therefore it pleased the Ancients, for Redemption of the *Fridays* in *Quinquagesima*

Quinquagesima (except *Good-Friday*) to add this other Week, which they called *Sexagesima*.

Note, *Though the Lord's Supper was instituted on the Thursday Night before the Crucifixion, according to the civil Day, which begins at Midnight, yet the ecclesiastical or scriptural Day, begins six Hours sooner, that is, at Six o'Clock in the Evening, and holds till Six in the Evening of the ensuing Day. Hence the Thursday Evening preceding, immediately, Friday Morning, and both making but one Day, the Institution of the Lord's Supper, is (above) said to be as on Friday: And if the Ascension of our Saviour was in the Afternoon, it will hold nearly good in this Respect also: but the Scriptures being silent in this Case, makes it difficult to determine the particular Time of the Day when Christ ascended into Heaven.*

3. *Septuagesima* is said to have been instituted for two Reasons;

(1.) For supplying or making up that which lacketh. For in regard some have not only not fasted upon the *Friday* (and therefore *Sexagesima* was instituted, as before) but neither also upon *Saturday*, because thereon our Saviour rested in the Grave, in token of our future Rest; (and indeed it is noted out of *St. Augustine*, that the People of *Asia*, and some others, grounding their Practice on a certain Tradition of the Apostles, did not fast upon the *Saturday*) to supply therefore the seven Days of *Sexagesima*, was thereunto added this Week, or Sev'n-night, called *Septuagesima*.

(2.) This Time of *Septuagesima*, denotes unto us the Exile and Afflictions of Mankind from *Adam*, to the End of the World; and therefore all Songs of Joy, were anciently intermitted by the Church, during the Time of *Septuagesima*. And as of old, during the seventy Years Captivity in *Babylon*, the *Israelites* laid aside their Instruments, saying, *Psalms cxxxvii. 4. How shall we sing the Lord's Song in a strange Land?* So now the Church lays aside her Songs of Praise during all this Time.

OF SHROVE TUESDAY,

And of the Custom of Ringing the Great Bell, in ancient Parish-Churches, at Ten o'Clock in the Morning.

This Day always immediately precedes *Ash-Wednesday*; and was, in the *Romish* Times, in *England*, and is now in all *Romish* Countries abroad, the Day of a general Confession in every Parish. For the Word *Shrive* is an old *Saxon* Word of which *Shrove* is a Corruption) and signifies Confession; hence *Shrove-Tuesday* signifies *Confession-Tuesday*; on which Day all the People in every Parish throughout the Kingdom, were

were obliged to confess their Sins, one by one, to their own Parish-Priests, in their own Parish-Churches; and that this might be done the more regularly, the great Bell in every Parish was rung at Ten o'Clock in the Morning (or perhaps sooner) that it might be heard by all, and that they might attend according to the Custom, then in Use. And as (God be praised) the *Romish Religion* has given Way to a much better, I mean the *Protestant Religion*, yet the Custom of ringing the great Bell in our ancient Parish Churches, at least in some of them, yet remains, and obtains, in and about London, the Name of *Pancake-Bell*; perhaps because, after the Confession, it was customary for the several Persons to dine on *Pancakes* or *Fritters*. Later Churches indeed, have rejected that Custom of ringing the Bell on *Shrove-Tuesday*, but the Usage of Dining on *Pancakes*, *Fritters*, and such like Provision still continues.

Of the F A S T of L E N T.

LENT, in the old *Saxon* Language signifies the *Spring*: And as the Time, or Forty Days of Fasting and Humiliation, generally observed by *Christians* before *Easter*, happens in or near the Spring, therefore that Time of Fasting is commonly called *Lent*.

Why this Fast should be confined to forty Days, neither more nor less, may be judged to arise from a Sanction given to that Number, for the following Reasons, *viz.*

Forty Days and *forty* Nights it continued raining, when the old World was drowned. *Gen. vii. 4, 12.*

Forty Years the Children of *Israel* did Penance in the Wilderness. *Numb. xiv. 34.*

Ten times *Forty*, or four hundred Years, the Children of *Israel* were afflicted, before they obtained their Deliverance by *Moses*. *Gen. xv. Acts vii. 6.*

Forty Stripes were given to Malefactors, when they were corrected. *Deut. xxv. 4.*

Forty Days and *forty* Nights *Moses* fasted twice, at his receiving the Law, and once more at his deprecating God's Anger against the *Israelites*. *Deut. ix. 9, 18, 25.*

Forty Days *Elias* fasted in the Wilderness. *1 Kings xix. 8.*

Forty Days the *Ninivites* were allowed to repent in. *Jonah iii. 4.*

Forty Days our blessed Saviour fasted in the Wilderness. *Matt. iv. 2.* And

Forty

Forty Days he conversed with his Apostles after his Resurrection. *Acts* i. 3.

So that whoever considers these Facts, cannot but think that this Number of Days was appointed by the Church, to be used by all as the common solemn Number belonging to extraordinary Humiliation. *Vid. Nelson's Festivals and Fasts.*

Sir Richard Baker saith, that this Fast of *Lent* was first commanded to be observed in *England*, by *Ercombert*, the 7th King of *Kent*, before the Year of Christ 800.

Of A S H W E D N E S D A Y.

This is the Head, or Beginning of the *Quadragesimal* Fast, or holy Time of *Lent*, dedicated by *Gregory* the Great, to the Consecration of and Sprinkling with Ashes, being therefore called *Dies Cinerum*, or *Ashwednesday*. And *Hospinian* confesseth, there was extant an Homily of *Maximus*, Bishop of *Tours* in *France*, with this Inscription, IN DIE CINERUM, which shews the Institution thereof before his Time: For that *Maximus Taurinensis* lived 170 Years before *Hospinian* viz. Anno Christi 440.

Quadragesima is so called, because (as before has been observed) it is forty Days distant from *Easter*, comprehending the Fast of *Lent*, as kept by the primitive Christians, in Imitation of our Saviour's Fast of forty Days and forty Nights in the Desert. In the Latin Church, the several *Sundays* in *Lent* obtain'd different Names from the first Words of such *Antiphons* as were sung on those Days, viz. *Invocavit*; *Reminiscere*, &c. but in *England*, those *Sundays* now go by the Names, first, second, third, &c. Sunday in *Lent*.

The fourth Sunday was called *Dominica de Rosa*, or *Rose-Sunday*, from the golden Rose, which the Bishop carried in his Hand before the People in the Temple: Likewise *Dominica de Panibus*, or *Loaf-Sunday*, because thereon the Miracle of the five Loaves in the Gospel used to be explained: In *England* we call it *Mid-lent Sunday*.

The sixth was called *Dominica Magna*, or great Lord's Day, because of the great and ineffable good Things which befel the Faithful in the following Week, viz. Sin cancelled; Death abolished; Heaven opened; Scripture verified; Man redeemed; and the Tyranny of the Devil spoiled by the Death of Christ. It is also called *Dominica Palmarum*, or *Palm-Sunday*, from the Branches of Palms, which the Jewish People strewed

on the Ground, when our Saviour (as on this Day) entered *Jerusalem*. Likewise *Dominica Passionis*, or *Passion-Sunday*, because it was the *Sunday* next before his Passion.

The *Wednesday*, next after this, is the Council-Day of the Scribes and Pharisees : The *Thursday* following, the *Parasceve*, or Preparation of the legal Passover ; and the Night thereof, the Institution of the Supper ; this is otherwise called *Maundy Thursday*, from a Ceremony anciently used by the Bishops and Prelates in Cathedral Churches, and Religious Houses, of washing the Feet of those who were subject to them. Which Ceremony is terminated the Fulfilling the Mandate, and is in Imitation of our Saviour Christ, who on this Day at Night, after his last Supper, and before his Institution of the blessed Sacrament, washed his Disciples Feet, telling them afterwards, that they must do the like to one another, which is the Mandate whence the Day is denominated. At the Beginning of the aforesaid Ceremony, these Words of Christ, uttered by him after his washing their Feet, *John xiii. 34.* were sung for an Antepson, viz. *Mandatum novum do vobis, ut diligatis invicem, sicut dilexi vos. A new Commandment I give unto you, that ye should love one another, as I have loved you.* And lastly, *Good-Friday*, being the Day of the Passion and Cross of Christ, whereon he suffered, and satisfied for the Sins of the whole World.

Next to the great Week, succeeds the *Passover*, or Feast of *Easter*, celebrated in Memory (not of the Angel's Transfit in *Egypt*, according to the *Jewish* Custom) but of the Resurrection of our Saviour. And yet we still retain the Name of *Passover*, not only because the Lamb, which of old was killed by the *Jews* in the *Passover*, was a Type of the Lamb of God, *Christ Jesus*, which was slain and sacrificed for the Salvation of the World ; but because at that very time he passed from this World to his Father ; or because that then a Passage was made from an old to a new Life.

It is called *Easter* from a Compellation or Name, made up of a *German* Term, first brought in among us by the *Saxons*, which is *Oest*, signifying *arising*, or the *East* ; and an *English* Term *Star*, which imports a Luminary of Heaven ; and both therefore now most emphatically suited unto Christ and his Arise, whose Name is the *East*, *Zech. ix. 12*, and whose Nature is the *bright and Morning Star. Rev. ii. 8.* And this is the Foundation and Basis of all the Lord's Days in the Year. And to the End, that we might have Leisure to confirm our Faith in the grand Article of our Resurrection, and to exert
our

our devout Affections in all those happy Consequences that are deducible from it; the Church has taken particular Care to set apart the two following Days, *viz. Monday and Tuesday*, for the Exercise of Religious Duties.

After this, immediately follows the *Quinquagesimal* Interval of fifty Days, between *Easter* and *Pentecost*, which was kept by the Primitive Christians, as a whole Festival, in Honour of the Resurrection and Ascension of *Christ*, and the glorious Mission of the Holy Ghost, with exceeding great Rejoicing and Gladness. It containeth six Lord's Days, or *Sundays*, which are all numbered according to their Distance from *Easter-Day*, as the first, second, third, fourth, fifth and sixth *Sundays* after *Easter*, whereof the first was anciently called *Dominica in Albis*, or *White Sunday*, because all the Catechumens, or Persons instructed in the Christian Religion, who had been baptized in the preceding *Easter-Day*, appeared in white Garments; and the fifth is still called *Rogation-Sunday*, and the Week following Rogation Week, invented, or as some think, restored by *Mamercus*, Bishop of *Vienna*, a City of *Austria* in *Germany*, *Anno Christi* 452, and so called *à rogando Deum*, from supplicating God, on the Account of such Earthquakes and Terrors which befel that City about that Time, as amazed the Hearts of all Men, who then began to forsake it, as a Place which Heaven seemed to have destined to Ruin. For then it was that the just mentioned Bishop earnestly exhorted the Remainder of the People, to prevent portended Calamities, by those holy and virtuous Means, whereby others have prevailed with God. It afterwards became general in the Christian Church; and the *Rogation Sunday*, and three following Days, *viz. Monday, Tuesday and Wednesday*, were (and great Pity we cannot say now) extraordinarily consecrated above all other Weeks in the Year unto Prayer and Supplication, for the following Reasons, *viz.*

1. Because Princes about this Time undertake their Wars.
2. Because the Fruits of the Earth (being some in the Herb and some in their Blossom) are in great Hazard: In both which Respects all Christians have good Occasion, at this Time especially, to pray.

In this Week also, usually on *Ascension-Day*, it hath been an ancient and good Custom, yearly (till of late Days) to make Perambulations and Processions in every Parish and Township, for viewing and considering the ancient Bounds and Limits, to prevent Incroachments and Contentions.

On

On the same *Ascension-Day* also of this Week (which is the fortieth Day from *Easter* inclusive, was wont to be, and is still celebrated the Feast of Christ's Ascension) thence called *Ascension-Day*, which is the Consummation of all he did and taught whilst on Earth, and therefore termed *Felix clausula totius Itinerarij filij Dei*, *The happy Period of the whole Journal of the Son of God*; the very Sabbath of all his Labour in the Work of our Redemption.

After the sixth *Sunday*, doth succeed the Solemnity of *Pentecost*, so called, because the fiftieth Day inclusive from the Resurrection of Christ. It was anciently called *Dominica in Albis*, like the first *Sunday* after *Easter*, or *White Sunday* (now corruptly *Whitsunday*) partly from the new baptized Christians then appearing in white Garments, in Token of the Joy and Solemnity thereof, which they were obliged to preserve in the future Course of their Lives; and partly from the Mission of the Holy Ghost, or glorious Light of Heaven, which was this Day sent down upon the Earth from the Father of Lights, and sat upon each of the Apostles in the visible Appearance of *fiery cloven Tongues*. And to the End that we might have Leisure to offer up our Praises and Thanksgivings to God, for that perfect Discovery he hath made of his Will to Mankind, in the Christian Revelation, which contains the best and surest Means of serving him, and of performing those Obligations we lie under to the divine Majesty, and which hath been confirmed by the Descent of the Holy Ghost; so the Church hath taken particular Care to set apart the two following Days, *viz. Monday* and *Tuesday*, for the Exercise of religious Duties.

The next is the Feast of the holy *Trinity* (being the Lord's Day next following) which was instituted *Anno Christi* 827, in Honour of the holy *Trinity*, by *Gregory* the Fourth, who then held the *Episcopal* Chair.

The *Thursday* next after is the Festival of the *Body of Christ*, commonly called *Corpus Christi* Day, which *Urban* the fourth, Bishop of *Rome*, instituted about the Year of Christ 1264.

The *Sundays* following this of the holy *Trinity*, are all of them called according to their numeral Order, whereby they succeed *Trinity Sunday*, until the first *Sunday* in *Advent*; they continually looking backwards towards the Mystery of the *Trinity*, till about the Mid-way, and then looking forward towards the *Advent* or coming of *Christ*.

Lastly, The four Lord's Days immediately preceding the Nativity of Christ, are called the *Sundays* in *Advent*, *ab adventu*

Domini in Carnam, i. e. from the coming of Christ in the Flesh ; and were instituted by the Church, to the End, that from the first of them, until the Nativity of our Saviour, our Minds might be prepared to a sober Life, and a pious Meditation of his Birth, then approaching ; alluding to that Passage in Isaiah xl. 3. Prepare ye the Way of the Lord, make straight in the Desert a Highway for our God.

Of the Fixed or Immoveable F E A S T S.

THE fixed, stative, or immoveable Feasts, are they, which notwithstanding they fall upon divers Days of the Week, yet they do not change, but always fall upon one and the same Day of the Month, and so have a fixed and certain Seat in the Calendar.

Of this Sort are,

1. *St. Andrew*, commemorated *November 30*. He was the Brother of *Simon-Peter*, and by Profession a *Fisherman*, yet an Apostle and Martyr ; and as he first came to Christ, and followed him before any of the other Apostles ; so he first appears among the Church Solemnities : His Day beginning the Order of the Service for all the other Saints Days in the Year ; because his Feast ever falls out to be either next before, or next after *Advent Sunday*, as bringing the first News of the coming of Christ. He preached in *Scythia*, and in the neighbouring Countries ; after that in *Cappadocia*, *Galatia*, *Bithynia*, and along the *Euxine Sea* : Lastly in *Thrace*, *Macedonia*, *Thessaly* and *Achaia*, where (in the Time of *Vespasian*) he was crucified by the Command of *Ageus*, Proconsul of *Achaia*, and buried at *Patris*, a City of *Achaia*, about the 80th Year of Christ.

2. *St. Thomas Didymus*, commemorated *December 21*, Christ's Apostle and Martyr. He preached to the *Parthians*, *Medes* and *Persians* ; also to the *Caramans*, *Hircans*, *Bactrians*, *Medes* and *Magicians* : And was slain by a Lance at *Calamina*, some say *Malapour*, a City of *India*, where he was honourably buried, *Anno Christi 35*, some say 25.

3. The Feast of Christ's Nativity, ordinarily called *Christmas-Day*, which, without all Doubt, was on the 25th Day of *December*, as has been, long since, fully proved by *Edward Fisher*, Esq; in his *Vindication of our Gospel Festivals*.

It was commonly called by the antient Saxons *Mærran*, [*Mærran*] says *Sir George Wharton* ; but with more Propriety *Mærræ* [*Mæsse*] as *Mr. Bailey* observes, signifying *Mass* ; and accordingly, with them, an holy Festival Day was called *Mærran dæg*, or *Mærræ dæg*, i. e. *Mass-Day*. In

In the Northern Parts of this Nation it is called *Yule*, which signifies a Time of Rejoicing and Festivity. By the Western or Latin Church, *Luminaria*, or the Feast of Lights, because they used many Lights and Candles at this Feast; or rather because Christ, the true Light, then came into the World. And this is the Body and Foundation of all other Christian Festivals, and ought to be celebrated accordingly.

4. St. *Stephen* (observed *December 26*) was the first Martyr, and was ordained one of the seven Proto-deacons, who were to take Care of the Treasure of the Church, and distribute it rightly to the Widows and the Poor. It was this St. *Stephen* who zealously refuted the erroneous Opinions of the *Jews*, concerning the Messiah, affirming *Jesus Christ of Nazareth*, to be the true one foretold by the Prophets; and being therefore accused of Blasphemy, was condemned and stoned to Death, by the *Jews*, at *Jerusalem*, *Anno Christi 35*.

5. St. *John* (observed *December 27*) the Brother of St. *James*, who was also an Evangelist, and the best beloved Apostle. He preached the Gospel in *Asia*, and founded the Churches of *Smyrna*, *Pergamos*, *Sardis*, *Philadelphia*, and *Laodicea*; but his chief Place of Residence was at *Ephesus*, where he wrote his Gospel. The Emperor *Domitian* ordered him to be put into a Caldron of boiling Oil, that he might be scalded to Death, but being miraculously preserved, he came out more lively and vigorous than when he was put in. The Emperor being disappointed thereat, was regardless of the Miracle, and exiled him into *Patmos*, an Island in the *Egean* Sea, where he wrote his Revelation, which was afterwards published at *Ephesus*, by *Gaius*, his Host and Deacon. After the Death of *Trajan*, he returned from *Patmos*, and remained at *Ephesus*, until he had lived 100 Years or upwards, where he died (as some say) of an Apoplexy, *Anno Christi 104*.

6. The holy Innocents of *Bethlehem*, celebrated *December 28*. These were slain by *Herodes Ascalonita*, otherwise called *Herod the Great*, in our Saviour's stead, though not for his Sake, to the Number of 14000, amongst whom, his own Son (as some Historians affirm) escaped not his (till then) unheard of Cruelty; which gave *Augustus Caesar* occasion to say, *Melius est esse Herodis Porcum quam Puerum: It is better to be Herod's Hog than his Son*.

7. The Circumcision of Christ, observed *January 1*, in Commemoration of the Mystery of his legal Circumcision, when he, who was the Truth and Substance, did at once fulfil and take away the Type thereof.

8. The *Epiphany*, or *Apparition*; or the Feast of *Twelfth-Day* after *Christmas*, observed *January 6th*; so called and celebrated in Memory and Honour of Christ's Manifestation, or Apparition made to the *Gentiles*, by a miraculous *Comet*, or Blazing Star, by virtue whereof he drew and conducted the three *Magi* or *Sages* (commonly called the three Kings) who, upon Sight of that Star, came out of the *East*, into the Country of *Palestine*, or *Jewry*, to adore him in the Manger, where (twelve Days after Christ's Birth) they presented him with *Gold*, in Testimony of his Regality; *Frankincense*, in Testimony of his Divinity; and *Myrrhe*, in Testimony of his Humanity.

Or, from the Holy Ghost's appearing in the Shape of a Dove, at Christ's Baptism, thirty Years after (for this 6th Day of *January* was the Day of his Baptism) and therefore it is also called by *Alcas Cyriacus*, in an *Arabic* Manuscript of Astronomical Tables, in the Archbishop's Archives in the *Oxford* Library (as the learned Dr. *Hammond* informed Sir *George Wharton*) The Feast of *Epiphany*, or Benediction of Waters; the Vigil whereof was of old called *Vigilia Luminum*, or the Eve of Lights, because the Ancients were then wont to send Lights, one to another; or, which is more probable, because they illuminated their Houses.

This Day was also celebrated by the Romans in Honour of *Augustus Cæsar*, for the Conquest of *Parthia*, *Egypt* and *Media*, which were thereupon added to the Roman Empire; wherefore the Church, willing to change that Solemnity for a better, instituted this of the *Epiphany*, in the room of it.

9. The *Conversion* of St. *Paul*, observed *January 26*, who in an extraordinary Manner (that is by a Light from Heaven, greater than the Brightness of the Sun) was converted to the Christian Faith, and made an Apostle of Christ, whom before that Time he had persecuted; as appears at large in the ninth Chapter of the Acts of the Apostles: He is commemorated on this Account, because it was, not only wonderful in itself, but a miraculous Effect of the powerful Grace of God, and therefore highly beneficial to the Church of *Christ*.

10. The Testification of Christ's true *Incarnation*, was by the Feast of the *Purification* of the blessed Virgin, observed *February 2*, when *Jesus* was presented in the Temple, and proclaimed by *Simeon* and *Anna* to be the *Messiah*. This Feast was instituted by *Justinian* the Emperor, *Anno Christi* 542.

11. St. *Matthias*, observed *February 24*, who being one of the seventy Disciples, was (after the Ascension) chosen an Apostle.

Apostle by Lot, in the room of *Judas* the Traitor: He preached the Gospel in *Judea*, and afterwards, as some think, he travelled Eastward, where he was first stoned by the *Jews*, for Blasphemy, and then beheaded after the Roman manner. *Anno Christi* 51.

12. The Feast of the *Annunciation* of the blessed Virgin, observed *March* 25, is kept in Remembrance of the Time when the *Angel Gabriel* declared our Saviour's Conception, or Incarnation by the Holy Ghost.

13. *St. Mark* the Evangelist, who penned the Life, Acts, Miracles, Death and Resurrection of our Saviour, and is commemorated on the 25th Day of *April*. He was the first Bishop of *Alexandria*, where he preached the Gospel, and also over all the bordering Regions, from *Egypt* to *Pentapolis*. At the same *Alexandria*, in the Time of *Trajan*, one of the Roman Emperors, he had a Rope tied about his Neck (some say Feet) by which he was drawn from the Place called *Bucolis*, unto another called *Augetis*, where he was burnt to Ashes by the furious Idolaters (against whom he preached) *Anno Christi* 63, and buried at *Bucolis*.

14. *St. Philip* and *St. James*, who are commemorated on the 1st Day of *May*, were both Apostles and Martyrs. There were two *Philips*, the one an Apostle chosen by Christ, the other a Deacon, he being one of the seven chosen by the Apostles. The first, *viz.* the Apostle, was of the City of *Bethsaida*, and probably a Fisherman, who preached the Gospel at *Phrygia*. The other, *viz.* the Deacon, was he, who converted the Eunuch *Candaules*, belonging to *Candace*, Queen of *Ethiopa*. He is by some said to have sent twelve Disciples into *Britain*, for Conversion thereof. But though this Day commemorates *St. Philip* the Apostle, in the Gospel, and *St. Philip* the Deacon in the Lesson, yet it was the Apostle whom the *Painims* laid hold on and crucified, under the Emperor *Claudius*, at *Hierapolis*, about the Year of Christ 53. No Account being transmitted about *Philip* the Deacon.

The latter, *viz.* *St. James* the Less, Son of *Alpheus*, was the Author of that excellent Epistle bearing his Name, and was for his Wisdom and Piety, surnamed the Just. After the Ascension of Christ he was created Bishop of *Jerusalem*, where (when he had governed that Church for the Space of thirty Years) he was first stoned, and afterwards set on a Pinnacle of the Temple, from whence he was precipitated or thrown down, and then (lying with his Thighs broken, and half dead, lifting up his Hands to Heaven, and praying for his

Murderers) knocked on the Head with a Fuller's Club, in the seventh Year of *Nero* the Roman Emperor, and in the ninety-sixth Year of his Age, about thirty-four Years after Christ's Ascension.

15. The Feast of *St. Barnabas*, observed on the 11th Day of *June*. He was by the Antients generally esteemed one of the seventy Disciples of our Saviour. It is thought he suffered *Martyrdom* at *Salamis*, a City in the Island of *Cyprus*, where the *Jews* being come from *Syria*, set upon him as he was disputing in the Synagogue; in a Corner of which they shut him up till Night, and then brought him forth; and after they had put him to exquisite Tortures, stoned him to Death, *Anno Christi* 49 or 50. He was afterwards buried by his Kinsman *Mark*, in a Cave not far distant from the City. The Remains of his Body are said to have been discovered in the Reign of *Zeno* the Emperor, *Anno Christi* 485, and *St. Matthew's Gospel*, written in *Hebrew* by *St. Barnabas's* own Hand, lying upon his Breast.

16. The Feast of the *Nativity* of *St. John the Baptist*, observed the 24th Day of *June* (Son of *Zachariah* and *Elizabeth*) who was of the Tribe of *Levi*. It was him that shewed to his Disciples the *Lamb of God*, the Son of the Father, that taketh away the Sins of the World. He was beheaded by *Herodes Antipas*, otherwise called *Herod the Tetrarch*, at the Request of *Herodias*, the Wife of his Brother *Philip*, *Anno Christi* 30, but it is his *Nativity* only which the Church celebrates.

17. *St. Peter* and *St. Paul*, observed the 29th Day of *June*. The first whereof was Chief of the Apostles, and preached the Gospel in *Pontus*, *Galatia*, *Cappadocia*, *Bitbynia*, and at *Rome*; where he was afterwards crucified under *Nero*, with his Head downward (at his own Desire) because he said he was not worthy to be crucified in the same manner with his Lord and Master, *i. e.* with his Head upward, and there also buried.

The latter, *viz.* *St. Paul* (who being called of Christ himself, after his Ascension, and numbered in the Catalogue of the Apostles) preached the Gospel from *Jerusalem* to *Illyricum*, and many other Cities in *Greece* and *Asia*; from thence to *Italy* and *Spain*; and lastly at *Rome*, where he was beheaded under *Nero*, *Anno Christi* 68, on the same Day that *St. Peter* was crucified, with whom he there lieth buried.

18. *St. James* the Greater, Brother to *St. John*, Son of *Zebedee*, an Apostle and Martyr, commemorated the 25th Day

Day of *July*. He preached the Gospel to the twelve dispersed Tribes; and also in *Spain*, where he is owned as their Tutelar Saint; and lastly, was slain by the Sword, or beheaded, by *Herod Agrippa*, Grandson of *Herod the Great*, in *Judæa*, *Anno Christi* 45, where also he was buried, and so consequently was the first of all the twelve Apostles in Christ's Kingdom.

A very remarkable Circumstance happened as this Apostle was led to the Place of his Martyrdom, which was this; his Accuser being enlightened by the Courage and Constancy *St. James* shewed at his Trial, repented of what he had done, and falling at the Apostle's Feet, heartily begged his Pardon for what he had testified against him: The holy Man, after a little Surprise, raised him up, and embracing him, said, *Peace be to thee*: Whereupon he publickly professed himself a Christian, and was beheaded at the same Time.

19. *St. Bartholomew* (commemorated *August* 24) who was Nephew (some say) and Heir to a King of *Syria*, yet both an Apostle and Martyr. He preached the Gospel to the *Indians*; afterwards, he preached in *Hierapolis* and *Lycaonia*: and lastly at *Albenople* in *Armenia the Great*, where by the Command of the Governor of that Place, he was the first Day beaten with Cudgels, and stoned; the next, crucified and excoriated, or flea'd alive, as he was fastened to the Cross. And, last of all (whilst Breath remained) beheaded, *Anno Christi* 51. Wherefore it is called *Duplex Festum*, or double Festival, some keeping it the 25th, as we the 24th of *August*, he suffering two Days together.

20. *St. Matthew* (observed *September* 21) who being a *Jew* by Birth, and a Publican or Toll-Gatherer by Profession, became a *Disciple*, an *Apostle*, an *Evangelist* and *Martyr*. He wrote the Gospel of Christ in the *Hebrew* Tongue, and delivered it to *James* the Brother of our Lord, then Bishop of *Jerusalem*. The same he preached in *Æthiopia*, where he was entertained by the Eunuch, Chamberlain to Queen *Candace*, whereof mention is made in the Acts of the Apostles, and prevailed so far, that *Æglippus* the King, and his People came to Baptism; but there reigning after him one *Hyrtacus*, who hated the Apostle, by his Command, he was run through with a Sword, or beheaded, in the Year of Christ 71.

21. *St. Michael* the Archangel, is he, who figured Christ, and with a Host of Angels fought for his Church, against the red Dragon, or the Devil, and his Angels; and is commemorated on the 29th Day of *September*.

22. St. *Luke* (observed *October 18*) born in *Syria*, by Profession a *Physician* of *Antioch*, an *Evangelist*, and the Penman of the *Apostles Acts*: He accompanied the *Apostles* in their *Peregrination*, but especially *St. Paul*, and died at *Ephesus* (some say by being hanged upon an *Olive Tree*) in the 84th Year of his Age, where also he was buried, *Anno Christi 74*; but many Years after translated, together with *Andrew* and *Timothy*, to *Constantinople*, in the Time of *Constantine*, Son of *Constantine* the Great.

23. St. *Simon Zelotes*, and St. *Jude*, the Brother of *James*, were both *Apostles* of *Christ*. They are commemorated on the 28th Day of *October*: The first of which was born in *Cana*, a Town in *Galilee* (being the Son of *Cleophas* and *Mary*, according to *Eusebius*, lib. 3, cap. 11) and preached the Gospel in *Egypt*, and *Persia*; whence he returned and succeeded St. *James* in the Bishoprick of *Jerusalem*, where he was crucified under *Trajan*, in the 120th Year of his Age; and so the last Martyr of all the *Apostles*.

The latter, viz. St. *Jude* (likewise called *Thaddæus* and *Lebbæus*) he preached the Gospel to the *Edeffæans*, and throughout all *Mesopotamia*: And was slain at *Berytus*, by the heathenish Priests of that Place, in the Time of *Agbarus*, King of *Edeffa*, where also he was honourably buried, *Anno Christi 51*.

24. Lastly, The Feast of *All Saints* (observed *November 1*) is dedicated to all *Christ's Apostles*, *Martyrs*, and holy *Confessors* in general.

Of the E M B E R W E E K S.

THE Ember Weeks are four in every Year, as may be seen in the Calendar; and anciently *Wednesday*, *Friday*, and *Saturday* in each, were fasting Days.

They are of great Antiquity in the Church, and called by the Latin Fathers *Quatuor Anni tempora*, the four times or Seasons of the Year. For (besides the first Institution of them, for quarterly Seasons of Devotion, proportioned to each Part of the Year, as the first Fruits of every Season, that the Whole, and each Division of it, might be thereby blest; and again, besides their Answerableness to the *Jejunia quatuor*, or solemn Days of Fasting among the *Jews*, before-mentioned, that we *Christians* may not be inferior to them in that Duty) an admirable Use is assigned to them in the Church, in Imitation of the *Apostles*, *Acts* xiii. 3, *Who, when*
they

they had fasted and prayed, laid their Hands on Barnabas and Saul, and sent them away to preach the Gospel. Others think they are called *Ember Days*, or Days of Ashes, from the no less ancient than religious Custom of using Hair-Cloth and Ashes in Time of public Piety and Penance: Or from the old Custom of eating nothing on those Days till Night, and then only a Cake baked under the *Embers*, or Ashes, which was called *Panis subcineritius*, or *Ember-bread*.

Of the VIGILS, or FASTING EVES of FESTIVALS.

VIGIL, or *Eve*, in Church Chronology, is the Day before any Feast.

Though the civil Day begins at Midnight, yet the ecclesiastical or Scripture Day, begins at Six o'Clock in the Evening next preceding, and holds till Six o'Clock in the Evening the ensuing Day. Hence the Collect for every *Sunday* and *Holy Day*, by order of the Church, is to be read at the preceding Evening-Service; that is at Six o'Clock in the Evening next before, from which Time the religious Day was supposed to begin. And this first Part of the *Holy Day*, from Six o'Clock the Day before, was by the primitive Christians, spent in Hymns, and other Devotions, in their Churches; and being often continued till late at Night, was called *Vigil*, from *Vigilo*, I watch, or keep awake; or from *Vigilia*, a watching or keeping awake in the Night.

In the Apostles Days, and some Time after, when the poor Christians durst not appear in Public, because of the continual Snares, Treacheries and Persecutions of Tyrants, and the Enemies of their Religion, they were forced to meet in the Night Time for the Exercise of their Devotion. And in the first Church after the Times of the Apostles, when they stood not in fear of any Persecution, they publicly watched and fasted in their Churches, before great Festivals, but especially on the Eve of the Resurrection. Whence grew the Custom, both for Christian Men and Women, to watch and fast on the Eves of great Solemnities, in their Churches.

But forasmuch, as in Process of Time, these nocturnal and promiscuous Watchings, or Night Meetings, came to be so abused, that no Care could prevent the several Disorders and Irregularities which crept in among them, the *Vigils*, or Night Watches were prohibited; and the Fasts (which are now retained and kept on the Days preceding the greatest Festivals,

and observed as well as the holy Fast of *Lent*) instituted in their stead; howbeit, they are still called *Vigils*, as being the Name of a Duty therein. And this (as some say) was confirmed by *Innocent* the Third, about the Year of *Christ* 1210.

For the very Purpose of the Church of God (saith judicious *Hooker*) both in the Number, and in the Order of the Feasts, hath been, not only to preserve thereby, throughout all Ages, the Remembrance of Miseries heretofore sustained, and of the Causes in ourselves, out of which they have risen, that Men considering the first, might fear the other the more; but further also to temper the Mind, lest contrary Affections coming in place, should make it too profuse and dissolute; in which Respect it seemeth, that Fasts have been set as Ushers of Festival Days, for Prevention of those Disorders, as much as might be, wherein, notwithstanding the World always will deserve (as it hath done) Blame, because such Evil being not possible to be rooted out, the most we can do, is in keeping them low, and (which is chiefly the Fruit we look for) to create in the Minds of Men, a Love towards frugal and severe Life; to undermine the Palace of Wantonness; to plant Parsimony as Nature, where Riotousness hath been studied; to harden them whom Pleasure would melt; and to keep the Tumours under, which always Fulness breedeth, that Children, as it were, in the Wool of their Infancy, dyed with Hardness, may never afterwards change Colour. That the Poor, whose perpetual Fasts are necessity, may with better Contentment endure the Hunger which Virtue causeth others so often to chuse; and by the Advice of Religion itself, so far to esteem the above contrary, that they, which for the most Part do lead sensual and easy Lives; they which are not plagued like other Men, may, by a public Spectacle of all, be still put in Mind what themselves are. Finally, that every Man may be every Man's daily Guide and Example, as well by Fasting to declare Humility, as by Praise to express Joy in the Sight of God, although it hath herein befallen the Church, as it sometimes did *David*, so that the Speech of one may be truly the Voice of the other. *I wept and chastened myself with fasting, and that was turned to my Reproof. Psalm lxx. 10.*

OBSERVATIONS on such other HOLIDAYS as are mentioned in the NEW CALENDAR, but not regarded by the Church of ENGLAND.

1. **LUCIAN**, a Priest and Martyr, celebrated by the Roman Catholics *January* the 8th.

It is affirmed by some, that he was one of *St. Peter's* Disciples, and by him was sent into *France*, to preach the Gospel, where he suffered Martyrdom: By others, that he was a Presbyter of *Antioch*, and understood the *Hebrew* Tongue extremely well; by which Means he was enabled to compare and amend the several Copies of the Bible. However that be, we find that after long and severe Exercise in the Church, he was brought before *Galerius Maximianus* the Emperor, who was then at *Nicomedia*; and having made an Apology for the Christians, he was cast into Prison, where he was put to great Torture, and afterwards to Death.

2. **Hilary**, Bishop and Confessor, commemorated the 13th Day of *January*, by the Church of *Rome*.

He was Bishop of *Poitiers* in *France*, and a great Defender of the Catholic Doctrine against the *Arians*, for which being persecuted by their Party, he was banished into *Phrygia*, where it is said he died soon after.

3. **Prisca**, a Roman Virgin and Martyr, commemorated the 18th Day of *January*, by the Church of *Rome*.

She was a Lady who embraced the Christian Religion, and upon her Refusal to abjure it, and to offer Sacrifice to Idols, was extremely much tortured, and after having endured the same with a great deal of Patience, was beheaded in the Year of our Lord 47, under the Emperor *Claudius*.

4. **Fabian**, Bishop of *Rome*, and Martyr, commemorated by the Church of *Rome* the 20th Day of *January*.

He is said to have been a married Man, and was afterwards made Bishop of *Rome*, on the following Occasion, viz. At a Meeting of the Clergy for the Election of a Bishop of that See, it was agreed upon by them, to nominate some noble and worthy Personage of that City for that Purpose: *Fabian* (who was lately come out of the Country to reside in *Rome*) being present, a Dove flying from above, suddenly sat herself upon his Head; whereupon all the Congregation then present, with one Mind and Voice, chose him for their Bishop, in which Office he remained thirteen or fourteen Years, unto the Time of *Decius*, who commanded him, among other Christians,

Christians, to be put to Death, on the above-named Day, or thereabout, *Anno Domini* 250.

5. *Agnes*, a Roman Virgin and Martyr, who is commemorat'd by the Church of *Rome* the 21st of *January*.

She was a young Lady of noble Distinction, who suffered Martyrdom in the tenth general Persecution under the Emperor *Dioclesian*, in the Year of our Lord 306. She is said to have undergone her Persecution with the greatest Readiness, though not above fourteen Years of Age: And though the Executioner hew'd her Body with the Sword, in a very unmerciful Manner; yet she endured it with admirable Constancy, singing Hymns whilst Life lasted.

She is pictured with a white Lamb standing by her, because (as the Report goes) she appeared to her Parents in that Form, amidst a Vision of Angels, eight Days after her Execution, for which Reason the Roman Ladies, every Year, offer a white Lamb to St. *Agnes*, at her Altar. These, the Pope takes care to have fed in the finest Pasture; and when they are sheered, the Wool is sanctified, with which fine white Cloth is made, and then consecrated by his Holiness. With this Cloth *Palls* are made, and sent to every Archbishop, which they must purchase at a very exorbitant Price, before they can exercise any Authority within their own Districts.

6. *Vincent*, a *Spanish* Deacon and Martyr, commemorated by the Church of *Rome* the 22d Day of *January*.

When *Vincent* was at *Rome* with *Eusebius*, *Peregrinus*, and *Potentianus*, *Lucius Antoninus Commodus* then Emperor, commanded the People to sacrifice to *Hercules*, who, he said, was their Patron and Defender; but *Vincent*, with the other three, taught the People to believe in and worship God only; which the Emperor hearing of, ordered them to be apprehended, and compelled to sacrifice to *Hercules*, but upon their Refusal, were pressed to Death with great Leaden Weights.

7. King *Charles* the Martyr, solemnized on the 30th Day of *January*, by the Church of *England*.

He was King of *England*, and murdered by his Subjects in the Year of our Lord 1648, on the above Day, a Scaffold being erected before his Palace at *Whitehall* for that Purpose. His Royal Confort was a profest Papist, but himself liv'd and dy'd in the Principles of the Church of *England*, according to his own Declaration made upon the Scaffold immediately before his Death, as well as by his Writings.

Note, At the Bottom of the Calendar in the Month of *January*, there is a Direction, that the 6th Chapter of *Exodus*, which is the first Lesson in the Morning for *January* 30, is to be read only to Verse the 14th. The Mean-

ing of which is, That as the Subject Matter of Discourse concerning Moses, Aaron and Pharaoh, breaks off there, and the rest of the Chapter goes on with some Chronological Accounts not so instructive, the Compilers of the Common Prayer gave that Direction for that Breaking off accordingly. And though this happens upon the Martyrdom of King Charles I. and so is not read at all (except that Day fall on a Sunday) Yet when the Legislative Power shall think proper to remove the Observation of that Day, it will then be read as at first intended.

8. *Blasius*, Bishop and Martyr, celebrated on the 3d Day of February, by the Church of Rome.

What particular Place he was Bishop of, and where he suffered Martyrdom, is not known at present; or else the Account remains buried in some ancient Records not very easy to come at.

9. *Agatha*, a Sicilian Virgin and Martyr, commemorated by the Church of Rome on the 5th Day of February.

She was said to be very beautiful, which occasioned *Quintianus*, the Governor of a Province in *Sicilia*, to fall in Love with her, but for an ignoble End: But she withstood his base Designs, for which Reason, and also for not worshiping the Heathen Gods, he ordered her to be scourged and then imprisoned. — Not terrified at this, but persisting in the Christian Faith, she was afterwards put upon a Rack, which she endured with great Constancy; was next burnt with hot Irons, and had her Breasts cut off; after this she was again imprisoned; from whence some little Time after, the Governor sent for her again, imagining he should be able to bring her over to his own Terms, but she being already half dead, and supposing what it was that she was sent for, begged of the Almighty that he would release her, by taking her to himself, which Petition was heard, and she expired immediately, on the above Day.

10. *Valentine*, a Bishop and Martyr, celebrated on the 14th Day of February, by the Church of Rome.

He is said, on the Account of his Religion, to have been imprisoned at Rome, and delivered to the Care of one *Asterius*: This *Asterius* had a Daughter, who was blind, whom *Valentine* restored to Sight; and by that Means converted the whole Family. After he had been confined about a Year in Prison, he was ordered to be brought forth on the abovesaid Day, and publicly executed, which was done by beheading him, about the Year 271. He was possessed of very great Abilities, and was famous for his uncommon Love and Charity. Hence the Custom among the young Men and Maidens of chusing Valentines on this Day.

11. *David*

11. *David*, Archbishop of *Menevia* in *Wales*, commemorated on the 1st Day of *March*, by the Church of *Rome*.

He was Son of *Xantus*, Prince of *Wales*, by *Melearia* a Nun, and was Uncle to King *Arthur*; he was both learned and eloquent, and in his Life and Conversation very austere. He was made Bishop of *Caerleon* in *Wales*, from whence removing his See to *Minevia*, it was from him ever afterwards called *St. David's*. He built twelve Monasteries about the Place where he lived; sat sixty-five Years in his See, and died *Anno Christi* 642, aged 146 Years. He was canonized by Pope *Calixtus* the Second, about 500 Years afterwards.

12. *Cedde* or *Chad*, Bishop of *Litchfield*, observed by the Church of *Rome*, on the 2d Day of *March*.

He was made Bishop of that See by *Egfrid*, King of *Northumberland*, in the Absence of *Wilfride*, who was gone to *Paris* to be consecrated Archbishop of *York*, by whom a speedy Return was not expected. At last *Wilfride* returned, and then *Egfrid* was persuaded by *Theodorus*, Archbishop of *Canterbury*, to resign that See to him again; after which, he the said *Chad*, led a monastic Life at *Lestingeag*, till, by the same *Theodorus*, he was made Bishop of *Litchfield*, under *Wolfhere*, King of *Mercia*, whom he is said to have converted. He died *March* the 2d, 672.

13. *Perpetua Mauritania*, a Martyr, commemorated *March* 7, by the Church of *Rome*.

She was a Lady of Quality, and suffered Martyrdom about the Year 205, under the Emperor *Severus*. *St. Austin* says this Holyday was settled in his Time; and assures us that she gave Suck to an Infant at the Time of her Martyrdom.

14. *Gregorius Magnus*, i. e. *Gregory* the Great, Bishop of *Rome*, and Confessor, commemorated *March* 12, by the Church of *Rome*.

He is said to be of noble Parentage, and to have applied himself to Study very early. The greatest Part, if not the Whole of his Estate, he gave to the building and supporting of Religious Houses. In or about the Year 590, he was consecrated Pope, but always opposed the Title of Universal Bishop, as blasphemous and Antichristian. His Memory was every Year celebrated in *England*, when Popery had large Footing here, and perhaps may be so still by the Roman Catholics of the present Time, for sending *Austin* the Monk to convert the People, who at that Time were *Saxons*. He died about the Year 604, after having filled the Chair of *St. Peter*, fourteen Years, and left behind him many learned Books which are still extant.

15. *Edward*

15. *Edward*, King of the *West Saxons*, is by the Church of *Rome* celebrated on the 18th Day of *March*.

This *Edward* was the Son of King *Edgar*, who first reduced the Heptarchy into one Kingdom. He came to the Crown *Anno Domini* 975, aged about twelve Years, and enjoyed it about two or three Years, being murdered by the Order of his Mother-in-Law *Elfride*, at *Corf Castle* in *Dorsetshire*, whilst he was drinking a Cup of Wine, that her own Son *Ethelred* might come to the Throne.

From his being a Fovourer of the Monks, they made his Murder become a Martyrdom, which was appointed by Pope *Innocent* in the Year 1245, to be held yearly as a Festival.

16. *Benedict*, an Abbot, is commemorated by the Romish Church on the 21st Day of *March*.

He was born of an honourable Family in *Italy*, and being very devout, set up an Order of Monks, in or about the Year 529, which still bears his Name. The Monks of his Order tell us, that he was very remarkable for Self-Mortification, and that he would frequently wrap a Heap of Briars about him, and roll in them, to put a Stop to any inordinate Desires which at that Time should arise within him.

There is a famous Miracle related by St. *Gregory*, concerning him, which is this; When the *Goths* invaded *Italy*, they endeavoured to burn his Cell, and himself in it; but the Fire would only burn round him, without doing him the least Hurt; the *Goths* being enraged at this, flung him into a hot Oven, and then stopped it up; however the next Day they found him alive and unhurt.

17. *Richard*, Bishop of *Chichester*, was commemorated by the Church of *Rome*, *April* the 3d — but for what Reason, is at present hard to determine, there being no authentic Account of the same that I have yet met with.

18. St. *Ambrose*, Bishop of *Milan*, commemorated by the Church of *Rome*, *April* the 4th.

He was born about the Year 340. One Day as he was asleep in his Cradle, a Swarm of Bees settled upon it, by which some ventured to foretell his future Eloquence. Immediately after the Death of *Auxentius*, Bishop of *Milan*, he was made Bishop of that See, which he govern'd with great Vigilance and Piety, upwards of twenty Years, giving all his Mony to charitable Uses, and settling the Reversion of his Estate upon the Church. He died *Anno Domini* 396, aged fifty-seven Years, having first converted St. *Augustin*, and then baptized him in the Christian Faith, at which Baptism it is reported,

reported, that he (*extempore*) pronounced that divine Hymn called *Te Deum*, which, in the Church of *England*, is used every Morning immediately after the first Lesson.

19. *Alphege*, Archbishop of *Canterbury*, commemorated by the Church of *Rome* on the 19th Day of *April*.

He was an *Englishman* of noble Parentage, and led a holy but severe Life, which he began in his juvenile Years. He was first made Abbot of *Bath*, then Bishop of *Winchester*, and afterwards, in the Year 996, Archbishop of *Canterbury*. After this, the *Danes* pretended to lay claim to a Tribute, which they said was due to them from the Archbishop, which he refused to pay, for which Reason they sacked and burnt the City and Church of *Canterbury*. Nine Parts in Ten of the People they put to the Sword; put the Archbishop in Prison for seven Months, and then stoned him to Death at *Greenwich*, after which he was canonized for a Saint and Martyr, by the Pope, who directed the aforementioned Day to be observed as his Festival.

20. *St. George the Martyr*, observed by the Church of *Rome* on the 23d Day of *April*.

He was born at *Cappadocia*, and was martyr'd for being a Christian, in the Year 290, under *Dioclesian* the Emperor, whom he served in the Army: *Dioclesian* being angry with the Christians, published an Edict against them, which he caused to be put upon the Church Doors; but *George* not wanting Courage and Resolution, pull'd it down again, for which he suffered as above. How he came to be the tutelar Saint of *England* is supposed to arise from the following Account.

Robert, the Son of *William* the Conqueror, who was Duke of *Normandy*, was a Christian, and being at War with the *Turks*, laid Siege to the City of *Antioch*, but a large Army of *Saracens* appearing, had like to have saved it, had it not been for *St. George*, who with a much greater Army of Christians, coming down from the Hills in *White*, joined with *Robert*, and put the Infidels to Flight, by which Means the Christians possessed themselves of the City,

21. *The Invention of the Cross*, commemorated on the 3d Day of *May*, by the Roman Catholics.

This is one of the fabulous Stories of that lying Church, and runs thus;

Helena, who was the Mother of *Constantine* the Great, having dream'd that she was to go to *Jerusalem*, and search there for the Cross of *Christ*, went accordingly, and when arrived

arrived in that City, procured Labourers to dig at *Golgotha*, where, after much Trouble, they found three Crosses, and brought them to *Helena*, who presently conjectured they were the very Crosses on which our Saviour and the two Thieves were crucified. However, not being able to determine which was the Cross of *Christ*, she ordered a dead Body to be put to each of them; two of them producing no Effect, the dead Body revived at the third, which entirely convinced her, that *that* was the Cross sought for.

As soon as the Miracle became public, every body was desirous of having a Piece of it, that it might be preserved as a precious Relique, whereby, in the Time of *Paulinus*, Bishop of *Nola*, in the Year 420, it appeared that the Quantity of Reliques, when put together, made more Wood than the original Cross was made of; to solve which Difficulty we are inform'd by that Father, that it was increased miraculously.

22. *St. John the Evangelist*, ante portam Latinam, celebrated by the Church of *Rome* on the 6th Day of *May*.

St. John the Evangelist being intended to be made a Sacrifice to the Rage of the Emperor *Domitian*, was put into a Caldron of boiling or burning Oil, as has been before related, before the *Porta Latina*, but was miraculously delivered from the same, by which Means he had the Honour of Martyrdom, without enduring the Torments of it. Hence the above-named Day was celebrated in Memory of that Evangelist.

23. *Dunstan*, Archbishop of *Canterbury*, has by the Church of *Rome*, the 19th Day of *May* consecrated to him.

He is said to have been nearly related to King *Athelstan*; and by his superior Knowledge in the Arts and Sciences of those Times, was thought to be a Conjuror; however he was canoniz'd for a Saint. He was Confessor to four Kings of the *West Saxons* successively; and being stout in the Cause of *Christ*, was fearless in reproving any of them.

By King *Edgar* he was promoted to the See of *Worcester*, then to *London*, and after that to *Canterbury*, in which See he sat twenty-seven Years, and deceased on the abovesaid Day, *Anno Domini* 988.

24. *Augustine*, first Archbishop of *Canterbury*, has the 26th Day of *May* dedicated to him, by the Church of *Rome*.

When Pope *Gregory* the Great was minded to convert the *Saxons*, he sent over the just named *St. Augustine* for that Purpose, from whence he obtained the Name of the Apostle of the *English*. During his Residence in *England*, he was made Archbishop of *Canterbury*, in the Year 596, and died *May* 29, 610.

25. *Venerable*

25. *Venerable Bede*, a Presbyter or Priest, celebrated on the 27th Day of *May*, by the Church of *Rome*.

He was born at *Yarrow* in *Northumberland*, Anno 673, and was educated, among other Branches of Literature, in the *Greek* and *Latin* Languages, wherein he succeeded beyond most of his Age, and left several Philosophical and Mathematical Tracts behind him, together with his celebrated Ecclesiastical History of the *Saxons*.

Being only a Monk, he had a Cell allotted him, in which he studied so many Hours every Day, that it was reported he never went out of it. However that was, it is certain no Preferment at *Rome* could prevail upon him to leave it. The Name *Venerable* was given him on the Account of his Learning and Piety.

26. King *Charles* the Second, his Nativity and Return, commemorated on the 29th Day of *May*, by the Church of *England*.

On this Day King *Charles* the Second was born, and on the same Day many Years after, he was restored to the Throne of *England*, after a long Train of Afflictions, occasioned by those wicked Regicides, who had been the inhuman Instruments of putting his Father to Death.

27. *Nicomede*, a Roman Priest and Martyr, is commemorated on the 1st Day of *June*, by the Church of *Rome*.

He is said to have been one of *St. Peter's* Disciples, and by his having the Courage to bury the Remains of one *Felicula*, a Martyr, was discovered to be a Christian.

At last he was martyr'd himself, for his Religion, being beaten to Death with Leaden Plummets, in the Reign of the Tyrant *Domitian*.

28. *Boniface*, Bishop of *Mentz*, and Martyr, commemorated on the 5th Day of *June*, by the Church of *Rome*.

He was born in *England*, being at the first called *Winifrid*. Pope *Gregory* the Second sent him into *Germany*, to convert that People, and so he obtain'd the Name of the Apostle of *Germany*. He succeeded to the See of *Mentz*, in the Year 745, being one of the most considerable Men of his Time, and also a great Admirer of *Bede*. While he was in *France*, extending the Kingdom of Christ, he was murdered by the Populace, at or near *Utretch*, in the Year 755.

29. *St. Alban*, Martyr, celebrated on the 17th Day of *June*, by the Church of *Rome*.

Amphialus, a Priest of *Caerleon* in *Wales*, being persecuted, fled into *England*, and met *St. Alban* at *Verulam* in *Hertfordshire*,

shire, who entertain'd him secretly. But soon after, a strict Search being made for *Amphialus*, St. *Alban* contrived his Escape, which the Pagans highly resented; wherefore to be revenged on him for so doing, they endeavoured to make him sacrifice to their Idols, but he would not, for which Reason they put him to Death.

30. *Translation* of *Edward*, King of the *West Saxons*, observed by the Church of *Rome*, on the 20th Day of *June*.

He was murdered by his Mother-in-Law, as before observed, p. 39, and then buried privately at *Warham*; but three Years after, Duke *Alferus* caused him to be carried to *Shaftsbury*, where he was interred with great Pomp on the abovesaid Day.

31. *Visitation* of the Blessed Virgin *Mary*, observed by the Church of *Rome*, *July* the 2d.

Sacred Writ (*Luke* i. 39.) informs us of a Journey into the Hill-Country, made in Haste by the Virgin *Mary*, to visit her Cousin *Elizabeth*, who was then great with Child of *John* the Baptist. This famous Journey was thought on by Pope *Woban*, who instituted a Feast in Honour of it; the End of which was, that he might obtain her Intercession, in order that the Schisms made by the *French* and *Italians* might be removed.

32. The *Translation* of St. *Martin*, Bishop and Confessor, commemorated on the 4th Day of *July*, by the Roman Catholics.

He was born in *Pononia*, and bred up a Soldier; afterwards he went into sacred Orders, and at Length was consecrated Bishop of *Tours* in *France*. His Enmity to Paganism was manifested by his throwing down their Heathen Images and Altars, whenever they came in his Way. He sat twenty-six Years in that See, and deceased *Anno Christi* 400.

His Helmet (for in those Days Helmets were worn in the Field of Battle) was so much valued by the *French*, that they carried it with them into the Field, which being placed on High, served to animate their Soldiers in order to obtain a Victory.

33. *Swithun*, Bishop of *Winchester*, translated on the 15th Day of *July*, and therefore that Day is held sacred to him by the Church of *Rome*.

There was at that Time a Convent in *Winchester*, of which St. *Swithun* was first a Monk, and afterwards a Prior. When *Helinstan*, Bishop of that See died, by the Favour of *Ethelwolph* St. *Swithun* succeeded him, *Anno Domini* 852; in which See
he

he sat eleven Years, and then died. By his Will he directed that he might not be buried within the Church (it being customary at that Time to bury Bishops in the Church) but in the Church-yard. However, it is said a Translation was made of his Remains (but where we know not) and a Chapel built over his Grave.

34. *Margaret*, Virgin and Martyr at *Antioch*, who is celebrated on the 20th Day of *July*, by the Church of *Rome*.

She was the Daughter of an Heathen Priest, and born at *Antioch*. *Olybius*, a Heathen Roman, would have married her, but perceiving her to be a Christian, declined it, endeavouring in the mean Time to bring her over to the heathenish Religion again: But finding her strong in the Faith of *Christ*, and consequently himself unable to overthrow her by Argument, he used her very cruelly, and then put an End to her Pain, by taking off her Head, *Anno Christi* 278.

She is invoked by the Roman Catholics to assist Women in the Time of their Labour.

35. *St. Mary Magdalene*, commemorated on the 22d Day of *July*, by the Church of *Rome*.

It has been a Doubt with some, especially the last Compilers of the Common Prayer, whether this *Mary Magdalene*, was the same with her mentioned in the 7th Chapter of *St. Luke*, v. 37, &c. and therefore, though this Day was celebrated according to the Common Prayer Book, in the Time of *Edward VI.* yet the last Reformers thought proper to discontinue the Service, and only left her Name in the Calendar.

36. *St. Anne*, Mother to the Blessed Virgin *Mary* celebrated on the 26th Day of *July*, by the Roman Catholics.

This Day is set apart by the Roman Catholics for nothing that we know of, but, the Birth of *St. Anne*.

37. *Lammas-Day*, celebrated by the *Roman Catholics*, on the 1st Day of *August*.

Many Papists had a foolish Conceit that *St. Peter* was the Patron of the Lambs and Sheep, because our Saviour said to him, feed my Lambs, and feed my Sheep; and therefore they thought that the Mass celebrated on this Day was serviceable to their Lambs and Sheep, by making them thrive. It is also said to be observed upon the Account of *St. Peter's* Imprisonment, and known by the Name of *St. Peter in the Fetters*. But however all this is, there are some People, who, perhaps with greater Probability, derive the Expression from an ancient *Saxon* Word, signifying Loaf-Mass; because the *Saxons* used

used on that Day, to offer to their Deities, some new Loaves made of the first Fruits of their new Wheat.

38. *Transfiguration of our Lord*, has the 6th Day of *August* dedicated to it by the Church of *Rome*.

This was instituted by Pope *Calixtus*, *Anno Domini* 1455, and therefore, of late Date, among the Roman Catholics; but whether this was really the Day on which our Saviour was transfigured on the Mount, *Matt.* xvii. 2, is at this Time very hard to affirm.

39. *Name of Jesus*, hath the 7th Day of *August* dedicated to it; but by whom, or for what Reason, no body can determine. Formerly it was said to be dedicated to one *Afra* of *Crete*, who was converted by *Narcissus*, Bishop of *Jerusalem*, and was martyr'd on this Day.

40. *St. Laurence*, Arch Deacon of *Rome*, and Martyr, celebrated on the 10th Day of *August*, by the *Roman Catholics*.

He was born in *Spain*, and in Length of Time, was made Arch Deacon and Treasurer of the Church of *Rome*, under Pope *Sixtus*, about the Year 259.

In the Time of *Valerian* the Emperor, *Sixtus* was persecuted, and the Soldiers using him very severely, occasioned *St. Laurence* to abide by him, even to the Place of Execution.

Not long after the Death of *Sixtus*, the lowest Part of the Pagans accused *Laurence* of secreting the Treasure of the Church, because he did not deliver it up to them; for which Reason they laid him on a Gridiron, and broil'd him over a slow Fire, during which Time, his Behaviour was remarkably courageous and resolute; for having laid some Time on one Side, he called to his envious and inhuman Tormentors, to turn him on the other Side, that being broil'd enough; adding, that he received more Comfort than Pain; for however great his Pain might be, arising from the Fire; his Comfort was abundantly greater by his dying for the Cause of Christ.

In after Ages, the Empress *Pulcheria* built a Temple in Memory of him, which was afterwards enlarged by *Justinian*, or wholly rebuilt by him. In this Church, it is said, was preserved the aforementioned Gridiron, which the too credulous *St. Gregory* affirmed to have been productive of many Miracles.

41. *St. Austin*, Bishop of *Hippo*, Confessor and Doctor, has the 28th Day of *August* dedicated to him.

His Birth-Place was at *Togalle* in *Numidia*, a Province in *Africa*, *Anno Christi* 354. At first he is said to have studied
Poetry,

Poetry, Plays, Rhetoric and Philosophy, in which he became a Professor at *Rome*, and next at *Milan*. During his Studies at *Milan* he became acquainted with *St. Ambrose*, and was by him instructed in Divinity, which he here studied. About the Year 391, he was consecrated Bishop of *Hippo*, which See he filled with Honour, being a judicious Divine: and died *Anno Domini* 430, aged 77 Years.

42. *Beheading of John the Baptist*; a Romish Festival, celebrated on the 29th Day of *August*.

At first it was called, *The Feast of gathering up the Relics of St. John the Baptist*, but afterwards the Feast of his *Beheading*.

In the 4th Century, some of his Remains were said to be productive of several Miracles; at the hearing of which, *Julian* the Apostate, order'd them to be burnt, but some of them were secretly preserved. In the Time of the Emperor *Valens*, his Head was found, or said to be so, and as a precious Relic, carefully placed in the Church at *Constantinople*.

43. *Giles*, Abbot and Confessor, has the 1st Day of *September* dedicated to him.

He was born an *Athenian*, and being brought up in the Christian Religion, disposed of his Patrimony to charitable Uses. He travelled into *France* in the Year 715, and lived two Years with *Cæsarius*, Bishop of *Arles*; after which he led a Hermit's Life, till an Abby was built for him at *Nismes*, by the King of *France*, of which he was made Abbot. He departed this Life *Anno Domini* 795.

44. *Fire of London*, observed *September* 2d, by the Inhabitants of *London* only.

It broke out at a House in *Pudding-Lane* on *September* 2d, 1666, on a *Saturday* Night, about Midnight, and in three Days consumed 13200 Houses (which composed 400 Streets) the Cathedral Church of *St. Paul*, 86 Parish-Churches, 6 Chapels, *Guildhall*, the *Royal Exchange*, *Custom-House*, *Blackwell-Hall*, 52 of the Company's Halls, 3 City Gates, 4 Stone Bridges, and the Prisons of *Newgate* and the *Fleet*; also the *Poultry* and *Woodstreet* Compters; all which stood on 436 Acres of Ground; the Loss of which amounted to upwards of 10730500*l*. 6 Persons only perishing in the Flames. Afterward this City was rebuilt, and on that House where the Fire began, was by Authority the following Inscription.

Here by Permission of Heaven, Hell broke loose upon this Protestant City, from the malicious Hearts of barbarous Papists, by the Hand of their Agent Hubert, who confess'd, and on the Ruin of this Place declared the Fact for which he was banged, viz. That
here

here began the dreadful Fire, which is described and perpetuated on and by the neighbouring Pillar [Monument] erected Anno 1680, in the Mayoralty of Sir Patience Ward, Knt. This Inscription has some Time since been taken away.

45. *Enurchus*, Bishop of Orleans in France, has the 7th Day of September dedicated to him, by the Roman Catholics.

He was present at the Council of Valencia, Anno Domini 375; and we are informed that within the Space of three Days he converted 7000 Infidels to the Christian Faith.

46. *The Nativity of the Blessed Virgin Mary*, is a high Festival among the Roman Catholics, and solemnized on the 8th Day of September.

It is affirm'd that a Choir of Angels were heard singing in the Air on that Day, and therefore in after Ages, it was appointed by the Church of Rome to be kept holy, but the Truth of the Affirmation is very much to be doubted.

47. *Holy Cross-Day*, sometimes called Holy-rood Day, observed by the Roman Catholics on the 10th Day of September. The Occasion of it is as follows; viz.

In the Year 615, *Cosroës* King of Persia, plundered Jerusalem, and among other Things, carried away a Piece of the Cross, which *Helena* had left there: And when in his Cups, or otherwise merrily disposed, would always divert himself with that and the holy Trinity. After this *Heraclitus* the Emperor commenced a War against him, and defeated him; by which Means he recovered the Piece of the Cross, and brought it back again in Triumph to Jerusalem; but instead of entering the City, he found the Gates shut against him, not by the Contrivance of Man, but by the Arm of Heaven (if you will believe it) and heard a Voice which said, *the King of Kings did not enter into that City in so stately a Manner, but meek and lowly, riding upon an Ass*. Whereupon the Emperor immediately left his Horse, and (for want of an Ass) went into the City barefoot, carrying the Wood of the Cross upon his Shoulder, which gave Rise to this Festival: which ought to be laugh'd at by every honest Protestant.

48. *Lambert*, Bishop and Martyr, a Festival held on the 17th Day of September in Honour of him.

He was, in the Time of King *Pepin I.* Bishop of Utrecht; and observing some Lewdness in the King's Grandson, reproved him for it, for which Reason one of his Concubines murder'd the good Bishop herself, or order'd him so to be served. *Robert*, Bishop of Leeds, procured this Day to be solemnized with a Festival in Honour of him, Anno Christi 1240.

49. *St. Cyprian*, Archbishop of *Canterbury*, and Martyr, has the 26th Day of *September* dedicated to him.

After he was converted from Idolatry, he gave all his Riches to the Poor; and having been made Bishop of *Carthage*, *Anno Domini* 248, sat in that See ten Years, and then suffered Martyrdom.

50. *St. Jerome of Prague*, Confessor and Doctor, has the 30th Day of *September* dedicated to him.

In his Youth he discover'd great Parts, and was sent to *Rome* to study Rhetoric, where he behaved so well, as to gain the Favour of Pope *Damascus*, and be made his Secretary. Here it was that he was converted and baptized; after which he studied Divinity, and made himself Master of the *Hebrew* Language. The greater Part of his Time by far, he spent at *Bethlehem*, in close Retirement, and hard study, where, it is said he translated the Bible. He died *Anno* 422, aged 80 Years.

50. *Remigius* Bishop of *Rhemes*, has the 1st Day of *October* dedicated to him, probably upon Account of his Death.

He stands recorded for Learning and Piety; and converted *Clodoveus*, the then King of *France*, together with a great Part of his Kingdom, for which he is styled the Apostle of *France*. He held his See seventy-four Years with Honour, and died in the 96th Year of his Age, *Anno* 535. A certain Cruse, which he used to put Water in, is to this Day preserved; out of which the Kings of *France* are usually anointed at their Coronation.

52. *Faith*, Virgin and Martyr; commemorated on the 6th Day of *October* by the *Roman Catholics*.

Her Birth-place was *Pais de Gavre* in *France*, she was persecuted about the Year 290, and suffered very cruel Torments, and at last Death itself for the Sake of *Christ*.

53. *St. Denys* the Areopagite, Bishop and Martyr, commemorated on the 9th Day of *October*, by the Church of *Rome*.

He was converted by *St. Paul*, while he was at *Athens*, his Name then being *Dicnysius*, as mentioned *Acts* xvii. 34, but for what Reason it was afterwards changed, is not easily known, except by Corruption. After he was converted, he made Divinity his Study, in which he succeeded so well, as after he had entered into holy Orders, to be made Bishop of *Athens*, at which Place, for the sake of *Christ*, he chose to become a Martyr. In *France* he is admitted as the Tutelar Saint of that Kingdom, he being the first that preached the glad Tydings of the Gospel there.

54. *Translation of King Edward the Confessor*, celebrated on the 13th Day of *October*, by the *Roman Catholics*.

He was the youngest Son of King *Ethelred*, and came to the Crown of *England*, Anno 1042. During his Reign, he was very industrious to have wholesome Laws, and therefore collected all the most useful of the *Danish* and *Saxon* Laws that he could meet with, and incorporated them among the Laws of *England*. By him was settled that Collection called* *Peter-Pence*, for which he obtained of the Pope, then in being, the Character of Confessor. Many Miracles were said to be done by him and his Vestments together, which by the Monks are (if they have any of them) esteemed holy. His Crown, Chair, Staff, Spurs, &c. are all of them used at the several Coronations of our Kings of *England*.

* Note, It was called *Peter-Pence* because made on the 1st Day of August, called St. Peter ad vincula, or St. Peter in the Fetters aforementioned, by every House paying a Penny, which was said to be for the Use of the English School, or College, at Rome. It was prohibited by King Edward the Third: Afterwards, in a succeeding Reign it was revived: but at last it was wholly abrogated by Queen Elizabeth, in the first Year of her Reign.

55. *Etheldred*, a Virgin, has the 17th Day of *October* dedicated to her, by the Church of *Rome*.

She was twice married; first to *Torfbert*, a Nobleman in *Lincolnshire*, and after his Death to King *Egfrid*, Anno 671, or thereabout, without being known by either of them; she having Pretensions to a holy Life. After staying twelve Years at Court, she obtain'd Leave to go to the Abbey at *Coldingham*, in the County of *Mers* in *Scotland*, where she became a Nun, under the Direction of the Abbess *Ebba*, Daughter of King *Ethelfrida*. After this she caused an Abbey to be built at her own Expense, of which she became Abbess herself, and died and was buried there.

56. *Crispin*, Martyr, who stands commemorated on the 25th Day of *October*, by the *Roman Catholics*.

He was born at *Rome*, and by Trade a Shoemaker. *Crispin* with his Brother *Crispianus*, who was of the same Trade, travelled from *Rome* to *Soissons* in *France*, about the Year 303, to enlarge the Kingdom of Christ, by preaching his Doctrine. Like St. Paul, they work'd at their own Trade for a Maintenance, that they might not be chargeable to others. However, the Governor of the Town, having no Relish to the Christian Religion, laid Hands on them, and order'd them to be beheaded.

The Shoemakers in *England*, of what Religion soever, and very likely in all *Romish* Places, choose him for their Tutelar Saint.

57. *All Souls*, commemorated on the 2d Day of *November*, by the Church of *Rome*. This is not mentioned in our *Calendar*, but only in some of our *Almanacks*; and therefore for the Oddity of it, I have inserted the Story, which runs thus.

A certain Monk went to pay a Visit to *Jerusalem*, and in his Return Home, his Curiosity led him to see Mount *Ætna*, which, by some, was imagined to be the Mouth of Hell. When he arrived there, he heard a horrid Noise; but however could easily distinguish the Complaints which several Devils made there, of many Souls, when delivered into their Custody, were taken from them again by the Prayers of some Monks. When he came Home, he related this Affair to an Abbot of his Acquaintance, who from that Time order'd the abovesaid Day to be annually kept in his Monastery, and Prayers to be offered up for all departed Souls. This coming to the Pope's Ear, he afterwards order'd it to be observed as a solemn Festival. *This is one of the Deceits of the Church of Rome, from which I hope God Almighty will always keep us.*

58. *Gunpowder Plot*, observed on the 5th Day of *November*, by the Church of *England*.

This was one of the wicked Contrivances of the Roman Catholics, in the Time of King *James I*, to destroy at once both the King, and the two Houses of Parliament, in full Assembly. *Catesby* was at the Head of this Hellish Body, and *Guy Fawkes*, was to have set Fire to the Train; thirty-six Barrels of Gunpowder being conveyed under the House of Lords for that Purpose.

Note, The Kingdom of England has received several very signal Deliverances from Papal Tyranny; would to God the People may make a right Use of those Deliverances, by adhering more strictly to the Principles of that Church in Opposition to the Church of Rome.

59. *Leonard*, Confessor, has the 6th Day of *November* dedicated to him by the Roman Catholics.

He was first made *Bishop* of *Rhemes*, and afterwards of *Limosin*; both of them in *France*; and obtained of *Clodius*, then King of *France*, and the second King, the Liberty of setting such Prisoners free, as he should think fit to visit. Upon the which, he spared no Pains (for the sake of the Christian Religion) of visiting all that were under any Confinement, by which Means, in all Probability, he gain'd many Profelytes to Christ, as well as a Remittance from their Imprisonment. He deceased about the Year 500, and 'tis said

said has been, and likely is still acknowledged by the *Roman Catholic* Prisoners, as their Tutelar Saint.

60. *St. Martin*, Bishop and Confessor; his Death is commemorated on the 11th Day of *November*, by the *Roman Catholics*, and is called *Martin-Mass*; see No. 32, on the 4th of *July* foregoing.

61. *Britius*, Bishop, has the 13th Day of *November* dedicated to him by the Church of *Rome*.

He succeeded *St. Martin* in the See of *Tours*, about the Year 432. The Occasion of this Day being devoted to him, might probably proceed from his Decease on the same Day.

62. *Machutus*, Bishop, is commemorated on the 15th Day of *November*, by the Church of *Rome*.

He was Bishop of *St. Maloes* in *France*, and is said to have wrought many Miracles; but we are not obliged to believe all that the *Roman Catholics* say. He lived about the Year 500, and very likely has the abovesaid Day dedicated to him as the Day of his Death.

63. *Hugh*, Bishop of *Lincoln*, has the 17th Day of *November* dedicated to him by the *Roman Catholics*.

He was a Man famous for Abstinence and Austerity; and was made Prior of the *Carthusian* Convent at *Wittenham* in *Somerseſshire*, and afterwards Bishop of *Lincoln*, both by King *Henry* the Second. Being under an Obligation of coming up to *London* in 1200, he was seized with a *Quartan* Ague, of which he died on the Day above-mentioned. His Remains were laid in the Cathedral at *Lincoln*, with a great deal of Pomp and Solemnity. About twenty Years afterwards the Appellative *Saint* was given to him at *Rome*; and about sixty-two Years after that his Body was put into a Silver Shrine.

64. *Edmund*, King and Martyr, has the 20th Day of *November* dedicated to him.

He was King of a People called the *East Angles*, including *Norfolk*, and the neighbouring Parts, in *England*. The *Danes* making some Incurſions in his Territories, gave him and his People a great deal of Trouble: At Length, finding it not in his Power to overcome them, he made an Offer of himself to them, if they would let his Subjects remain in Peace; but the *Danes* perceiving their Strength to be greater than his, rejected his Offer; and as soon as they became Conquerors, made *Edmund* their Prisoner. The next Attempt was to bring him over to their Religion (he being a Christian, and they Idolaters) but on his refusing, they beat him severely;

then he was scourged; and last of all they shot him to Death with Arrows. His Body was buried at *St. Edmund's Bury* in *Suffolk*, which Town, in Process of Time, derived its Name from him, it being only called *Bury* before.

65. *Cecilia*, a Virgin and Martyr, has the 22d Day of *November* devoted to her Service, by the Church of *Rome*.

She was a Roman Lady, and a Christian. Being persecuted, she was required to renounce her Religion, but having Courage enough to refuse their Demand, and acknowledge Christ for her Saviour, she was put into a large Vessel of boiling Water, in which she expired. Yet there are some who say she was suffocated in a warm Bath, the Air being shut out. She fell a Sacrifice to the Enemies of the Christian Religion *Anno 225*, probably on the abovesaid Day.

66. *St. Clement I.* Bishop of *Rome*, and Martyr, has the 23d Day of *November* dedicated to him by the Church of *Rome*.

He was by Birth a Roman, and a very early Bishop of that Place, being one of the first of them; which See he held about seventeen Years. His Writings were very much esteemed by the Primitive Christians. Being persecuted for his Religion, he was condemned to the Mines, there to hew Stones; but this being thought not Punishment enough, inasmuch as he preached the Gospel to the rest of the Miners; he had an Anchor fastened to his Neck, with which he was thrown into the Sea and drowned.

67. *Catherine*, Virgin and Martyr, has the 25th Day of *November* consecrated to her, by the Church of *Rome*.

She was born at *Alexandria*, and brought over to the Christian Religion about the Year 305, which she professed with the utmost Resolution. Her Courage was so great, that she durst openly reprove the idolatrous People, for their Sacrifices, and upbraided the Emperor *Maxentius* to his Face, for his Cruelty; for all which she was condemned to die, by having a great Wheel, stuck full of Spikes, with the Points outward, rolled over her Body; which very likely gave Birth to what is now commonly called the *Catherine-Wheel*.

68. *Nicolas*, Bishop of *Myra* in *Lycia*, is commemorated on the 6th Day of *December*, by the Church of *Rome*.

He was remarkable for his great Charity; and the following Narrative will sufficiently discover him to have been such an one. A certain Man having three Daughters, who were young Women, was fallen to decay; and not knowing immediately what Course to take for an honest Livelihood; the Girls were tempted to prostitute themselves, that they might thereby

thereby maintain themselves and their Father. The good Bishop hearing of this, ordered a Sum of Mony to be given to the Father, that they might live virtuously.

69. *Conception of the Blessed Virgin Mary*: She is commemorated on the 8th Day of *December*, by the Church of *Rome*.

When the Fleet of *William* the Conqueror had been at Sea in a Storm, and come safe home again, then it was, and upon that Occasion, that *Anselm*, Archbishop of *Canterbury*, instituted this Festival.

70. *Lucy*, Virgin and Martyr, celebrated on the 13th Day of *December*, by the Church of *Rome*.

She was a young Lady of *Syracuse*, who preferred a Virgin State to that of Matrimony. Being solicited by a young Gentleman to become his Wife, she refused him; and to avoid any further Addresses, gave her Fortune to the Poor; at which being greatly vex'd, he went to a Heathen Judge, and accused her of being a Christian. The Judge ordered her to be dishonoured in a Brothel-House (such being allowed by Law) but in her Way thither, she so provoked the Officers by struggling with them, that they used her very barbarously, and then killed her, about the Year 305.

71. *O Sapientia*, *December* 16.

This Day, and the following, to *Christmas-Eve*, were consecrated by the Church of *Rome*, to the Honour of the Advent of *Christ*; hence a Latin Anthem, beginning with *O Sapientia*, used to be sung on those Days; the first Day beginning as above.

72. *Silvester*, Bishop of *Rome*, has *December* 31st dedicated to him by the Church of *Rome*.

He came to the See of *Rome* in the Year 314, and is said to have invented several Rites and Ceremonies, which are now practised, such as *Afylums*, *Unctions*, *Palls*, *Corporals*, *Mitres*, &c. He went off the Stage of Life Anno 334.



Miscellaneous Arithmetic :

OR A FULL

ACCOUNT of the NEW CALENDAR, &c.

PART II.

A

D I S S E R T A T I O N

C O N C E R N I N G

Years, Months, Weeks, Days, Hours,
Minutes and Seconds ;

And the Manner of their being settled in the
World, for the better Computation of Time.

I. Of the Y E A R.

 **Y E A R** is the principal and most ordinary Part of Time, whereby not only the Ages of Men, of the World, and of other Things, but also of the Times of almost all Actions in the World, *viz.* Their Beginnings, Progress, Durations, and Intervals, are measured and numbered.

It is a periodical Revolution, or a great Circle of Months and Days, in which the four Seasons, *Spring, Summer, Autumn* and *Winter*, are, after one Revolution of the Sun, ordained to return in their Courses.

It is called *Annus*, from *Annulus*, a Ring; because a Motion in a Ring finished, begins again without End: Or, it may be, from *Anguis*, a Snake; because the *Egyptians*, before they had the Use of Letters, represented it by a Serpent, or Snake, biting her own Tail.

The *Year* is of two Sorts, Astronomical and Political.

The astronomical Year is two fold, *viz.* *Solar* and *Lunar*.

The *Solar Year* is either *Natural* or *Sydereal*.

The *natural Year* is that Space of Time, which the Sun takes up in departing from any one Point of the Ecliptic, to his Return to the same Point again, whether the Point be *Tropical*, *Equinoctial*, or *Solstitial*. This Motion is two-fold, viz. *mean* and *true*.

Note, It is called *natural*, because it seems to be designated by Nature for the Mensuration of Time.

The *mean Motion* of the Sun is ascribed to the *mean Equinox*, or *Solstice*, and contains 365 Days, 5 Hours, 48 Minutes, 55 Seconds; and this is the standing Rule and Level for the Length of the Year.

The *true Motion* (called also *apparent* and *unequal*) is ascribed to the *true Equinox* or *Solstice*, *i. e.* It is the Space of Time, in which the Sun, by his Motion, according to the Succession of the Signs, returns to the *true Equinox* or *Solstice*, and this increaseth or decreaseth according to the swifter or slower Progress of the *Equinoctial* or *Solstitial Points*; and contains in its greatest Quantity 365 Days, 5 Hours, 56 Minutes, 53 Seconds; but in the least Quantity 365 Days, 5 Hours, 24 Minutes, 38 Seconds.

The *Sydereal Year* is that Space of Time in which the Sun returns to the same Star, whether fixed or erratical, *i. e.* planetary, from whence it departed; and this is either fixed or moveable.

The fixed *Sydereal Year* is referred to the fixed Stars, whose Quantity is invariable; being according to *Copernicus* 365 Days, 6 Hours, 9 Minutes, 40 Seconds.

The moveable *Sydereal Year* is referred to any one of the Planets: The mean Quantity of Time being in Proportion to such Planet's Distance from the Sun, but inversely. Thus the mean Quantity of a *Sydereal Year* with *Saturn*, which is the most distant, is 378 Days, 2 Hours, 12 Minutes, 13 Seconds; with *Jupiter* (which is next nearer) it is 398 Days, 21 Hours, 12 Minutes, 9 Seconds; with *Mars* (which is next nearer to *Jupiter*) it is 779 Days, 22 Hours, 40 Minutes, &c.

The *Lunar Year*, is that wherein the Moon, after several Conjunctions with the Sun, as it were, meets and unites with him again, at or near the same Point in the Heavens, where they appeared together before; and this is two-fold, viz. *Common* and *Embolimial*, and each of these is either *mean* or *true*.

The mean *common Lunar Year*, contains 12 synodical Lunations, or 354 Days, 8 Hours, 48 Minutes, 38 Seconds, and this is the Rule of all the civil *Lunar Years*. The

The mean *embolismal Lunar Year*, contains 13 such Lunations, or 383 Days, 21 Hours, 32 Minutes, 41 Seconds.

The *Political or Civil Year*, is such as is every where used for Distinction of Time; wherein a Respect is had,

1. To the Sun alone.
2. To the Moon alone. Or,
3. To the Sun and Moon together.

1. The *Political or Civil Year* was framed by the Sun.

The *Egyptians*, by this Luminary, made their Year to consist of 365 Days exactly, and began their Year at the Noon of the first Day of their first Month *Tboth*. They had 12 Months, each containing 30 Days; and at the End, they always added 5 Days more to compleat the Year, by which Means the Sun was nearly brought to the same Place again as at first. But because they made no Reckoning of the odd 6 Hours, whereby the Year exceeded 365 Days, by that Means it anticipated one Day in every four Years, and caused the first Day of their Year, which was fixed to neither *Equinox* nor *Solstice*, to wander through all the Seasons of the Year.

The *Hebrews* observed the like Year before the *Alexandrian Era*, but with this Difference, that they intercalated, or added, one whole Month of 30 Days, at the End of every 120 Years: For they perceiving that the Year was too short by 6 Hours, were contented to stay so long, and then an intire Month of thirty Days was added, by which Means they brought the Sun nearer to his former Place than the *Egyptians*.

The *Hebrews* had also a two-fold Year, viz. *Ecclesiastical* and *Civil*. Their *Ecclesiastical Year* began from the new Moon next the *Vernal Equinox*, in the Month *Nisan*; and the *Civil* began from the new Moon next the *Autumnal Equinox*, in the Month *Tifri*.

The *Persians* used the same Year with the *Egyptians*, viz. 365 Days, and began it with the first Day of their first Month *Pharawardin*, exactly agreeable with *Chæac*, the fourth Month of the *Egyptians*, which also wandered through the several Seasons of the Year. They reckoned from the *Æra* of *Jesdegird*, which was *Anno Christi* 632, unto the *Galalean Year*, which was *Anno Christi* 1079, equal to 447 *Egyptian Years*; after which Time the *Persians* observed that their Year was too small, and that the Days of the Month anticipated by little and little; and therefore, by the Authority of the Emperor *Alb. Arsalem*, they instituted an Emendation thereof, beginning at the *Vernal Equinox*, and to the fourth Year, for the

most Part, and sometimes also to the fifth, they intercalated a Day, as we do in our *Bissexile* or *Leap Year*, but in such Manner, that in 648 Years they included 33811 Weeks, or 236677 Days; so that their Year, upon an Average, consisted of 365 Days, 5 Hours, 48 Minutes, 53 Seconds, and this Emendation is said to continue in use in that Empire to this Day.

Note, If 236677 Days be divided by 648, the Quotient will give the Length of the Year above-mentioned.

The Romans used a greater Year than either the *Egyptians* or *Persians*. For, according to *Julius Cæsar's* Constitution, their Year consisted of 365 Days, 6 Hours; which 6 Hours in every fourth Year make an intercalary Day, containing 366 Days, and therefore the common Year consisted of but 365 Days.

By the Appointment of *Romulus*, their first Founder, they began their Year about the *Vernal Equinox*; but afterwards, by the Decree of *Numa Pompilius*, and the Approbation of *Julius Cæsar*, they began it from the shortest Day thereof, viz. the *Winter Solstice*.

The *Venetians* began their Year from the 1st Day of *March*, perhaps because at that Time the Foundation of their City might be laid.

There are others, who are said to begin their Year from the Birth of *Christ*, viz. *December 25*. But the *Britons*, and most others, begin it the 1st Day of *January*; and so do all Astronomers.

Note, In England we had formerly a two-fold Year, viz. a Civil Year, which began January 1, and an Ecclesiastical Year, which began March 25: but since the Reformation of the Calendar in 1752, they are both the same, and begin January 1.

The *Muscovites* and *Russians* used the same Quantity of Time for their Year, and also retained the Names and Quantities of the Roman Months, but began their Year on the 1st Day of *September*.

The *Syrians*, or *Syro-Græcians*, numbered their Months and Days according to the *Julian* Manner, but gave them other Names; and began their Year after the *Autumnal Equinox*, viz. on the 1st Day of *October* of the *Julian* Year, and called it *Tisrin* prior, as hereafter.

The *Habassines*, or *Abyssines*, *Copti*, *Ethiopians*, and *Alexandrians* (all of them in *Africa*) numbered their Months and Days like the *Syrians*, but began their Year before the *Autumnal Equinox*, viz. the 4th of the *Calends* of *September*, answering

swering to the 29th of *August* of the *Julian Account*, or 9th Day of *September*, according to the new Account.

Note, *The Abeffines, were the People of Abeffinia; the Copti, the People of Coptos, a City in Egypt; Ethiopians, the People of Ethiopia; and Alexandrians, the People of Alexandria, another City in Egypt, built by Alexander.*

The *Julian Year*, which consisted of 365 Days, 6 Hours, as before mentioned, being by Observation found too long, it was by Pope Gregory the Thirteenth, in the Year of our Lord 1582, reduced to 365 Days, 5 Hours, 49 Minutes, 12 Seconds; and the Reason is obvious enough; for the odd 6 Hours in the *Julian Year* being not reckoned every Year, but once every fourth Year, they making this just 24 Hours, or a natural Day, were always put between the 23d and 24th Days of *February*, in the Bissextile or Leap Year, by which Means the 24th Day, which in the common Year, was the Festival of St. *Matthias*, became in the Leap Year the 25th, and was accordingly observed; and the Letter F, which stood against the 24th Day, was also put against the intercalated Day, and so both of them having the same Letter, were taken and accounted for one Day. Thus it appeared that the *Julian Year* was two-fold, viz. *Common*, consisting of 365 Days, and *Bissextile*, consisting of 366 Days. It was called *Bissextile* from *Bis*, twice, and *Sex*, six, because the 6th of the *Calends* of *March*, in the *Roman Calendar*, was twice repeated; *Intercalar*, because of the Day that was put in between; and *Leap Year*, because the fixed Holy Days did, as it were, and do still, leap one Day further into the Week, than they did the Year next before.

But besides this shortening of the Year, which alone was not sufficient; the aforesaid Pope, in the said Year 1582, caused ten Days to be intirely taken out of the Year, from *October* the 4th, so that the next Day after *October* the 4th, was taken and accounted for *October* the 15th, by which Means the *Equinoctium vernum*, or *Vernal Equinox*, which before was anticipated, or brought forwarder than it ought to have been, was brought back again to the 21st Day of *March*, agreeable to the *Nicene Council*, established *Anno Dom.* 324; and that the *Equinoctium Vernum* might invariably, for the Time to come, fall upon the same 21st Day of *March*, he appointed that the intercalated or Leap-Day, which should happen in the 1st, 2d and 3d Hundredth Year, according to the *Julian Account*, should be omitted, but in the 4th hundredth Year, the said Leap-Day should not be omitted, but intercalated in its proper Place.

This Account was, and is still received in all Countries subject to the See of *Rome*, or in Communion with that Church; but the *Julian* Account was retained in several other Countries, particularly in *Great Britain*, till the Year 1752, when 11 Days were intirely taken out of the Calendar from the 2d Day of *September* (the next succeeding Day becoming the 14th Day) and the Year was fixed to 365 Days, 5 Hours, 48 Minutes, 55 Seconds. This Account, though nearly agreeing with the *Gregorian*, yet being something better, was called the *New Account*.

2. The *Political* or *Civil Year*, was by some Nations framed by the Moon.

Thus the *Arabians*, *Indians* and *Turks*, reckon by the Moon, and make their Year to consist of 12 *Synodical* Lunations, and their Period to consist of 30 such Years; 19 of which Years, viz. the 1st, 3d, 4th, 6th, 7th, 9th, 11th, 12th, 14th, 15th, 17th, 18th, 20th, 22d, 23d, 25th, 26th, 28th and 29th, they reckon 354 Days to the Year, and the other 11 Years they reckon 355 Days to the Year: So that by this Account their whole Period consists of 10631 Days (for $354 \times 19 + 355 \times 11 = 10631$) and therefore one Lunation (there being 360, or 12 times 30 in the whole Period) contains 29 Days, 12 Hours, 44 Minutes exactly, as will appear by dividing 10631 by 360.

The ancient *Romans* also are said to have respected the Moon in their Description of the Year, according to the Ordination or Direction of *Numa Pompilius*.

3. The *Political* or *Civil Year*, was also by some Nations framed by the Sun and Moon together.

The ancient *Hebrews* had Respect to the Moon from their Departure out of *Egypt*, to the Time of the *Alexandrian* *Æra*; for in that Interval of Time they instituted the Ceremonies of the Temple, according to God's Command, by the Motion of the Moon. And although they retained some things of a pristine Form, so that their Year was, as it were, mixed, being partly *Solar*; running back, in some sort, to the *Equinoxes* and *Solstices*; and partly *Lunar*, according to which their *Feræ*, or Holy Days and Festivities were directed; yet by little and little they anticipated the *Equinoxes* till the Death of *Alexander* the Great, when they received the *Græcian* Year, as is plain by the Books of the *Maccabees*.

The *Attics* and *Græcians*, for the most Part, fitted their Descriptions of the Year to the Course of the Moon, and made a Year to consist of 12 such Months; yet observing that

that the Lunar Year did not answer to the Sun's Revolution, they therefore intercalated a whole Month, sometimes in the third Year, and sometimes also in the second Year, according to the *Calippic* Period; whereby they both accommodated their Year to the Sun's Motion (which indeed alone defineth a Year) and kept the *Equinoxes* and *Solstices* within their just Limits. However the *Attics* began their Year from the *Summer Solstice*, or from the new Moon next it, whether before or after it.

The *Jews*, about the Time of *Constantine* the Great (who began his Reign *Anno Dom.* 306) framed a peculiar Calendar, by the Help of *Rabbi Hillel*, wherein they brought the Moon's Motion (which defined the Feasts) to agree precisely enough with that of the Sun; so that the *Equinoxes* and *Solstices* could not easily be removed from their Places.

Those, who now follow the *Roman* Calendar, do not altogether neglect the *Lunar* Year, but think likewise that the same ought diligently to be considered, both because every one of the Months should have Names given them fitted to their Qualities and Operations; and also that the moveable Feasts, especially *Easter*, the Foundation of all the rest, might more exactly be determined.

II. Of the MONTHS.

THE Months, by which we measure the Year, are twofold, *viz.* *Astronomical* and *Political*.

The *Astronomical* Months, called also *Natural*, are considered according to the Motions of the *Sun* and *Moon*; and they are either *Solar* or *Lunar*.

The *Solar* Month is that Space of Time wherein the Sun runs through a twelfth Part of the *Zodiac*; which one Month with another, is 30 Days, 10 Hours and a Half, very near.

The *Lunar* Months refer to the Motion of the Moon, and are three-fold, *viz.* *Periodical*, *Synodical*, and the Month of *Illumination*.

The *Periodical* Lunar Month, is the Space of Time, in which the Moon, by her Motion, returns to the same Place of the *Zodiac* from whence she departed; which (according to her mean Motion) is performed in 27 Days, 7 Hours, 43 Minutes, 5 Seconds, nearly; but (according to her true Motion) about an Hour more or less.

The

The *Synodical Lunar Month*, is the Space of Time from one Conjunction of the Luminaries, till the next Conjunction following; which (according to her mean Motion) is 29 Days, 12 Hours, 44 Minutes, 3 Seconds; but (according to her true Motion) sometimes 14 Hours, more or less.

The Month of *Illumination*, or *Apparition*, is the Space of Time between the first Day wherein the Moon is seen after her Conjunction, and the last Day of her being visible, which is a little before her Conjunction with the Sun again; and this is sometimes 26 Days, sometimes 25 Days, and sometimes less. For although the new Moon is sometimes seen very early after her Conjunction with the Sun, she is not seen when she is so near to her next Conjunction, especially in the Summer Season, the Light of the Sun being then too powerful, unless it be a little after her rising, the Sun in the mean Time being below the Horizon; though it is very easy to know where to look for her, *viz.* a little to the Westward of the Sun.

The *Political* or *Civil Months*, are such as every Nation has made customary to themselves, whereby they distributed the Year as best pleased them. Hence arose the Proportion of the Months, and their Denominations.

The *Egyptian Months* and Days are these.

	Days		Days
1. <i>Thoth</i> - - - -	30	7. <i>Phameneth</i> - - -	30
2. <i>Phasphi</i> - - - -	30	8. <i>Pharmuthi</i> - - -	30
3. <i>Athyr</i> - - - -	30	9. <i>Pachsa</i> - - - -	30
4. <i>Chæac</i> - - - -	30	10. <i>Payni</i> - - - -	30
5. <i>Tybi</i> - - - -	30	11. <i>Epephi</i> - - - -	30
6. <i>Mechir</i> - - - -	30	12. <i>Mesori</i> - - - -	30

At the End of their last Month *Mesori* they added 5 Days more, thereby making their Year to consist of 365 Days.

The *Hebrew Months* and Days were these (the first beginning in *Autumn*) *viz.*

	Days		Days
1. <i>Ethenim</i> or <i>Tifri</i> -	30	7. <i>Nisan</i> or <i>Abib</i> - -	30
2. <i>Marchesuan</i> or <i>Bul</i> -	29	8. <i>Jiar</i> or <i>Ziph</i> - -	29
3. <i>Chisleu</i> - - - -	30	9. <i>Siwan</i> - - - -	30
4. <i>Thebeth</i> - - - -	29	10. <i>Thamuz</i> - - - -	29
5. <i>Shebeth</i> - - - -	30	11. <i>Ab</i> - - - -	30
6. <i>Adar</i> or <i>Ucadar</i> -	29	12. <i>Elul</i> - - - -	29

And

And this was their common, ordinary, or mean Year; which consisted of 354 Days; and when this Year was termed *full*, or *abundant*, then 1 Day was added to the second Month *Marchesuan*, by which that Year consisted of 355 Days; and when one Day happened to be taken off, which was from the third Month *Chisleu*, then it was called *common deficient*, and consisted of 353 Days.

The *Embolismical* Luration of the *Hebrews* exceeded the common Year by 30 Days, and was inserted next before the last Month, and was called *Adar*, like the 6th Month, and then the last was called *Veadar*, which otherwise was called *Elul*. And as by the Addition or Intercalation of the said 30 Days, there might sometimes be a Redundancy, and sometimes a Defect of 1 Day, so 1 Day was either taken off or added, as above-mentioned.

The *Persian* Months and Days were these, *viz.*

	Days		Days
1. <i>Pharawardin</i>	- - 30	7. <i>Mebar</i>	- - - 30
2. <i>Adarpabaseht</i>	- - 30	8. <i>Aban</i>	- - - 30
3. <i>Chardad</i>	- - - 30	9. <i>Adar</i>	- - - 30
4. <i>Thir</i>	- - - 30	10. <i>Di</i>	- - - 30
5. <i>Mardad</i>	- - - 30	11. <i>Behemen</i>	- - - 30
6. <i>Scheberiz</i>	- - - 30	12. <i>Asphander</i>	- - - 30

To which were added, in the common Year, 5 intercalar Days, and 6 in the intercalar or Leap Year, which they called *Musterka*.

The *Romans* (according to the Ordination or Direction of *Romulus*, who was the Founder of their City, as before-mentioned, and consequently their first King) had at first but 10 Months in the Year, wherein they included 304 Days.

The first of which was *Martius*, our *March*, which *Romulus* so named from *Mars* the God of War, because he would have the *Roman* Nation Martial or Warlike.

The second was *Aprilis* our *April*, from *Aperio*, to open; because then the Pores of the Earth were opened, and the Trees and Herbs began to spring out.

The third was *Maius*, our *May*, from *Major* greater; or from *Majus Deus*, *i. e.* *Jupiter*; or from *Madesacio*, to wet or moisten; because of the wet Weather then and there happening, which was thought to be occasioned by the rising of the *Pleiades* or *Hyades*, *i. e.* the seven Stars in *Taurus*, or the *Bull's Neck*.

The

The fourth was *Junius*, our *June*, from *Junior*, younger; or from *Juno*, the Wife of *Jupiter*, who, not unlikely, was younger than *Jupiter*; for though they were first of all, Brother and Sister, and born at the same Birth, it does not appear that *Juno* was the first born; consequently if *Jupiter* was first born, *Juno* must be *Junior* or younger.

The fifth was *Quintilis*, as being the fifth Month from *March* inclusive; now our *July*.

The sixth was *Sextilis*, as being the sixth Month from *March* inclusive, now our *August*.

The seventh was *September*, from *Septem*, seven (the same with our *September*) because it was the seventh Month from *March* inclusive.

The eighth was *October*, from *Octo*, eight (the same with our *October*) because it was the eighth Month from *March* inclusive.

The ninth was *November*, from *Novem*, nine (the same with our *November*) because it was the ninth Month from *March* inclusive.

The tenth was *December*, from *Decem*, ten (the same with our *December*) because it was the tenth Month from *March* inclusive.

Four of these Months, viz. *Martius*, *Maius*, *Quintilis* and *October*, i. e. *March*, *May*, *July* and *October*, were called *Pleni*, full, because each Month contained 31 Days, that is, they were the longest Months; and the other six, viz. *Aprilis*, *Junius*, *Sextilis*, *September*, *November* and *December*, i. e. *April*, *June*, *August*, &c. were called *cavi*, hollow, because each Month wanted a Day of being equal with the four longer Months.

This *Calendar* is said by some, to have continued no longer than *Romulus* reigned, viz. 45 *Romuleian* Years, and about 200 Days; making about 38 of our Years; but others say, it lasted only 24 *Romuleian* Years, making 20 of our Years.

But however this was, it is said that *Numa Pompilius*, the second King of the *Romans*, perceiving his Predecessor's Year to be too short, he added 51 Days, which together with 6 other Days that he took from the 6 *Carval Months*, of 30 Days each, he disposed into two new Months, calling them *Januarius*, *January*, and *Februarius*, *February*: To *January* he assigned 29 Days, and to *February* 28, and placed them before *Martius* or *March*.

Januarius

Januarius was so called, either from from *Janua*, a Gate, because an Entrance was thereby made into the Year, as through a Gate into the Hall; or from double-faced *Janus*, looking back upon the End of the past Year and the Beginning of the following, or next succeeding Year; of whom take the following Relation, *viz.*

Janus was the most ancient King of *Italy*, among the *Aborigines*, a Set of People, that *Saturn*, the Father of *Jupiter*, brought into that Country, where they settled in the Mountains. When *Jupiter* had made War against his Father, and banished him from *Crete*, *Janus* received him, and gave him Part of his Kingdom. Here *Saturn* taught *Janus* Husbandry, and the Method of coining Money of Brass, which on one Side had the Representation of a Ship, and on the other Side that of *Janus*. It was reported of him, that he was the wisest of all Kings, and knew Things not only past, but those which were to come, therefore the Ancients pictured him with two Faces. After his Decease, his People deified him, *i. e.* made a god of him, and *Numa* built a Temple in Honour of him, which, in the Time of Peace, was always kept shut, but in the Time of War was always kept open.

Janus was thought by some to be the same with *Noah*, whence he might be said to have two Faces, one looking backward upon the old World, which was before the Flood; the other forward upon the new World, which was after the Flood; and for this Reason, perhaps, the Ship on his Coin was in Memory of the Ark. He is said to have come into *Italy* in the golden Age of the World, not upon the Account of Gold itself (for perhaps there was none at that Time) but because Men were just, free from Avarice and Covetousness; and as he had learnt Husbandry from *Saturn*; so he taught the same to his People, and withal to live temperately, and offer Sacrifices.

Februarius, was so called from *Februo*, to sacrifice; because in this Month the *Romans* sacrificed to *Pluto* (who was also called *Februus*) and the other infernal gods, for the Souls of their Ancestors.

And thus were all the Months of the *Numan* Year ordained, and so the Year itself, to consist of an odd or unequal Number of Days; in Honour of an unequal Number accounted of as sacred by the *Pythagoreans*, excepting only *February*, which had an even or equal Number of Days allowed it, lest if all of them had run either by an equal or unequal Number of Days, they should have made a like Consum-

Consummation or Ending : And hence arose this Disposition of the Months, viz.

	Days		Days
1. <i>Januarius</i>	- - - 29	7. <i>Quintilis</i>	- - - 31
2. <i>Februarius</i>	- - - 28	8. <i>Sextilis</i>	- - - 29
3. <i>Martius</i>	- - - 31	9. <i>September</i>	- - - 29
4. <i>Aprilis</i>	- - - 29	10. <i>October</i>	- - - 31
5. <i>Maius</i>	- - - 31	11. <i>November</i>	- - - 29
6. <i>Junius</i>	- - - 29	12. <i>December</i>	- - - 29

Wherein, although *Januarius* and *Februarius*, were put before *Martius*, and so *Martius* was made the third Month instead of the first ; yet *Quintilis* (now no longer the fifth, but the seventh Month) retained still the same Name, as did also the other following Months in their Order.

But when *Numa* observed, that by this Quantity of the Year (which was only *Lunar*, and conformable to the *Græcian* Year) the Sun returned not to the same Point in the Heavens ; he reduced and accommodated this *Lunar* Year to the Sun's Motion, by the Intercalation of a new Month, consisting of 22 Days, or 23 Days, which afterwards the Romans called *Februarius intercalaris*, or *Mercedonius mensis*, which every other Year was intercalated, lest *March* should be removed from the Beginning of the Spring, or that more Years should be accounted from the Building of *Rome*, than justly the true Quantity of the Year would allow of.

Note, It was called *Mercedonius Mensis*, because (besides its being appointed for the rectifying of the Year) it was used as a Time for Payments of Rents, Wages, &c. Hence arose the *Mercedonice Dies*, or Pay-Days, instead of that Month, appointed by *Julius Cæsar*, which were 6 in July, 4 in September, and 3 in November ; which Days were all marked in the old Roman Calendar with *MERK* on the Side.

But although this kind of Intercalation, so restored the *Numan* Year (which without it was merely *Lunar*) to the Sun's Course, that the *Equinoxes* and *Solstices* were in a manner fixed to the same Months : Yet afterward, when they observed it exceeded the true and natural Quantity of the Year, and that the Arch Priest (whose Business it was to correct the Intercalation) had oftentimes omitted it, and either out of Malice or Favour (whereby any Man might be got rid of, or longer continued in his Mastership, whatever it was ; or the Renter of the Tribute or Customs, or other public Things, either gain or lose by the Increase or Decrease of the Year) had several Ways depraved it, it fell out that *Anno Urbis conditæ*

708, i. e. in the 708th Year of the Building of *Rome*, after the *Numan* Year had been in Use 670 Years, the Correction made by *Julius Cæsar* was received.

For *Julius Cæsar*, who was the first Monarch or Emperor of the *Romans*, having learned Mathematics at *Alexandria* observed that there were 10 Days and almost 6 Hours wanting in the *Numan* Year, to the full compleating of the Solar Year; and by the Advice of *Sofigenes* the Mathematician, whom after his Overthrow of *Pompey*, he brought with him out of *Egypt* to *Rome*, he added those 10 Days, whereof to *Januarius*, *Sextilis* and *December*, 2 Days each; but to *Aprilis*, *Junius*, *September* and *November*, but 1 Day each.

And now because *Quintilis* was a wrong Name for that Month, that being now the 7th Month from the Beginning of the Year inclusive, which at its first Institution was but the 5th, and *Julius Cæsar* having been born in that Month, it was thought proper, in Honour of him, to reject that Name, and give it the Name of *Julius*, the same with our *July*.

For a similar Reason was *Sextilis* rejected in the following Reign, or soon after: For *Augustus Cæsar*, who was Nephew to *Julius Cæsar*, succeeding his Uncle in the Empire, either called this Month by his own Name, or the Senate did it in Honour of him, he dying in this Month. Thus it was that the civil *Roman* Months were numbered and nominated with the same Number of Days, just as we have them at this present Time, viz.

	Days		Days
1. <i>Januarius</i> - - -	31	7. <i>Julius</i> - - -	31
2. <i>Februarius</i> - - -	28	8. <i>Augustus</i> - - -	31
3. <i>Martius</i> - - -	31	9. <i>September</i> - - -	30
4. <i>Aprilis</i> - - -	30	10. <i>October</i> - - -	31
5. <i>Maius</i> - - -	31	11. <i>November</i> - - -	30
6. <i>Junius</i> - - -	30	12. <i>December</i> - - -	31

And although the Year hath since been corrected by *Gregory* the 13th Bishop of *Rome*, yet do the Order of the Months, and the Number of Days in each Month, continue the same in the corrected, that they did in the old *Julian* Year: they differing only in this, that in the Space of 400 Years, the *Julian* Account exceeds the *Gregorian*, by 3 Intercalations, or Days, which in the last Emendation of our Calendar, is directed to be cut off in every hundredth Year, not divisible by 4 without a Remainder.

The

The *Syrian*, or *Syro-Chaldaean* Year, as used by that People anciently, and some say at this present Time, agrees with the *Julian* Year in Number of Months, Days in each Month, and manner of Intercalation; but has a different Beginning. For the first Month of the *Syrians* Year answers exactly to the *Romans* *October*, and consequently the 1st Day of that Month was the 1st Day of their Year, *viz.*

	Days		Days
1. <i>Tisrin</i> prior (<i>Oct.</i>)	- 31	7. <i>Nisan</i> (<i>Apr.</i>)	- - 30
2. <i>Tisrin</i> posterior (<i>Nov.</i>)	30	8. <i>Jiar</i> (<i>Maius</i>)	- - 31
3. <i>Canun</i> prior (<i>Dec.</i>)	- 31	9. <i>Huzaran</i> (<i>Junius</i>)	- 30
4. <i>Canun</i> posterior (<i>Jan.</i>)	31	10. <i>Tamuz</i> (<i>Julius</i>)	- 31
5. <i>Sabat</i> , common (<i>Feb.</i>)	28	11. <i>Ab</i> (<i>Aug.</i>)	- - 31
	bissextile 29	12. <i>Elul</i> (<i>Sept.</i>)	- - 30
6. <i>Adar</i> (<i>Mar.</i>)	- - 31		

The *Syro-Græcian* Year was the same with the *Syrian* as above, both in Number of Months and Days in each Month, and also the Beginning of their Year, *viz.*

	Days		Days
1. <i>Hyperberetæus</i> (<i>Oct.</i>)	- 31	7. <i>Xanthicus</i> (<i>Apr.</i>)	- 30
2. <i>Diuo</i> (<i>Nov.</i>)	- - 30	8. <i>Artemisius</i> (<i>Mai.</i>)	- 31
3. <i>Appellæus</i> (<i>Dec.</i>)	- - 31	9. <i>Dæsius</i> (<i>Jun.</i>)	- - 30
4. <i>Audinaus</i> (<i>Jan.</i>)	- 31	10. <i>Panemus</i> (<i>July</i>)	- 31
5. <i>Peritius</i> common (<i>Feb.</i>)	28	11. <i>Lous</i> (<i>Aug.</i>)	- - 31
	bissextile 29	12. <i>Gorpiæus</i> (<i>Sep.</i>)	- 30
6. <i>Dysurus</i> (<i>Mar.</i>)	- - 31		

The *Abyssines* and *Copti*, a People of the inner Part of *Africa*, began their Year on the 29th Day of the *Julian August*, whose Months and Days were as follows, *viz.*

	Days		Days
1. <i>Tuth</i>	- - - 30	7. <i>Pharmath</i>	- - 30
2. <i>Papa</i>	- - - 30	8. <i>Parmuda</i>	- - 30
3. <i>Hathur</i>	- - - 30	9. <i>Paschnes</i>	- - 30
4. <i>Chiac</i>	- - - 30	10. <i>Peuna</i>	- - 30
5. <i>Tuba</i>	- - - 30	11. <i>Epip</i>	- - 30
6. <i>Amschir</i>	- - - 30	12. <i>Musro</i>	- - 30

Unto which they added 5 Days in the common and 6 in the Bissextile Year.

From

From the same 29th of *August* did the *Ethiopians* reckon their Year, the Names of whose Months were as follows, viz.

1. <i>Mascaram</i>	5. <i>Tbir</i>	9. <i>Ginboth</i>
2. <i>Tikmith</i>	6. <i>Jacatib</i>	10. <i>Sene</i>
3. <i>Hadar</i>	7. <i>Magabith</i>	11. <i>Hamle</i>
4. <i>Tachbas</i>	8. <i>Miazia</i>	12. <i>Nabafe</i>

And, as far as we know, they had the same Number of Days, viz. 30 in each Month; adding likewise 5 Days at the End of the common Year, and 6 in the Bissextile.

The *Arabians* and *Turks* began their Year from the *Æra* of *Mahomet*, whose Months and Days are as follow, viz.

	Days		Days
1. <i>Muhartam</i>	- - 30	7. <i>Regeb</i>	- - - 30
2. <i>Spehar</i>	- - - 29	8. <i>Sahaben</i>	- - - 29
3. <i>Rabie prior</i>	- - 30	9. <i>Ramadhan</i>	- - - 30
4. <i>Rabie posterior</i>	- 29	10. <i>Scherwal</i>	- - - 29
5. <i>Giumadi prior</i>	- 30	11. <i>Dhilkahda</i>	- - - 30
6. <i>Giumadi posterior</i>	- 29	12. <i>Dhilkahda</i> or <i>Dhilkitsche</i>	29 in the common Year, and 30 in the Intercalar.

Thus their Year consists of but 354, and sometimes 355 Days, and therefore the first Day of their Year must wander through all the Seasons, but in a retrograde Manner, because it is shorter than the true Solar Year.

Note, In England, and no where else that I know of, we commonly reckon 4 Weeks to a Month; by which Month Sailors are commonly paid their Wages, 13 such Months, and 1 Day make a common Year.

III. Of the WEEKS.

THE *Hebdomada*, or *Week*, in Chronology, is a Division of Time, consisting of seven Days.

The Origin or Beginning of this Division of *Weeks*, or of computing Time by Sevenths, has been controverted: Some having supposed it to take its Rise from the four Quarters of the Moon, that is, New, first Quarter, Full, and last Quarter, (she having at those Times different Appearances) which being about 7 Days distant, gave Occasion to such a Division.

But however this was, the manner of dividing Time into *Weeks*, according to the present Manner, as observed by all Europe,

Europe, at least, and not unlikely in several Parts of *Asia*, *Africa* and *America*, is very ancient. The *Egyptians*, *Syrians*, and most of the Oriental Nations, appear to have used it from all Antiquity; though it did not get Footing in the Western Part of the World till Christianity brought it thither.

The ancient *Romans* are said to have reckoned their Days, not by *Sevenths*, but by *Ninths*, and the ancient *Greeks* by *Decads* or *Tenths*.

The *Hebrews* of old, divided their Time by *Weeks* or *Sevenths*, but it was upon a different Principle from the other Eastern Nations; God himself having appointed them to work six Days, and to rest the *Seventh*, as fully appears by the fourth Commandment. *Six Days shalt thou Labour, and do all thy Work, but the seventh Day is the Sabbath of the Lord thy God*, *Exod. xx. 9, 10.* And this was after God Almighty's own Pattern or Example, who at the Creation of the World, is said to have *worked six Days, but on the seventh Day rested from all his Work, and blessed it, and sanctified it*, *Gen. ii. 3.*

Among the Heathens of the East, it is, with very good Reason, supposed to be a Remain of the Tradition of the Creation, which they had still retained, with divers other Traditions.

The Days of the Week were denominated by the *Jews* from the Order of their Succession from the Sabbath. Thus the Day next after the Sabbath, they called the first of the Sabbath; the next the second of the Sabbath; and so of the rest, except the sixth, which they called *Parasceve*, or Preparation of the Sabbath, because they prepared and set all things in order on the *Friday*, that so nothing might be done on the Sabbath, but the Works of absolute Necessity; and the Sabbath was the last Day of the Week. The like Method is said to be still kept up by the *Persians*, *Ethiopians*, and the Christian *Arabs*.

The ancient Heathens denominated the Days of the *Week* from the seven Planets, which Names are still generally retained, not only in *England*, but in *France*, *Spain*, *Portugal*, *Italy*, *Germany*, *Holland*, *Denmark* and *Sweden*. Thus the first Day of the Week is commonly called *Sunday* (*dies Solis*, Sun's Day) and is derived from the *Sun*, that glorious Luminary of Heaven, which was worshiped by our idolatrous Ancestors on that Day.

The second Day is called *Monday* (*dies Lunæ*, Moon's Day) and is derived from the *Moon*; that Planet being anciently

ciently worshiped by some of the Heathens on that Day. Hence the French *Lundi*, from *Luna* the Moon.

The third Day is called *Tuesday* (*Tuisco's* Day) and is derived from *Tuisco*, a *Saxon* Deity, which was worshiped on that Day, and is supposed to be the same with *Mars* the God of War. Hence *dies Martis*, and the French *Mardi*, or *Mars's* Day.

The fourth Day is called *Wednesday* (*Woden's* Day) and takes its Name from *Woden*, an Idol worshiped by the ancient *Saxons* on this Day. He is supposed to be the same with *Mercury*. Hence *dies Mercurij*, and the French *Mecredi*, *Mercury's* Day.

The fifth Day is called *Thursday* (*Thor's* Day) and is derived from an ancient *Saxon* Idol called *Thor*, which used to be worshiped on that Day. It is supposed to be the same with *Jupiter*, hence called *dies Jovis*, or *Jove's* Day: hence also the French *Jendi*, *Jupiter's* Day.

The sixth Day is called *Friday* (*Friga's* Day) derived from *Friga*, an *Heathen* Goddess, who was worshiped by our Forefathers on that Day; and is supposed to be the same with *Venus*; hence the *Latins* call it *dies Veneris*, *Venus's* Day; and the French *Vendredi*, signifying the same.

The seventh, and last Day of the Week is called *Saturday* (*Saturn's* Day) from *Saturn*, an old *Heathen* Deity, or Idol, which was worshiped on that Day: The *Latins* called it *dies Saturni*, and the French *Samedi*, both signifying the same Day.

Under the *Mosaic* Dispensation, the seventh or last Day of the Week (which is our *Saturday*) was kept holy by an express Command from God, in Memory of the *Creation* of the World, as was before observed; but with the *Christians*, the first Day of the Week is kept holy, in Memory of our Saviour's *Resurrection* from the Dead: And this was begun to be transferred from one Day to the other, by the Apostles, but was not absolutely fixed till some Time after all the Apostles had suffered Martyrdom; the *Jewish* Converts, especially, in the mean While, retaining an Affection for their old Sabbath, insomuch that for a long Time both Days were religiously observed; till such Time as Kings themselves embraced the Christian Religion, and as such became the nursing Fathers to the Church of *Christ*, and Christianity became national, and then it was fixed to the first Day of the Week, by *Constantinus magnus*, *Constantine* the Great, who was the first Emperor that embraced the Christian Faith.

IV. Of the D A Y S.

THE ancient Romans divided each of their Months into *Calends*, *Nones* and *Ides*.

The *Calends* were the first Day of every Month, derived from *Calo*, an old Word in the *Roman* Language (the same with *Voco*, signifying to call) the Gerunds of that Word being *calendi* of calling, *calendo* in calling, and *calandum* to call; hence the Word *Calends*, because the People were then called or obliged to pay their Use-Mony; whence also those Days were called *Tristes Calendæ*, i. e. sad Calends or Days, because some People being either unable or unwilling to pay their borrowed Mony, with the Interest, were punished according to the Laws then in Force. They were also called *celeræ Calendæ*, swift Calends, because of their quick Return; unthinking People not regarding the Day till it came upon them, as it were, at once; and then they would complain, that those Days came about very quick; just, as many People do at this Time, who being indifferent about paying their Rents, say *The Quarters come about very fast*.

The *Nones* derived from the *Latin* Word *Nonus*, the ninth, because they were always the ninth Day before the *Ides*; and in *March*, *May*, *July* and *October*, happened upon the seventh Day, but in the rest of the Months on the fifth Day.

The *Ides* derived from the *Latin* Word *Idus*, and that from *Iduo*, which in the *Hetruscan* Tongue, or Language of *Tuscany*, is *Divido*, from an obsolete Word *Dividuo*, which signifies, I divide; hence by an Ellipsis *Iduo*, as before, signifying the same, because the *Ides* divided every Month almost in the Midst: The Months *March*, *May*, *July* and *October*, having the *Ides* on the 15th Day of each Month, and all the rest on the 13th Day; the other intervening Days were reckoned as so many Days, viz. 5th, 4th, 3d, &c. before the *Calends*, *Nones* or *Ides*.

Days are of two Kinds, *natural* and *artificial*.

The * *natural* Day contains the Time that is taken up in one intire Revolution of the Earth upon its own Axis, at the same Time that it moves round the Sun; and this makes the two Quantities of Light and Darkness, which immediately succeed each other, commonly called Day and Night, and is divided into twice 12, or 24 equal Parts, called Hours.

* Note, Some Writers call this a Civil Day; and that only a Natural Day, which is between Sun-rise and Sun-set,

The *artificial Day* is all that Space of Time between Sun-rising and Sun-setting, which is always increasing or diminishing, according to the Latitude, and according to the Sun's Place in the Ecliptic; or, which is the same thing, according to his Declination, whether North or South. The *artificial Night* is all that Space of Time between Sun-setting and Sun-rising; and this, like the *artificial Day*, is always increasing or decreasing, but with this Difference, that when the Day increases, the Night diminishes; and when the Night increases the Day diminishes.

The *Chaldeans* and ancient *Hebrews* began their *natural Day* at the Rising of the Sun, and ended it again at his next Rising.

The *Romans* began it at Midnight, and ended it the Midnight next following. — The same is done by several Countries at this present Time, *viz.* Great Britain, Ireland, France, Spain, Portugal, Holland, Denmark and Sweden.

The *Egyptians* began their Day at Noon, and ended it the Noon next following: And, according to this Account, do all Astronomers now frame their Computations; every one according to the Meridian of the Place where he lives, or where he makes his Calculations for.

The *Babylonians* began their *artificial Day* at Sun-rising, and ended it at Sun-setting; and their *artificial Night* at Sun-setting, and ended it at Sun-rising.

The old *Italians* began their *natural Day* at Sun-setting, and ended it at Sun-setting the next Day.

The *Jews*, at and before our Saviour's Time, began their *artificial Day* at the Time of Sun-rising, and ended it at Sun-setting; and their Night began at Sun-setting, and ended at Sun-rising, like the ancient *Babylonians*. But in the Division of their Hours, they differed from all others; for they divided the Time between Sun-rising and Sun-setting, into 12 equal Parts, and the Night, from Sun-setting to Sun-rising, they divided into 12 other equal Parts; so that the Hours of their Day and their Night were never equal one to the other, nor to those of other Countries; but when the Sun was in the *Equinoctial*, which now happens about the 20th or 21st of March, and the 22d or 23d of September: For all the Inhabitants on the North Side of the Equator, when the Sun is in North Latitude, have their Days longer than their Nights, from the 20th or 21st of March, to the 22d or 23d of September; and all on the South Side of the Equator, when the Sun is in South Latitude, have their Days longer than their Nights,

from the 22d or 23d of *September* to the 20th or 21st of *March*, notwithstanding the whole natural Day is divided into 24 equal Parts or Hours: But the *Jewish* Account of Hours differed from all those; for on the North Side of the Equator, from *March* to *September* as aforesaid, the Hours of their Day were longer than the Hours of their Night: And all the Time between *September* and *March* as aforesaid, the Hours of their Night were longer than those of their Day; the contrary in South Latitude: So that when our *artificial Day* was 15 Hours between Sun-rising and Sun-setting, then did the *Jewish* Day-hour contain one Hour and a Quarter of our Hour in Length, and their Night-hour but three Quarters of our Hour: Also when our *artificial Day* was but 9 Hours long, then was their Day-hour but 45 of our Minutes, or three Quarters of an Hour long, and their Night-hour equal in Length to 1 Hour and 15 Minutes of our Time. And so they varied all the Year, and were never equal with our Hours, or the rest of the World, except when the Sun, as aforesaid, was in the *Equinoctial*. Now, admitting our *Meridian* and theirs to have been the same, our 12 at Noon was then the same with their 6th Hour of the Day, and our 12 at Night the same with their 6th Hour of the Night; that is, our Noon would be the same with their Noon, and our Midnight the same with their Midnight: But in Fact it was not so; for the Difference between our *Meridian* and theirs is almost 45 Degrees, making 3 Hours of Time nearly, as appears very evidently by the Terrestrial Globe; and their *Meridian* being also to the Eastward of ours, made their 6th Hour, or Noon-Day, 3 Hours, or very near so, sooner than ours. Hence their Noon-Day was at our 9 in the Morning, or very near so; and hence also appears very plainly, what those 3d, 6th and 9th Hours were, at our Saviour's Passion, as mentioned *Mark* xv. 25th, 33d and 34th Verses; where at Verse the 25th, it is said, *That they crucified him at the third Hour*, which Hour, had our *Meridians* been the same, would have been about our 9 in the Morning, but as their Noon was very near 3 Hours before ours, so the Time of our Saviour's Crucifixion was, according to our Computation of Time, about 6 in the Morning; for the Crucifixion happening about the Time of the Vernal Equinox, reduced their Hours to an Equality with ours, or very nearly so — At Verse the 33d, it is said, *There was Darknes over the whole Land, from the 6th to the 9th Hour i. e. from their Mid-day to the End of 3 Hours after*; and at Verse 34th,

it is said, *That at the 9th Hour our Saviour cried with a loud Voice, uttering that most lamentable Expression, Eloi, Eloi, lama sabachthani; or, My God, my God, why hast thou forsaken me:* By which it appears, that he hung upon the Cross full six Hours before he expired, *viz.* from the 3d to the 9th Hour, *i. e.* from our 6 in the Morning to 12 at Noon, Regard being had to the Difference of Meridians, as was observed before. By this Means also will appear, what that 3d Hour of the Night was, when the chief Captain ordered St. Paul to be conveyed from *Jerusalem to Cesarea, Acts xxiii. 23.* For as the third Hour before mentioned at the Crucifixion of our Saviour was three Hours before their Noon, so by Parity of Reason, their 3d Hour of the Night was three Hours before their Midnight, *i. e.* Nine o'Clock with them, if Clocks had been then in use, as we have them now; equal to, or very near our Six in the Afternoon.

V. Of the H O U R S.

AT this present Time in *Europe*, and some other Parts of the World, the natural Day, whether it be taken from Noon to Noon, or from Midnight to Midnight, is divided into 24 equal Parts, called Hours, and these are subdivided into twice 12 Hours; one 12th Hour serves for Noon or Mid-day, the other 12th Hour for Midnight: And as all our Clocks and Watches have their Dial-Plates divided only into 12 equal Parts or Hours, so their *Indices* or *Hands* go twice round: Hence all the Hours from Midnight to Noon are called *Ante Meridiem*, before Noon, or Morning Hours; and all the Hours from Noon to Midnight are called *Post Meridiem*, or Afternoon; otherwise more commonly distinguished after this manner, *viz.* From Noon to Sunset, the Hours are called Afternoon; from Sunset during the Time of Twilight, 'tis called Evening; after Twilight it grows dark, and then it is called Night, even though the Moon should shine and be at the full.

The modern *Italians* differ from the rest of the *Europeans*; for they not only divide the natural Day into 24 equal Parts or Hours, but the Dial-Plates of their Clocks and Watches are divided so too; and whereas our *Indices* or *Hands* make two Rotations in that Space of Time, theirs make but one, and go regularly on from 1 to 24, so that 12 o'Clock is their Mid-day, and 24 o'Clock their Midnight.

But however it is now, that $\frac{1}{24}$ Part of a Day natural, makes what we now call an Hour, it was not so from the Beginning. For, as for the Method of computing the Time of the Day by the *Antediluvians*, or People before the Flood; we have no Footsteps of it remaining; and for a long Time after the Flood, it does not appear by any History, sacred or prophane, that the People divided their Time as we do now, or knew any thing of an Hour, as we now understand it.

In the Time of *Abaz*, King of *Judah*, 2 *Kings* xx. 11, there was a Sun-dial, whether placed horizontally in his Garden, or erect on the Side of his House, or whether it was on a convex or concave Superficies, or *in Plano*, is not easy to determine; and the Time that then passed was said to be by Degrees, of which we are equally as ignorant: however, it is certain there were some distinguishing Lines upon it, whereby the Increase of the Day before Noon, and Decrease of it after Noon, might be known.

In the *Old Testament*, the Word Hour occurs only in the Prophet *Daniel*, and no where else; and there five times, viz. *Daniel* iii. 6, 15; iv. 19, 33, and v. 5, in four of them the Expression is *same Hour*, signifying almost the same Point of Time; but in chap. iv. v. 19, it is said *one Hour*, i. e. at the Relation of King *Nebuchadnezzar's* Dream, told by *Nebuchadnezzar* himself, *Daniel was astonied*, i. e. astonished (some Bibles having it one way, some another) *one Hour*: The Meaning of which is, that he was in such Confusion within himself, that he was not able to express himself during that Time.

At the same Time the Prophet *Daniel* was in *Babylon*, captivated with the rest of his Brethren the *Jews*; and as the *Babylonians* began their artificial Day at Sun-rising, and ended it at Sun-setting, as has been said before: So by the Expression *one Hour*, we must imagin that the *Babylonians* divided their Day into other Portions of Time, than what was on the Dial of *Abaz*, the better to distinguish how the Time passed away; and not unlikely, but they might divide their artificial Day into 12 equal Parts, whatever their Names were, though those Parts, like the Day, might be daily increasing, or decreasing; and that the *Jews* received this Division of the Day from them; and then we may guess what the Quantity of that Time was, which is there called *one Hour*, and judge it to be not greatly differing from our own Hour, whether more or less, as was mentioned of the *Jewish* Division of the Day, a little before.

VI. OF MINUTES.

THE Division of the Day into equal Parts, of what sort soever they were when first invented, and since improved into what we call Hours, was certainly of much earlier Date than *Minutes*, inasmuch as the Minute (the mechanical Minute, if I may so call it, I mean) or 60th Part of an Hour, mechanically exhibited, was not known to the Ancients; nor immediately after the Hour was settled, as we now use it, though the Astronomical Minute was known long before, and therefore, very likely, it was some *Horologiorum fabricator*, i. e. *Clockmaker*, who first introduced the Minute, by dividing the Hour into 60 equal Parts, as we see them on the Dial-plates of Clocks and Watches, that such Piece of Clock-work might appear to be the more ingenious; and likewise shew to the Admirers, how easily, pleasantly, and almost insensibly the Hour passed away, by those small Portions of Time.

Note, *A Minute is sometimes called a Moment, derived from the French Word Moment, and that from the Latin Momentum, which signified the smallest Portion of Time that could be assigned, before Seconds were used.*

VII. OF SECONDS.

QUICK as the Minutes flee away, we find that they were capable of the same mechanical Divisions, that is, each one into 60 equal Parts, called *Seconds*, and be exhibited to Sight, as were the Minutes before mentioned. They are derived from Astronomical *Seconds*, as being the 60th Parts of a Prime or Minute in Astronomy, and thence became applicable to the 60th Part of a Minute of Time. This, no Doubt, was another Contrivance of some ingenious Clock-maker, to set three *Indices*, or *Hands*, as we commonly call them, a going at once, to point out the Time of the Day or Night, in the most minute and circumstantial Manner.

There are Clocks with short Pendulums which beat Half Seconds, and Watches that beat Quarter Seconds, but what Service such Beats would be of, if mechanically exhibited, seems, at present, not very easy to determin.

T A B L E S

O F

SCRIPTURE-MEASURES, WEIGHTS and COINS:

WITH AN
A P P E N D I X,

Containing the Method of calculating its
MEASURES of SURFACE.

A Measure is a known Quantity applied to another of the same Kind that is less known, to make its Dimensions better known, by Help of Numbers, expressing the Proportion that the known Quantity bears to the unknown.

The Dimensions to be measured are three.

First, Meer Length, which hath but one Dimension.

Secondly, Surface, which consists of Length multiplied into Breadth; so it hath two Dimensions, as it were interwoven, and this is always measured by some square Surface, already known, as by a square Foot, or a square Cubit, or any other Square already known, by the Help of its Side. *Moses* generally used the square Cubit.

Thirdly, Solidity or Capacity, which hath three Dimensions multiplied into each other, *viz.* Length, Breadth and Height or Depth. This is measured by a known Cube.

From Solidity ariseth Weight in all sublunary Bodies; and by Weight we measure the Value of Coins: Therefore I shall join Weights and Coins together in the fourth Table.

TABLE I.

Of Measures of Length.

The Cubit and its Parts are expressed both by Inch-Measure, and by Foot-Measure, which is deduced from Inches by this Proportion,

$$I. \quad F. \quad I. \quad F. \\ 12 : 1 :: 21.888 : 1.824$$

		In. Meas.	F. Meas.
A Cubit is	- - - - -	= 21.888	= 1.824
A Span, the longer	= $\frac{1}{2}$ of a Cubit	= 10.944	= .912
A Span, the less	= $\frac{1}{3}$ of a Cubit	= 7.296	= .608
A Hand's Breadth	= $\frac{1}{6}$ of a Cubit	= 3.684	= .304
A Finger's Breadth	= $\frac{1}{12}$ of a Cubit	= .912	= .076

Note, Measures of many Cubits Length are express'd only in Foot-Measure.

		Cubits.
A Fathom is	- - - - -	= 4 = 7.296
Exekiel's Reed	- - - - -	= 6 = 10.944

A Schænus, the Egyptian Line for Land Measure, which I think Scripture useth to divide Inheritances, *Psalms* xvi. 6, and lxxviii. 55. They used different Lengths, but the shortest, and most useful was - } = 80 = 145.92

Herodotus mentions a Schænus just 300 times as long: I judge that all the greater were made in Proportion to the least.

The Mile is	- - - - -	= 4000 = 7296.
The Stadium	= $\frac{1}{6}$ of their Mile	= 400 = 729.6
The Parasang	= $\frac{1}{3}$ of their Miles	= 1200 = 4 English Miles, and 580 Feet.

TABLE II.

Of Measures of Surface.

Moses hath described these by square Cubits. I here express them reduced to our square Feet: The Method of this Reduction is taught in the following Appendix; but here I shall

First, Propose three clear Examples given by *Moses*.

Secondly, Place six Instances of greater Difficulty.

First, The clear Examples are

1. The *Altar of Incense*. Only two Sides of it, *viz.* its Length and Breadth, are expressed by *Moses*; each of them is affirmed to be one Cubit. Yet he declares that it was four square: Whence we collect, that it was just one square Cubit. See *Exod.* xxx. 2. Now it is demonstrated in the *Appendix*, that one *Jewish* square Cubit amounts to, in Surface, three *English* square Feet, and about 47 square Inches.

2. The *Table of Shew Bread*, *Exod.* xxv. 23. It is affirmed to be two Cubits in Length, and one in Breadth: None doubt but it was rectangular, containing two *Jewish* square Cubits. These amount to above six *English* square Feet, and above half, *viz.* 94 square Inches.

3. The *Boards of the Tabernacle*, each 10 Cubits in Length and 1 and a half in Breadth, *Exod.* xxvi. 16, being rectangular, must contain 15 square Cubits, *Jewish*. These are proved to contain very near 50 square Feet of *English* Measure.

Secondly, The six Instances, or Cases of greater Difficulty, reserved to the *Appendix*, are

1. The *Mercy Seat*, whose Surface is = 12 square Feet and a Half.

2. A general Method is taught of reducing any given Number of *Jewish* Cubits to *English* square Feet.

3. The Example of the 15 square Cubits in the *Boards of the Tabernacle* is made clearer.

4. The *Court of the Tabernacle*, described *Exod.* xxvii. 18, is found to be just Half the *Egyptian Aroua*, and to contain 1 Rood, 21 Perches, 27 square Feet, &c.

5. The whole *Aroua* is determined, and reduced to our *English* Measures, *viz.* 3 Roods, 2 Perches, 55 square Feet.

6. The *Suburbs* or *Glebe-Land*, given to each City of the *Levites*, *Numb.* xxxv. 3, 4, 5 is shewed to be a Square, on each of the four Sides of every City, containing a Million of *Jewish* square Cubits, or 100 *Aroua*; which amount to, in each Square, 76 Acres, 1 Rood, 20 Perches, 80 square Feet: Whence we collect, that all the four Squares amounted to 305 Acres, 2 Rods, 1 Perch, 51 square Feet.

T A B L E III.

Of Measures of Capacity.

	Wine Gall.	Pts.	In.	fol.
An <i>Epba</i> , or <i>Bath</i> - - - - -	7	4	15.	
A <i>Chomer</i> (<i>Homer</i> in our Translation) - -	75	5	7.	
A <i>Seah</i> , $\frac{1}{2}$ of an <i>Epba</i> - - - - -	2	4	3.	
A <i>Hin</i> , $\frac{1}{6}$ of an <i>Epba</i> - - - - -	1	2	1.	
An <i>Omer</i> , $\frac{1}{10}$ of an <i>Epba</i> (<i>Exod.</i> xvi. 36) -	0	6	0.5	
A <i>Cab</i> , $\frac{1}{18}$ of an <i>Epba</i> - - - - -	0	3	10.	
A <i>Log</i> , $\frac{1}{72}$ of an <i>Epba</i> - - - - -	0	0 $\frac{1}{2}$	10.	
The <i>Metretes</i> of Syria (<i>John</i> ii. 6.) = <i>Congius</i> }	0	7 $\frac{1}{8}$	0.	
<i>Romanus</i> or <i>Roman Gallon</i> - - - - - }				
The <i>Cotyla</i> , Eastern, $\frac{1}{160}$ of an <i>Epba</i> - -	0	0 $\frac{1}{2}$	3.	
This <i>Cotyla</i> contains just 10 Ounces <i>Avoirdupois</i> of Rain Water				
The <i>Omer</i> - - - 100 d°				
The <i>Epba</i> - - - 1000 d°				
The <i>Chomer</i> - - - 10000 d°				

So by these Weights all these Measures of Capacity may be expeditiously recovered, very near Exactness.

Note 1, The above Measures, with Regard to their Quantities, are not exact in their several Parts; which inclines me to think they are erroneously printed in the Quarto Bibles (for they were taken from thence) though I imagin those Errors (if any) to be very small. However, whether right or wrong, I chose at this Time to copy them just as they are, till I can get an Opportunity of comparing them with some former Editions of that Bible; and also because they are said to be calculated by the Right Reverend Richard, Lord Bishop of Peterborough.

2. With Regard to the *Cotyla*, it is observed to weigh just 10 Ounces *Avoirdupois* of Rain Water, and to contain an English Wine Half Pint, and three solid Inches over. Now it is known that the Standard Wine Gallon contains 231 solid Inches, consequently the Wine Half Pint contains 14 solid Inches, and .4375 Parts of such an Inch: And from an Experiment made by the late Mr. Ward (*Young Math. Guide*, p. 120) a cubic Inch of common Water (he does not say whether Rain, River, or Spring Water) weighs .578697 Parts of an Ounce, that is very little more than Half an Ounce. Hence, if the *Cotyla* weighs just 10 Ounces *Avoirdupois*; the Cubic Inch of Water Half an Ounce, and that there are 14 Inches and almost an Half solid in a Wine Half Pint, the *Cotyla* will contain no more than Half a Pint Wine Measure, and 2.843045 solid Inches, as appears by the following Proportions, viz.

oz.	Cub.In.	oz.	Cubic In.
.578697	: 1	: 10	: 17.280545 +
Cub.In.	half Pt.	Cub.In.	half Pt.
14.4375	: 1	: 17.280545	: 1 & 2.843045

And this is another Reason, why I imagin there must be some misprinting, which the future Time may possibly discover.

T A B L E IV.

Of Weights and Coins.

Note 1. The Jewish Weights are reduced to the Standard Grains of our Troy Weight (whereof 438, are equal to the Roman Ounce) and to our ancient Avoirdupois Ounce.

2. The Value of the Jewish and Roman Weights and Coins, at the present Rate of Silver and Gold, is expressed in Pence and Decimal Parts of a Penny.

	Gr.	Pence.	£	s.	d.	gr.
A Shekel is the original Wt.	219.	= 28.2875	= 0	2	4	1.15
A Bekah, $\frac{1}{2}$ of a Shekel	109.5	= 14.14375	= 0	1	2	.14375
A Gerah, $\frac{1}{16}$ of a Bekah	10.95	= 1.414375	= 0	0	1	1.6575
A Maneh, = 100 Shekels	21900.	= 2828.75	= 11	15	8	3.
A Maneh, (in Coin) = 60 Shekels	13140.	= 1697.25	= 7	1	5	1.
A Talent of Silver, = 3000 She.	657000.	= 84862.5	= 353	11	10	2.

A Talent of Gold, the same Weight = 5329 11 4 3.5

Note, An Ounce of Standard Gold is worth 3 l. 17 s. 10 d. 2 grs. then by the following Proportion it will be

oz.	£	s.	d.	grs.
1	3	17	10 $\frac{1}{2}$	
657000	5329	11	4	3.5

The Golden Daries (Drams) mentioned Ezra ii. 69, seem to be Coins of Darius the Mede. They weighed 12 Gerahs

Gr.

= 131.4 = 0 1 4 3.89

Roman Money mentioned in the New Testament.

	d.	grs.
A Denarius, Silver	= 7	3
An As, Copper	= 0	3
An Assarium	= 0	1 $\frac{1}{2}$
A Quadrans	= 0	0 $\frac{1}{4}$
A Mite	= 0	0 $\frac{1}{5}$

A N
A P P E N D I X

T O T H E

Second TABLE of MEASURES of SURFACE,

Described by M O S E S,

Shewing the Method of reducing them by Calculation, to the Measures used in England, for the Benefit of those who understand Decimal Arithmetic, and desire to try the Reductions given in the Table, or to make further Improvements in this Kind of Measures.

I Shall begin with Reduction of the Measures of the *Mercy-Seat*, which was God's Throne of Grace among the *Jews*. *Moses* in *Exod.* xxv. 17, affirms, that its Length was two Cubits and an Half, its Breadth one Cubit and an Half. The Fractions adhering to its Length and Breadth, make some Difficulty to Beginners in Arithmetic, which the Decimal Way doth much abate. Supposing therefore, what in the Table is proved, that the *Jewish* Cubit was in Foot-Measure 1.824, the Length must then be 4.56 (for $1.824 \times 2.5 = 4.56$) and the Breadth must be 2.736 (for $1.824 \times 1.5 = 2.736$) wherefore the Product of these Numbers, *viz.* 4.56×2.736 gives its Surface 12.47616; if the Decimals be multiplied by 144 = the square Inches in a Foot square, the Product will be 68.56704 square Inches, and something above Half an Inch more.

2. In the Altar of Incense, *Exod.* xxx. 1, *Moses* describes the *Jewish* square Cubit, which (as was said before) was a Cubit long and a Cubit broad: Hence if the Length be multiplied by the Breadth, that is 1.824 by 1.824, the Product will be 3.326976, that is, 3 Feet and upwards: if the Decimals be multiplied by 144, the square Inches in a Foot square, the

the Product will be 47.684544, that is, 47 square Inches, and something more than half an Inch; so that the Surface of the Altar of Incense, at the Top, was 3 Feet, 47 Inches and an Half square. But the Altar had also four Sides, and was two Cubits high: Hence if the Height of the said Altar be multiplied by the Breadth at the Top, that is, two Cubits by one Cubit, or 3.648 by 1.824, it will give the Dimensions of each Side, because they were all alike, *viz.* 6.653952, or 6 Feet and upwards of Half a Foot square. If this Number be multiplied by 4, and the Top Surface added to it, that is, 6.653952 $\times$ 4 + 3.326976, the last Sum will give the whole Superficies of the said Altar, *viz.* 29.942782, or very near 30 Feet square. And as the Top and Sides were all overlaid with pure Gold, it must make the said Altar, according to our present Estimation of that Metal, very rich and valuable. If the Size of this Altar be required as to its Bulk, or outside Appearance, its Length was 1 Foot, 9 Inches, and .888 Decimal Parts of an Inch, its Breadth the same, and its Height 3 Feet, 7 Inches, and .776 Decimal Parts of an Inch; or, rejecting the Decimals, its Length was 1 Foot, 10 Inches, its Breadth 1 Foot, 10 Inches, and its Height 3 Feet, 8 Inches

By the same Rule we may form an Idea of the Bulk of the Ark of the Testimony, *Exod.* xxv. 10, which had the Mercy-Seat placed upon it, and the Testimony, which God gave to *Moses*, put within it, and thence called the Ark of the Testimony. The length of this Ark was two Cubits and an Half, the Breadth one Cubit and an Half, and the Height one Cubit and an Half: and as it was overlaid within and without, with pure Gold, and the Mercy-Seat upon it all of solid pure Gold also, together with the two Cherubims, with their out stretched Wings, of the like solid Gold, it must have been vastly more valuable than the Altar of Incense.

By the Rule just mentioned, we come also at the Size of the Table of Shew Bread, *Exod.* xxv. 23, which was two Cubits long, one Cubit broad, and one Cubit and an Half high. Also the Curtains for the Tabernacle, which were 28 Cubits long, and 4 Cubits broad; and the Curtains of Goat's Hair, which were thirty Cubits long, and four Cubits broad. It is likewise as easy to discover the greatest Size of the Altar of Burnt Offerings, mentioned *Exod.* xxvii. 1, which was five Cubits long, five Cubits broad, and three Cubits high: The Hangings for the Court of the Tabernacle, *Exod.* xxvii. 9, &c. which were Southward 100 Cubits long, and Northward 100 Cubits

Cubits long, also Westward 50 Cubits long, and Eastward 50 Cubits long, and all of them 5 Cubits high.

3. *Moses*, in *Exod.* xxvi. 16, describes the Boards of the Tabernacle, viz. ten Cubits in Length, and one Cubit and an Half in Breadth: Therefore to find the superficial Content of each Board, we are only to multiply the Length by the Breadth. Now 10 Cubits are equal to $10 \times 1.824 = 18.24$ Feet; and one Cubit and an Half are equal to 2.736 Feet, therefore 18.24×2.736 will give 49.90464, that is, 50 square Feet very near, for the Content of every Board of the Tabernacle.

4. We come next to the Measure of the Surface of Lands. And first of the Court of the Tabernacle, or the Ground on which the Priests performed all the solemn public Worship of *Israel*, in the Time of *Moses*. The Area of this Court is described by *Moses*, *Exod.* xxvii. 18, by its Length 100 Cubits, and its Breadth every where 50 Cubits: Wherefore this Area must be in *Jewish* Measure 5000 square Cubits, that being the Product of 100 multiplied by 50. Now as 3.326976 Feet square make a square Cubit, that Number multiplied by 5000 will give 16634.88 for the *English* square Feet, and Decimal Parts of a Foot. But because such long Numbers are not easily retained in our Memories, they may be reduced into Perches, or Roods, or Acres, which contain known Numbers of square Feet. Thus, a Perch is 5 Yards and an Half, or 16 Feet and an Half long, and consequently a square Perch is 16 Feet and an Half long, and 16 Feet and an Half broad, making 272.25 square Feet, or 272 square Feet and one Quarter; a square Rood contains 40 times as much, or 10890 square Feet, and an Acre contains four times that Quantity, or 43560 square Feet: Hence it appears that the aforementioned Area of the Court of the Tabernacle is greater than a Rood, and less than an Acre; but as Subtraction can be made but once, it appears that that Area is not so much as two Roods, though it is greater than one Rood: Then if the following Calculation take place, the Area will be 1 Rood, 21 Perches, 27 square Feet, and a very little above half a Foot more.

Sq. Feet	Rood	Sq. Feet.	R. Per.	Feet.
10890	: 1	: 16634.88	: 1	21 27.62793

Hence it must be understood of the whole Piece of Ground, including that whereon the Tabernacle stood, as well as the Court round about the Tabernacle. However, lest the Read-

er should be at a Loss to find out the foregoing Solution, it is given at large, as follows, *viz.*

<i>Rood.</i>	
108910.) 16634.8800010	(1.527537
1089	40
5744	<i>Per.</i> 21.101480
5445	272.25 Feet in 1 <i>Perch.</i>
2998	507 40
2178	2029 6
8208	20296
7623	71036
5850	27.6279300 Feet
5445	
4050	
3267	
7830	
7623	
207	

But reflecting upon the Measure by Cubits, used by *Moses*, and finding them to be precisely 5000 square Cubits, it was observed by his Lordship of *Peterborough*, to be just Half 10000, which he had observed from *Herodotus's* *Euterpe*, to be the Area of the *Egyptian Aroura*, by which their Land was as generally measured as ours is by Acres and Roods. See *Herodot.* l. 2. cap. 168. He called also to Mind a Passage in *Manetho*, an *Egyptian* Priest, cited by *Josephus*, in his first Book against *Apion*, where he affirms that *Manetho*, in his History of the Reign, Wars, and Expulsion of the *Pastors* (whom *Africanus* affirms to be *Phœnicians*, or *Canaanites*, and *Josephus* vainly believed to be *Jews*) wrote out of the public Records of *Egypt*, that these *Pastors* made at *Abaris*, a very large and strong Encampment, that encompassed 10000 *Aroure* sufficient to contain 240000 Men, and long enough to maintain their Cattle. Hence it appears, that not only the *Egyptians*, but the *Phœnicians* or *Canaanites* also, that had dwelt among them, and had reigned there during the Time of six Kings

Kings successively, used this Measure of Land, called *Aroura*. Now this was long before the Time of *Moses*; for the Beginning of *Amosis* or *Tethmosis*, who expelled them out of *Egypt*, was very near the Time of *Abraham's* Death, as appears by the Annals of the late learned Primate of *Ireland* (whom I imagine to be Archbishop *Usher*.) Wherefore I believe (says his Lordship of *Peterborough*) that *Moses*, who was skilled in all *Egyptian* Learning, especially surveying, did, of Choice, make the Court of the Tabernacle to be just Half an *Aroura*, which was a known Measure to him and his People, who had long dwelt in *Egypt*, and Divine Authority directed him so to do.

5. It was made to appear from *Herodotus*, that an *Aroura* is the square of 100 *Jewish* or *Egyptian* Cubits, and 100 such Cubits contain 182 Feet, and .4 in *English* Measure (for $1.824 \times 100 = 182.4$) it follows that $182.4 \times 182.4 = 33269.76$ square Feet, equal to the square Feet in an *Egyptian Aroura*, equal to 3 Roods, 2 Perches, 55 square Feet, and little more than a Quarter of a Foot; as appears by the following Arithmetic, the Proportion being the same as before.

Sq. Feet.	Rood.	Sq. Feet.	R.	P.	Sq. Feet.
10890	: 1	: 33269.76	: 3	2	55.25586

Note, The fourth Term is found in the same Manner as that is, which discovers the Area of the Tabernacle, and for that Reason the Operation at large is omitted

To this Place may be referred the Use of the lesser Sort of $\chi\omicron\upsilon\upsilon\theta$, *Choinos*, which yet is most convenient for the Use of the *Egyptians*, and of the *Jews*, to measure out private Mens Inheritances, by a Line which was 80 Cubits long. For the Length of this Line will measure one Side of an *Aroura*, if the other Side be 125 Cubits long, which is the Length of this Line, and its Half, and 5 Cubits above Half of it, which they might easily mark in it, by a Knot or a Ring. And by this Means, they might easily lay any Number of *Aroure* together, all of them rectangular, and parallel to each other. Such Lines, his late Lordship of *Peterborough* supposed for Measure of Inheritances, are intimated *Psalms* xvi. 6, where it is said *The Lines are fallen unto me in pleasant Places; yea, I have a goodly Heritage.* Also *Psalms* lxxviii. 55, *He cast out the Heathen also before them (i. e. the Jews) and divided an Inheritance by Line, and made the Tribes of Israel to dwell in their Tents.* See the new or Bible Translation.

6. The last Particular, which I shall take Notice of, relating to the *Jewish* Measures, is concerning the Suburbs or Glebe Land given to each City of the *Levites*, mentioned
Numbers

Numbers xxxv. 3, 4, 5, which runs thus, And the Cities shall they have to dwell in, and the Suburbs of them shall be for their Cattle, and for their Goods, and for all their Beasts. And the Suburbs of the Cities, which ye shall give unto the Levites, shall reach from the Wall of the City outward, a thousand Cubits round about. And ye shall measure from without the City, on the East-Side two thousand Cubits, and on the South Side two thousand Cubits, and on the West-Side two thousand Cubits, and on the North-Side two thousand Cubits: And the City shall be in the midst: This shall be to them the Suburbs of the Cities. Here *Moses* describes what Measure of Land the *Levites* were to be allowed for their Cattle, their Goods, and all their Beasts, on the North, East, South and West-Sides of each of their Cities: So that the City was to be exactly in the midst of the Land belonging to it. This Land in our Translation is called *Suburbs*, because of its nearness to all their Cities. But we must not thence imagin, that it means Houses and Streets, adjoining to their Streets, in which Sense we sometimes use the Word *Suburbs*. For *Moses* plainly tells us they were Places for their several Sorts of Cattle to feed in, such as might also be Orchards or Gardens for Fruits, or perhaps for a little Corn, comprehended in the Words *their Goods*. These Fields, Orchards, or Gardens, he limits by 1000 Cubits, which was just a Quarter of an Eastern Mile, but amounts, in meer Length, to 608 Yards *English* Measure, thus,

$$\begin{array}{r} \text{Foot.} \\ \text{A Cubit} = 1.824 \\ \hline 1000 \end{array}$$

3) 1824.000 (608 Yards
this therefore exceeds a Quarter of an *English* Mile, by 168 Yards in Length; thus,

$$\begin{array}{r} 4) 1760 \text{ Yards make a Mile} \quad 608 \\ \hline \quad 440 \\ 440 \text{ Yards make a Quarter of a Mile} \quad 440 \\ \hline \quad 168 \text{ Yds.} \end{array}$$

But it is certain that Cattle cannot feed upon meer Length, any more than Orchards or Gardens can consist of such lineal Measure: The 1000 Cubits therefore, just mentioned, must signify the Side of some Surface of Land bounded thereby, and we must have two Sides of that Surface given, before we can find the Area, or Surface contained. Therefore *Moses*, *ver. 5*, tells us, that on each Side of every City they must measure 2000 Cubits,

Cubits, which will determin no Surface, unless we understand it to mean the two Sides of a Square, bounded on every Side by 1000 Cubits; these two Sides multiplied into each other, will produce a Square, that contains just a Million of square Cubits; thus,

$$\begin{array}{r} 1000 \\ 1000 \\ \hline 1000000 \text{ Square Cubits.} \end{array}$$

and that is a known and exact Measure of just 100 *Aroure*: and this shews that the 2000 Cubits mentioned *ver.* 5, are the two Sides of that Square, whereof the 1000 Cubits mentioned *ver.* 4, is one of those Sides, and may be called the Root of the Square. This shews the Agreement of the two different Numbers; and to find the superficial Content of a Square, each of the Sides of which are 1000 Cubits, the following Arithmetic will determin, though it stands a little contracted.

1. 1000 Cubits are equal to 1824 *English* Feet.
2. $1824 \times 1824 = 3326976$ Feet square.
3. A square Acre contains 43560 Feet square.
4. $43560 \div 3326976 = 76.376859$

$$\begin{array}{r} 4 \\ \hline 1.507436 \\ 40 \\ \hline 20.297440 \end{array}$$

Hence it appears, that in a Square, each of whose Sides were 1000 Cubits, there are upwards of 76 Acres, 1 Rood, and 20 Perches: And to find the proper Quantity of the remaining Decimals, let .29744 be multiplied by 272.25, the square Feet and Decimals in a Perch, the Product is 80.97804 that is, very nearly 81 Feet. Hence it appears, that every Square on each Side of every *Levitical* City, contained, according to our Measure, 76 Acres, 1 Rood, 20 Perches, 81 square Feet, equal to a Million of square Cubits, *Jewish* Measure; and if the Sum of the four Squares belonging to each City be required, you need only multiply the Content of one Square

Square by four, and you have the whole Content of the Ground belonging to each City; thus,

A.	R.	P.	Sq.F.	
76	1	20	81	the superficial Content on each Side.
				4
305	2	0	324	
				272.25 square Feet in a Perch.
305	2	1	51.75	

But here is one Particular more to be observed, which is nowhere mentioned in sacred Writ; and that is, the several superficial Contents of the Ground on which every City stood; whether they were all alike, or whether one City was greater than another. Now as the Scriptures are intirely silent in this Respect, we are left wholly to Conjecture; and as there is as much Reason to imagin they were all alike, as that they were not so; I see no Harm, if for once, we suppose them all of a Size, since for Regularity's Sake, it is no way inconsistent; and that there might be Room enough for Families to increase for a long Time, it is not contradictory to Reason, to suppose the Quantity of Ground assigned for each City to be very superior, in Proportion to the Number of Inhabitants at that Time to make up that City, and that each City was an exact Square. However, we are yet at a Loss to know how the Suburbs belonging to each City were placed, though they were all of them to take the Beginning of their Measurements from the several Walls of each City; and among the several Ways of placing the Suburbs, there seems to me to be but three, which may be called regular, each of which I shall exhibit in Lines geometrically, to help the Idea of the Reader,



As the *Levites* were to have 48 Cities, with their Suburbs, it will be very easy at any time, to find the whole Quantity of Ground belonging to all the Suburbs, by multiplying the Quantity

Quantity of Ground contained in the Suburbs of one City by 48, or by the Parts thereof, which will produce 14666 Acres, 2 Roods, very little more or less, rejecting some smaller Quantities, which in this Case are trifling.

Note, In Exod. xxix. 40, Mention is made of a Tentb-deal of Flour; but what that Quantity is, in our Measure, I am at a Loss to know at present. However I chose just to mention it here, that it might not appear to be either overlook'd or forgot.

Before this Part is quitted, it will be worth the while to make an Observation concerning Ingenuity, or Perfection in Workmanship.

Fine Performances of any Kind, are, and always have been, very much valued, and justly esteemed: And History will furnish us with singular Productions, more than enough for our present Purpose. But without enumerating any of them, we may challenge the whole World to produce such Pieces of Mechanism, by their own Inventions, as were wrought by Men, who were immediately instructed by the great Creator of the Universe: Nor can any Performances, how beautiful and ingenious soever they be, stand in Competition with those which were wrought by divine Inspiration. We have God Almighty's own Word for it, *Exod. xxviii. 2; 40*, that they were to be made for *Glory* as well as *Beauty*; and *Exod. xxxi. 2*, and following Verses, that *Bezaleel, Aboliab*, and others, were those inspired Persons who were to make all those *glorious and beautiful Works*; consequently all meer human Pieces of Mechanism, even the very best of them, must fall vastly short of that Perfection, which was seen in the Workmanship of the *Tabernacle of the Congregation, and the Ark of the Testimony, and the Mercy-Seat, and all the Furniture of the Tabernacle, and the Table and his Furniture, and the pure Candlestick with all his Furniture, and the Altar of Incense, and Altar of burnt Offering with all his Furniture, and the Laver and his Foot, and the Clothes of Service, and the holy Garments for Aaron, and of his Sons, to minister in the Priest's Office*: And since these Men were filled with the Spirit of God in *Wisdom and Understanding, and in Knowledge, and in all Manner of Workmanship, to devise cunning Works, to work in Gold, and in Silver, and in Brass, and in cutting of Stones to set them, and in carving of Timber*, what could the Workmanship of all these be less than exquisitely curious, even in the most Superlative Degree! Certainly, if ever Art could be said to have arrived to any Degree of Perfection, it was in the *Tabernacle of God, and all its Apparatus, which were really Master-Pieces of their Kind*; such as for *Glory and Beauty of Workmanship*,

Workmanship, the World never saw before, nor will ever see again. And because some Men have already entertained, and others I fear do still entertain, mean and contemptible Thoughts of, and strongly object against all the aforementioned holy Works, which were directed by God himself, and shewn to *Moses* by way of Pattern, while he was with God on the Mount, I have made Choice of the foregoing Argument to close this Appendix with, in order to obviate, as much as possible, all such vain and sinful Objections.



Miscellaneous Arithmetic :

OR A FULL

ACCOUNT of the NEW CALENDAR, &c.

PART III.

Of the NEW CALENDAR.

I. Of the Golden Number.

 HE Golden Number, which is also called the Prime, is a circular Revolution of nineteen Years, in which Time it hath been supposed, the Sun and Moon do finish their Variety of Aspects.

R U L E.

When 1 to th' Year hath added been,
That Sum divide by just 19.
By th' Quote, the Revolution's shewn;
Th' Remainder is the Prime well known.

Note 1, One is added to the given Year, because this Revolution began one Year before the Birth of Christ.

2. If nothing remains, the Golden Number is 19, and the given Year is the last Year of the Revolution.
3. The Prime changeth the first Day of January.
4. It is called the Golden Number, because anciently, it used to be set down in the Calendar in Golden Letters.

E X A M P L E.

What is the Golden Number for the Year 1764 ?

$$\begin{array}{r}
 1764 \\
 1 \\
 \hline
 19 \overline{) 1765} 92 \\
 \underline{171} \\
 55 \\
 \underline{38} \\
 17 \\
 \hline
 \end{array}$$

Answer. The Golden Number is 17, and there have been 92 Revolutions since the Birth of Christ.

2. Of

2. Of the CYCLE of the SUN.

THE Cycle or Circle of the Sun is a Revolution of 28 Years, in which Time all the Variety of Dominical Letters and Leap Years expire; except in the Year 1800, which will make some Alteration.

R U L E.

To th' given Year add 9 complete;

That Sum divide by 28:

The Quote, the Revolutions tell,

Th' Remainder shews the Cycle well.

Note 1, Nine is added to the given Year, because this Revolution began nine Years before the Birth of Christ.

2. If nothing remains, the Cycle is 28, and the given Year is the last Year of the Cycle or Revolution.

3. The Cycle changes the first Day of January.

E X A M P L E.

What is the Cycle of the Sun for the Year 1764?

$$\begin{array}{r}
 1764 \\
 \underline{9} \\
 28 \overline{) 1773} 63 \\
 \underline{168} \\
 .93 \\
 \underline{84} \\
 .9
 \end{array}$$

Answer. The Cycle is 9, and there has been 63 Revolutions.

3. Of the E P A C T.

THE Epact is 11 Days nearly, which the Moon wants of the Solar Year, which is 365 Days, 5 Hours, 48 Minutes, and 55 Seconds, whereas the Lunar Year is but 354 Days, 8 Hours, 48 Minutes, and 38 Seconds: Or, it is the Moon's Age at the Beginning of January.

R U L E.

Take 1 from the Prime, multiply 't by 11,
Divide that by 30, the Epact is given.

E X A M P L E.

EXAMPLE.

What is the Epact for the Year 1764?

$$\begin{array}{r}
 \text{The Prime, or Golden Number, is} \quad - \quad - \quad - \quad - \quad - \quad - \quad - \quad - \quad - \quad - \quad 17 \\
 \text{From which subtract} \quad - \quad - \quad - \quad - \quad - \quad - \quad - \quad - \quad - \quad - \quad 1 \\
 \hline
 \text{And there remains} \quad - \quad - \quad - \quad - \quad - \quad - \quad - \quad - \quad - \quad - \quad 16 \\
 \text{This multiply by} \quad - \quad - \quad - \quad - \quad - \quad - \quad - \quad - \quad - \quad - \quad 11 \\
 \hline
 \text{And divide by} \quad - \quad - \quad - \quad - \quad - \quad - \quad - \quad - \quad - \quad - \quad 30 \overline{) 176} \begin{array}{l} 5 \\ 150 \\ \hline 26 \end{array} \\
 \hline
 \text{The Epact is} \quad - \quad - \quad - \quad - \quad - \quad - \quad - \quad - \quad - \quad - \quad 26
 \end{array}$$

Note 1. The Epacts are the same every 19 Years

2. The Epact changes the first Day of January.

3. One is taken from the Prime, because the Prime began 1 Year before the Birth of Christ

4. The Epacts always proceed by the Addition of 11, till the Golden Number happens to be 19, and then the Number 12 is added for the Epact of the following Year.

5. As often, as by the Addition of several Epacts together, the Number 30 shall be included in the Sum, 30 must be taken away, and what remains is to be retained for the Epactal Number of the following Year; hence every third Year in which 30 is cast away, there happens an Embolismical Moon, that is, 13 Moons in that Year; the last Moon in that Year being the Intercalary or Embolismical Moon.

6. The Quotient of the Division by 30, shews how many Embolismical Moons have happened since the first Year of that Cycle.

7. By the foregoing Rule, the following Table is calculated, as appears from the above Operation, where the Golden Number being 17, the Epact is 26.

A TABLE of the EPACTS for every Golden Number.

Golden Numbers.	Epacts.	Golden Numbers.	Epacts.	Golden Numbers.	Epacts.
I	30 or 0	VIII	17	XV	4
II	11	IX	28	XVI	15
III	22	X	9	XVII	26
IV	3	XI	20	XVIII	7
V	14	XII	1	XIX	18
VI	25	XIII	12		
VII	6	XIV	23		

Its Use.

It is only of use to know, at Sight, what Epact belongs to any particular Golden Number.

4. Of

4. OF BISSEXTILE OR LEAP YEAR.

LEAP YEAR has one Day more in *February* than any other Year; because the common Year, or Course of the Sun, is computed to be six Hours more than 365 Days, which in four Years Time make a Day, called in the ancient Roman Calendar *Bissextile*, which Day was then appointed to be the Day before the 24th Day of *February*.

By the Statute *De anno bissextile*, 21 Hen. III. Anno Dom. 1236, to prevent Misunderstandings, the intercalary Day, and that next before it, are to be accounted as one Day: Though Astronomers do not regard it now, because St. *Matthias's* Day is placed on the 24th of *February*, both in a common Year and Leap Year, which otherwise, in a Leap Year used to be on the 25th Day, they placing the intercalary Day next after the 28th, which makes in the Leap Year 29 Days.

The Statute runs thus,

The King unto his Justices of the Bench, greeting. Know ye, That where within our Realm of England, it was doubted of the Year and Day that were wont to be assigned unto sick Persons being impleaded, when and from what Day of the Year going before unto another Day of the Year following, the Year and Day in the Leap Year ought to be taken and reckoned how long it was.

II. *We therefore, willing that a Conformity be observed in this Behalf every where within our Realm, and to avoid all Danger from such as be in Plea, have provided, and by the Counsell of our faithfull Subjects, have ordained, That, to take away from henceforth all Doubt and Ambiguity that might arise hereupon, the Day increasing in the Leap-Year shall be accounted for one Year, so that because of that Day none shall be prejudiced that is impleaded, but it shall be taken and reckoned of the same Month wherein it groweth, and that Day, and the Day next going before, shall be accounted for one Day. And therefore we do command you, that from henceforth you do cause this to be published afore you, and be observed. Witness myself at Westminster, &c. Vid. Keble's Statutes at Large, p. 9 and 10.*

But as this Method of allowing the *Julian* Year to consist of 365 Days, 6 Hours, instead of 365 Days, 5 Hours, 48 Minutes, 55 Seconds, which is the true Solar Year, has obtained since the Reformation of the Calendar by the Council of *Nice*, in the Year 325, to the Year 1751 inclusive, it has brought the Equinoxes and Solstices 11 Days nearly, or 10 Days, 23 Hours, 24 Minutes, 50 Seconds, earlier than by the *Julian* Account they are supposed to be. As appears by multiplying

multiplying the Difference between the Julian Year and the true solar Year, by the Difference between the Years 325 and 1751.

Thus 365 D. 6 hrs. — 365 D. 5 hrs. 48 m. 55 sec. = 11 m. 5 s.

Again 1751 — 325 = 1426

M. Sec. Days. hrs. min. sec.

Lastly 11 5 × 1426 = 10 23 24 50

In plain Numbers thus.

	D.	h.	m.	s.	Yrs. of our Lord.
Julian Year	365	6	0	0	1751
Solar Year	365	5	48	55	325
Difference	0	0	11	5	1426

M. sec.

11 5

60

665

1426

3990

1330

2660

665

610

24 D. h. min. sec.

610)9482910(158014(263(10 23 24 50

50 24 23

R U L E.

Divide the Year by 4, what's left shall be
For Leap Year 0, for past, 1, 2, or 3.

Note, This Rule, since the Act for regulating the Commencement of the Year, will not always be true: for neither the several Years 1800, 1900, 2100, 2200, 2300, nor any other hundredth Year of our Lord, where the even Hundreds are not divisible by 4 without a Remainder, will be Leap-Years. But in all other Respects the common Years will be the same, and the Leap Years will contain 366 Days, as usual: but because in every 400 Years, by admitting the Year to be 365 Days, 6 Hours, and the Leap Year to consist of 366 Days, there will be gained 3 D. 1 h. 53 m. 20 s. therefore one Day is taken off from every hundredth Year, where the Hundreds are not divisible by 4, which will be 3 times in every 4 hundred Years, making

E

just

just 3 Days. By this Means the Equinoxes and Solstices are brought back again to their proper Days. This Method is not exact, but the Error is so small as to leave an Exceeding of only 1 h. 53 m. 20 sec. in 400 Years, which will not amount to 24 Hours in 5082 Years, as appears by the following Calculation, viz.

665 = the Seconds gain'd in 1 Year.

$$\begin{array}{r} 400 \\ \hline 60 \quad 24 \quad D. \quad h. \quad m. \quad sec. \\ 60) 266000 (443 \quad 73 \quad 3 \quad 1 \quad 53 \quad 20 \\ \quad 20 \quad 53 \quad 1 \end{array}$$

Now the 3 Days being taken off as before mentioned, there will remain only 1 h. 53 m. 20 sec. then by the Rule of Three,

H.	m.	s.	Yrs.	hrs.
1	53	20	: 400	: : 24
60				60
113				1440
60				60
6800				86400
				400
				Yrs.
68100) 345600 (5082				$\frac{24}{83}$
				340
				560
				544
				160
				136
				24

EXAMPLES.

1. The Year 1764, is it a common Year or Leap Year?

$$4) 1764 (441$$

Answ. Bissextile or Leap Year, because nothing remains.

2. The Year 1765, is it a common Year or Leap Year?

$$4) 1765 (441$$

I

Answ. A common Year, or the first after Bissextile or Leap Year.

5. Of the DOMINICAL LETTER.

THE Dominical Letter is one of the first seven Letters of the Alphabet in the Calendar expressing Sunday, from *Dominicalis*, belonging to Sunday or the Lord's Day.

RULE.

R U L E.

The Year, it's Fourth and 1 together add;
Let 7 divide : What's left, the Letter's had.

- Note 1, In every Leap-Year there are two Dominical Letters; one serves to the 29th of February (which before used to be the 25th, according to the Act of King Henry III.) and the other to the End of December.
2. This Rule finds only the latter Dominical Letter in Leap-Year.
3. The Dominical Letter goes backward in a common Year one Letter, but in Leap-Year two Letters.
4. This Rule finds the Dominical Letter till the Year 1799 inclusive: but from 1800 to the Year 1899 both inclusive, you must add to the current Year only its fourth Part.

E X A M P L E.

What is the Dominical Letter for the Year 1764?

The Year — — 1764
Its Fourth — — 441
Add — — — —

$$7)2206(315 \text{ \& 1 over} = G.$$

according to the annexed Table.

0	A
1	G
2	F
3	E
4	D
5	C
6	B

Another Way to find the Dominical Letter.

R U L E.

Add the Year and its Fourth, then divide by just 7,
What's left take from 7; the Letter is given.

E X A M P L E S.

1. What is the Dominical Letter for the Year 1764?

$$\begin{array}{r} 4)1764 \\ \underline{541} \\ 7)2205(315 \end{array}$$

$$7 - 0 = 7 = G$$

1	A
2	B
3	C
4	D
5	E
6	F
7	G

2. What is the Dominical Letter for 1765?

4) 1765

441

7) 2206(315

7 - 1 = 6 = F

Note, I have used this Method in the Rule for finding of Easter-Day.

6. To find what Day of the WEEK, any Day of any MONTH falls on.

FIND the Dominical Letter (which expresses *Sunday*) for the Year given; and with it reckon downward in the Calendar, in the Month given, till you come to the given Day, which shews the Day of the Week required.

Note, In Almanacs, the Dominical Letter is known by its being a Red and Capital Letter.

When any Calendar is wanting observe this

R U L E.

At *Dover* dwells *George Brown*, Esquire,
Good *Caleb Finch*, and *David Fryer*.

Here it is to be observed, that each Line contains six Words, answering to six Months, and the first Letter of each Word is the Letter of the first Day of each Month in order, as

Jan. A. Feb. D. Mar. D. Apr. G. May B. June E.
July G. Aug. C. Sept. F. Oct. A. Nov. D. Dec. F.

So then knowing the Dominical Letter, and the Letter belonging to the first Day of the Month, 'tis easy to find the Day of the Week required.

E X A M P L E.

What Day of the Week will *December* the 5th be in the Year 1765?

The Dom. Letter
for the Year 1765
is F.

1 f or Sunday
2 g Monday
3 a Tuesday
4 b Wednesday
5 c Thursday

Ans. Thursday.

7. OF EASTER LIMIT.

EASTER LIMIT is the Paschal full Moon, and is an uncertain Number of Days from *March 1*, inclusive, and helps to find *Easter-Day*.

Note, It is called an uncertain Number of Days from *March 1*, because it is in one Year more, and in another less.

R U L E.

The Epact, more 6, from which 30 reject;
That taken from 50, gives the Limit direct,
Which if it exceed 31, this pray do,
Reject *March's* Days, and 'twill *April's* Day shew.

E X A M P L E S.

1. What is *Easter Limit* for the Year 1764?

$$\text{Epact} = 26$$

$$\text{Add} - 6$$

32 which because it is more than 30

subtract 30 from it

2 which subtracted

from - 50

The Remainder, or Limit is 48 Days from *March 1*.

Subtract 31 for the Days in *March*

Remainder is the 17th Day of *April*.

2. What is *Easter Limit* for 1765?

$$\text{Epact} - 7$$

$$\text{Add} - 6$$

13 which because it is less than 30

Subtract from 50

The Remainder, or Limit is 37 Days from *March 1*

Subtract 31 for the Days in *March*

Remainder is the 6th Day of *April*.

According to this Method, the following Table of *Easter* Limits, or Paschal Full Moons, is calculated; the Golden Numbers and Epacts being first known, as before taught.

A TABLE of the Golden Numbers, Epacts and Paschal Full Moons, for every 19 Years, till the Year 1899 inclusive.

Golden Numbers	Epacts	Paschal Full Moons.	Golden Numbers	Epacts	Paschal Full Moons.
I	0	April 13	XI	20	March 24
II	11	2	XII	1	April 12
III	22	March 22	XIII	12	1
IV	3	April 10	XIV	23	March 21
V	14	March 30	XV	4	April 9
VI	25	April 18	XVI	15	March 29
VII	6	7	XVII	26	April 17
VIII	17	March 27	XVIII	7	6
IX	28	April 15	XIX	18	March 26
X	9	4			

From this Table, calculated according to the orderly Proceeding of the Golden Numbers, is framed the following Table for finding of *Easter Day*, as it stands in the Act of Parliament for regulating the Commencement of the Year; and for correcting the Calendar now in Use; and also in the Common Prayer-Books, before the Order for Morning Prayer.

A TABLE

A TABLE to find EASTER-DAY till the Year 1899 inclusive.

Golden Number.	Day of the Month.	Sunday Letter.
14	Mar. 21	C
3	22	D
	23	E
11	24	F
	25	G
19	26	A
8	27	B
	28	C
16	29	D
5	30	E
	31	F
13	Apr. 1	G
2	2	A
	3	B
10	4	C
	5	D
18	6	E
7	7	F
	8	G
15	9	A
4	10	B
	11	C
12	12	D
1	13	E
	14	F
9	15	G
	16	A
17	17	B
6	18	C
	19	D
	20	E
	21	F
	22	G
	23	A
	24	B
	25	C

The Construction.

This Table is made by setting down the Days of the Month in their natural Order, and the Sunday Letters against them, the same as they are in the Calendar, or the common Almanacs; and then place such Golden Number against its Day, as the preceding Table directs, and thus is the Table completed.

Use.

This Table contains so much of the Calendar as is necessary for the determining of *Easter*; to find which

1. Look for the Golden Number of the Year in the first Column.

2. Against that stands the Day of the Paschal Full Moon, in the second Column.

3. Look in the third Column for the Dominical or Sunday Letter for the same Year, next after the Day of the Full Moon.

4. The Day of the Month, in the second Column, standing against that Sunday Letter is *Easter Day*.

Note. If the Full Moon happens upon a Sunday, then the next Sunday after is *Easter-Day*.

Example. What is *Easter-Day* for 1764?

The Golden Number for that Year is 17, and the Dominical Letter is G.

1. Look for 17 in the first Column.

2. Against it stands April 17, in the second Column.

3. Guide your Finger downward in the third Column till you come to G.

4. Against it, in the second Column is April 22, which is *Easter-Day*.

8. OF EASTER-DAY.

EASTER-DAY, on which all the other moveable Feasts depend, is always the first *Sunday* after the Full Moon, which happens upon, or next after the 21st Day of *March*; and if the Full Moon happens upon a *Sunday*, *Easter-Day* is the *Sunday* after, and never happens before *March 22*, nor after *April 25*.

R U L E.

First take from the Limit the * Letter and 4;
What's left from next 7's take, but nothing more;
This add to the Limit, and then you will see
What Day of the Month in *March* *Easter* will be:
Which Number, if more 'tis than 30 and 1,
Subtract *March's* Days, then for *April* 'tis done.

* Note, By the Letter, is to be understood the second Way of finding the Dominical Letter, as before mentioned.

E X A M P L E S.

1. What is *Easter-Day* for 1764?

The Dominical Letter is G - - = 7

To which add - - - - - 4

The Sum is - - - - - 11

Which subtract from Easter Limit - 48

The Remainder is - - - - - 37

Which subtract from nearest 7's - 42

The Remainder is - - - - - 5

To which add Easter Limit - - 48

The Sum is - - - - - 53

From which take the Days in March 31

Remainder is the - - - - - 22d Day of Apr.

2. What is *Easter-Day* for 1765?

The Dominical Letter is F - - = 6

Add - - - - - 4

The Sum is - - - - - 10

Which subtract from Easter Limit - 37

The Remainder is - - - - - 27

Which subtract from nearest 7's = 28

The Remainder is - - - - - 1

To which add Easter Limit - 37

The Sum is - - - - - 38

From which take the Days in March 31

Remainder is the - - - - - 7th Day of Apr.

Another TABLE to find EASTER-DAY till the Year 1899 inclusive.

SUNDAY LETTERS.							
G. N.	A	B	C	D	E	F	G
I	Apr. 16	17	18	19	20	14	15
II	Apr. 9	3	4	5	6	7	8
III	Mar. 26	27	28	29	23	24	25
IV	Apr. 16	17	11	12	13	14	15
V	Apr. 2	3	4	5	6	Mar. 31	Apr. 1
VI	Apr. 23	24	25	19	20	21	22
VII	Apr. 9	10	11	12	13	14	8
VIII	Apr. 2	3	Mar. 28	29	30	31	Apr. 1
IX	Apr. 16	17	18	19	20	21	22
X	Apr. 9	10	11	5	6	7	8
XI	Mar. 26	27	28	29	30	31	25
XII	Apr. 16	17	18	19	13	14	15
XIII	Apr. 2	3	4	5	6	7	8
XIV	Mar. 26	27	28	22	23	24	25
XV	Apr. 16	10	11	12	13	14	15
XVI	Apr. 2	3	4	5	Mar. 30	31	Apr. 1
XVII	Apr. 23	24	18	19	20	21	22
XVIII	Apr. 9	10	11	12	13	7	8
XIX	Apr. 2	Mar. 27	28	29	30	31	Apr. 1

The Construction of the foregoing Table.

It has been found by Calculation, that whatever *Golden Number* and *Dominical Letter* happens in any one Year, whenever they occur afterwards, they produce the same Day of the same Month for *Easter-Day* that they did before. Hence it follows, that whenever the *Golden Number* happens to be 1, and the *Dominical Letter* A, *Easter-Day* will then be on the 16th Day of *April*: The same Number and B makes *Easter Day* fall on the 17th Day of *April*: The same Number and C makes *Easter Day* fall on the 18th Day of *April*, &c.

Again, When the *Golden Number* is 2, and the Letter is A, *Easter-Day* will be on *April* 9: The same Number and B, makes it *April* 3, &c. After the same Manner is the whole Table formed.

EXAMPLES at large.

1. What will *Easter-Day* be, when the Golden Number is 1, and the Dominical Letter A?

1	<i>Epaet</i> 0	A = 1
<u>1</u>	<u>6</u>	<u>4</u>
0	6	5
11	50	<i>Easter Lim.</i> 44
<u>30</u> 0 (0	<u>0</u> <i>Epaet</i>	<u>39</u>
		<i>nearest 7's</i> 42
		<u>3</u>
		<i>Easter Lim.</i> 44
		<u>47 Days from March 1</u>
		<u>31</u>
		<i>Answer</i> 16th of April

2. What will *Easter-Day* be, when the Golden Number is 1, and the Dominical Letter B?

The Golden Number	B = 2
being 1, the <i>Epaet</i> and	4
<i>Easter Limit</i> are the	<u>6</u>
same as above.	<i>Easter Limit</i> 44
	<u>38</u>
	<i>nearest 7's</i> 42
	<u>4</u>
	<i>Easter Limit</i> 44
	<u>48 Days from March 1</u>
	<u>31</u>
	17th Day of April.

A TABLE of the MOVEABLE FEASTS, according to the several Days that EASTER can possibly fall upon.

Sundays after E- piphany.	Septuagesima Sunday.		Ash-Wednesday.		Easter Day.	Ascensi- on Day.	Whit- sunday.	Sundays after Trinity.	Advent Sunday.
	Com.Yr.	LeapYr.	Com.Yr.	LeapYr.					
1	Jan. 18	Jan. 19	Feb. 4	Feb. 5	Mar. 22	Apr. 30	May 10	27	Nov. 29
1	19	20	5	6	23	May 1	11	27	30
1 2	20	21	6	7	24	2	12	27	Dec. 1
2	21	22	7	8	25	3	13	27	2
2	22	23	8	9	26	4	14	27	3
2	23	24	9	10	27	5	15	26	Nov. 27
2	24	25	10	11	28	6	16	26	28
2	25	26	11	12	29	7	17	26	29
2	26	27	12	13	30	8	18	26	30
2 3	27	28	13	14	31	9	19	26	Dec. 1
3	28	29	14	15	April 1	10	20	26	2
3	29	30	15	16	2	11	21	26	3
3	30	31	16	17	3	12	22	25	Nov. 27
3	31 Feb.	1	17	18	4	13	23	25	28
3	Feb. 1	2	18	19	5	14	24	25	29
3	2	3	19	20	6	15	25	25	30
3 4	3	4	20	21	7	16	26	25	Dec. 1
4	4	5	21	22	8	17	27	25	2
4	5	6	22	23	9	18	28	25	3
4	6	7	23	24	10	19	29	24	Nov. 27
4	7	8	24	25	11	20	30	24	28
4	8	9	25	26	12	21	31	24	29
4	9	10	26	27	13	22	June 1	24	30
4 5	10	11	27	28	14	23	2	24	Dec. 1
5	11	12	28	29	15	24	3	24	2
5	12	13	Mar. 1		16	25	4	24	3
5	13	14	2		17	26	5	23	Nov. 27
5	14	15	3		18	27	6	23	28
5	15	16	4		19	28	7	23	29
5	16	17	5		20	29	8	23	30
5 6	17	18	6		21	30	9	23	Dec. 1
6	18	19	7		22	31	10	23	2
6	19	20	8		23	June 1	11	23	3
6	20	21	9		24	2	12	22	Nov. 27
6	21	22	10		25	3	13	22	28

Note, This Table appears as if it was copied from that in the late Act for correcting the Commencement of the Year, &c. but it was made by me several Years before that Act took Date.

Let this Table front p. 107.

Its Use.

Find the *Sunday* Letter for the given Year, in the uppermost Line, and the Golden Number in the Column of Golden Numbers; against the said Golden Number in the same Line, and directly under the *Sunday* Letter, you have the Day of the Month on which *Easter* falleth that Year.

Note, *The Name of the Month is set on the Left Hand, or just with the Figure, and followeth not as in other Tables by Descent but Collateral.*

E X A M P L E.

What is *Easter-Day* for 1757?

The Golden Number is 10, and the Dominical Letter is B.

Look among the Golden Numbers for 10, then guide your Finger along the same Line till you come under B, and there is *April 10*, which shews that to be *Easter-Day*.

9. OF ADVENT SUNDAY.

To find *Ad-vent Sunday* for ever.

R U L E.

Find the Dominical Letter for the given Year, and against it stands the Day of the Month, which is *Ad-vent Sunday*.

A	December	3
B	November	27
C		28
D		29
E		30
F	December	1
G		2

E X A M P L E.

What is *Advent Sunday* for the Year 1764?

The Dominical Letter is G, therefore *Advent Sunday* is on *December 2*.

Note, *Advent Sunday never falls before November 27, nor after December 3, and is always the nearest Sunday to the Feast of St. Andrew, whether before or after it.*

The Construction of this Table.

1. Find *Easter-Day* by the foregoing Rules ; which suppose to be *March 22*.

2. *Septuagesima Sunday*, being nine Weeks before *Easter*, reckon nine Weeks backward, in the Calendar, from *Easter-Day* ; and if it be a common Year, *Septuagesima Sunday* will fall on *January 18*, but if it be a Leap Year, then on *January 19*.

3. The *Epiphany* is the 6th Day of *January* ; then reckon backward from *Septuagesima* to the *Epiphany*, and you will find that there can be but one *Sunday* after the *Epiphany*.

4. *Ash-Wednesday* is 46 Days before *Easter-Day* ; then reckon 46 Days backward from *Easter*, and *Ash-Wednesday* will be on *February 4*, in a common Year, but in a Leap Year on *February 5*.

5. *Ascension-Day* is 40 Days after *Easter*, including *Easter-Day* ; then begin at *Easter-Day*, and reckon forward 40 Days, and *Ascension-Day* will be on *April 30*.

6. *Whitsunday* is 7 Weeks after *Easter* ; then if you reckon forward from *Easter* 7 Weeks, *Whitsunday* will be *May 10*.

7. *Trinity Sunday* is 8 Weeks after *Easter*, or it is the *Sunday* next after *Whitsunday*.

8. *Advent Sunday* is always known by the Dominical, as before mentioned, which in this Case is *November 29*.

9. The Number of *Sundays* between *Trinity Sunday* and *Advent Sunday*, are the *Sundays* after *Trinity*, which here are 27, the greatest Number that can be. After the same manner is the rest of the Table calculated.

Its Use.

1. Find *Easter-Day* as before taught.

2. Look for *Easter-Day* in the Table, and on the same Line, either before or after it, stands the Holyday sought for.

EXAMPLE.

I demand all the movable Holydays for the Year 1764 ?

1. *Easter-Day* for that Year is *April 22*.

2. Look for *April 22* in the Column of *Easter-Day*, and on the same Line you will find,

6 *Sundays* after *Epiphany* in that Year.

February 19 to be *Septuagesima Sunday*.

March 7 to be *Ash-Wednesday*.

May 31 to be *Ascension-Day*.

June 10 to be *Whitsunday*.

23 *Sundays* after *Trinity* in that Year ; and

December 2 to be *Advent Sunday*.

A TABLE of the GOLDEN NUMBERS, EPACTS, SUNDAY LETTERS,
and MOVEABLE FEASTS, calculated for Fifty Years.

Year of our Lord.	Golden Number.	Epact.	Sunday Letter.	Sundays after E- piphany	Septua- gesima Sunday.	The first Day of Lent.	Easter- Day.	Rogati- on Sun- day.	Ascen- sion-Day.	Whit- Sunday.	Sundays after Trinity.	Ad-vent Sunday.
1752	5											Dec. 3
1753	6	25	G	6	Feb. 18	Mar. 7	Apr. 22	May 27	May 31	June 10	23	2
1754	7	6	F	4	10	Feb. 27	14	19	23	2	24	1
1755	8	17	E	2	Jan. 26	12	Mar. 30	4	8	May 18	26	Nov. 30
1756	9	28	D C	5	Feb. 15	Mar. 3	Apr. 18	23	27	June 6	23	28
1757	10	9	B	4	6	Feb. 23	10	15	19	May 29	24	27
1758	11	20	A	2	Jan. 22	8	Mar. 26	Apr. 30	4	14	27	Dec. 3
1759	12	1	G	5	Feb. 11	28	Apr. 15	May 20	24	June 3	24	2
1760	13	12	F E	3	3	20	6	11	15	May 25	25	Nov. 30
1761	14	23	D	1	Jan. 18	4	Mar. 22	Apr. 26	Apr. 30	10	27	29
1762	15	4	C	4	Feb. 7	24	Apr. 11	May 16	May 20	30	24	28
1763	16	15	B	3	Jan. 30	16	3	8	12	22	25	27
1764	17	26	A G	6	Feb. 19	Mar. 7	22	27	31	June 10	23	Dec. 2
1765	18	7	F	3	3	Feb. 20	7	12	16	May 26	25	1
1766	19	18	E	2	Jan. 26	12	Mar. 30	4	8	18	26	Nov. 30
1767	1	0	D	5	Feb. 15	Mar. 4	Apr. 19	24	28	June 7	23	29
1768	2	11	C B	3	Jan. 31	Feb. 17	3	8	12	May 22	25	27
1769	3	22	A	2	22	8	Mar. 26	Apr. 30	4	14	27	Dec. 3
1770	4	3	G	5	Feb. 11	28	Apr. 15	May 20	24	June 3	24	2
1771	5	14	F	2	Jan. 27	13	Mar. 31	5	9	May 19	26	1
1772	6	25	E D	5	Feb. 16	Mar. 4	Apr. 19	24	28	June 7	23	Nov. 29
1773	7	6	C	4	7	Feb. 24	11	16	20	May 30	24	28
1774	8	17	B	3	Jan. 30	16	3	8	12	22	25	27
1775	9	28	A	5	Feb. 12	Mar. 1	16	21	25	June 4	24	Dec. 3
1776	10	9	G F	4	4	Feb. 21	7	12	16	May 26	25	1
1777	11	20	E	2	Jan. 26	12	Mar. 30	4	8	18	26	Nov. 30
1778	12	1	D	5	Feb. 15	Mar. 4	Apr. 19	24	28	June 7	23	29
1779	13	12	C	3	Jan. 31	Feb. 17	4	9	13	May 23	25	28
1780	14	23	B A	2	23	9	Mar. 26	Apr. 30	4	14	27	Dec. 3
1781	15	4	G	5	Feb. 11	28	Apr. 15	May 20	24	June 3	24	2
1782	16	15	F	2	Jan. 27	13	Mar. 31	5	9	May 19	26	1
1783	17	26	E	5	Feb. 16	Mar. 5	Apr. 20	25	29	June 8	23	Nov. 30
1784	18	7	D C	4	8	Feb. 25	11	26	20	May 30	24	28
1785	19	18	B	2	Jan. 23	9	Mar. 27	1	5	15	26	27
1786	1	0	A	5	Feb. 12	Mar. 1	Apr. 16	21	25	June 4	24	Dec. 3
1787	2	11	G	4	4	Feb. 21	8	13	17	May 27	25	2
1788	3	22	F E	1	Jan. 20	6	Mar. 23	Apr. 27	1	11	27	Nov. 30
1789	4	3	D	4	Feb. 8	25	Apr. 12	May 17	21	31	24	29
1790	5	14	C	3	Jan. 31	17	4	9	13	23	25	28
1791	6	25	B	6	Feb. 20	Mar. 9	24	29	June 2	June 12	22	27
1792	7	6	A G	4	5	Feb. 22	8	13	May 17	May 27	25	Dec. 2
1793	8	17	F	2	Jan. 27	13	Mar. 31	5	9	19	26	1
1794	9	28	E	5	Feb. 16	Mar. 5	Apr. 20	25	29	June 8	23	Nov. 30
1795	10	9	D	3	1	Feb. 18	5	10	14	May 24	25	29
1796	11	20	C B	2	Jan. 24	10	Mar. 27	1	5	15	26	27
1797	12	1	A	5	Feb. 12	Mar. 1	Apr. 16	21	25	June 4	24	Dec. 3
1798	13	12	G	4	4	Feb. 21	8	13	17	May 27	25	2
1799	14	23	F	1	Jan. 20	6	Mar. 24	Apr. 28	2	12	27	1
1800	15	4	E	4	Feb. 9	26	Apr. 13	May 18	22	June 1	24	Nov. 30
1801	16	15	D	3	1	18	5	10	14	May 24	23	29

N. B. 1. The Method of calculating this Table is the same with that of the preceding one, and its Use obvious.

2. The Year 1800 is not a Leap Year, because the Number of Hundreds are not divisible by 4 without a Remainder, and for that Reason has not two Letters annexed to it.

3. The several Omissions or Blanks standing against the Year 1752, denote, that when those respective Days, according to their Titles, happened in that Year, they were reckoned according to Old Stile: And as they were all pass'd before the New Calendar took Date; that is the Reason why they are omitted.

A general TABLE for finding the DOMINICAL or SUNDAY LETTER.

6	5	4	3	2	1	0
B	C	D	E	F	G	A
				1600	1700	1800
1900	2100	2200	2300	2500	2600	2700
2000			2400			2800
2900	3000	3100	3300	3400	3500	3700
		3200			3600	
3800	3900	4100	4200	4300	4500	4600
	4000			4400		
4700	4900	5000	5100	5300	5400	5500
4800			5200			5600
5700	5800	5900	6100	6200	6300	6500
		6000			6400	
6600	6700	6900	7000	7100	7300	7400
	6800			7200		
7500	7700	7800	7900	8100	8200	8300
7600			8000			8400
8500	&c.					

The Use of the foregoing Table.

To find the Dominical or *Sunday* Letter for any given Year of our Lord, add to the Year its fourth Part, omitting Fractions, and also the Number, which standeth at the Top of the Column, wherein the Number of Hundreds contained in that given Year is found: Divide the Sum by 7, and if there is no Remainder, then A is the *Sunday* Letter; but if any Number remaineth, then the Letter, which standeth under that Number, at the Top of the Table, is the *Sunday* Letter. See the *Act of Parliament* for correcting the Calendar.

E X A M P L E

EXAMPLE.

What is the Dominical Letter for the Year 1764?

$$\begin{array}{r} 4)1764 \\ \hline \text{Its fourth Part is} - 441 \\ \text{Add} - - - - - 1 \text{ which stands against the Number of} \\ \hline \text{Hundred, viz. 17 Hundred.} \end{array}$$

$$\begin{array}{r} 7)2206 \\ \hline 315 \text{ 1 remains, which shews the Letter} \\ \hline \text{to be G.} \end{array}$$

General TABLES for finding the Places of the GOLDEN NUMBERS in the CALENDAR.

TABLE I.

1	2	3	1	2	3	1	2	3	1	2	3
	Years of our Lord.			Years of our Lord.			Years of our Lord.			Years of our Lord.	
B	1600	0		3400	8	B	5200	15		7000	24
	1700	1		3500	9		5300	16		7100	24
	1800	1	B	3600	8		5400	17	B	7200	24
	1900	2		3700	9		5500	17		7300	25
B	2000	2		3800	10	B	5600	17		7400	25
	2100	2		3900	10		5700	18		7500	26
	2200	3	B	4000	10		5800	18	B	7600	26
	2300	4		4100	11		5900	19		7700	26
B	2400	3		4200	12	B	6000	19		7800	27
	2500	4		4300	12		6100	19		7900	28
	2600	5	B	4400	12		6200	20	B	8000	27
	2700	5		4500	13		6300	21		8100	28
B	2800	5		4600	13	B	6400	20		8200	29
	2900	6		4700	14		6500	21		8300	29
	3000	6	B	4800	14		6600	22	B	8400	29
	3100	7		4900	14		6700	23		8500	0
B	3200	7		5000	15	B	6800	22		&c.	
	3300	7		5100	16		6900	23			

Note, The Letter B prefixed to certain Hundredth Years, divisible by 4, without any Remainder, denotes those Years, which are still to be accounted Bissextile or Leap Years, in the New Calendar; whereas all the other Hundredth Years are to be accounted only common Years.

TABLE

TABLE II.

		The GOLDEN NUMBERS.																		
Paschal Full Moon.	Sunday Letter.	I	II	III	IV	V	VI	VII	VIII	IX	X	XI	XII	XIII	XIV	XV	XVI	XVII	XVIII	XIX
Mar. 21	C	8	19	0	11	22	3	14	25	6	17	28	9	20	1	12	23	4	15	26
22	D	9	20	1	12	23	4	15	26	7	18	29	10	21	2	13	24	5	16	27
23	E	10	21	2	13	24	5	16	27	8	19	0	11	22	3	14	25	6	17	28
24	F	11	22	3	14	25	6	17	28	9	20	1	12	23	4	15	26	7	18	29
25	G	12	23	4	15	26	7	18	29	10	21	2	13	24	5	16	27	8	19	0
26	A	13	24	5	16	27	8	19	0	11	22	3	14	25	6	17	28	9	20	1
27	B	14	25	6	17	28	9	20	1	12	23	4	15	26	7	18	29	10	21	2
28	C	15	26	7	18	29	10	21	2	13	24	5	16	27	8	19	0	11	22	3
29	D	16	27	8	19	0	11	22	3	14	25	6	17	28	9	20	1	12	23	4
30	E	17	28	9	20	1	12	23	4	15	26	7	18	29	10	21	2	13	24	5
31	F	18	29	10	21	2	13	24	5	16	27	8	19	0	11	22	3	14	25	6
April 1	G	19	0	11	22	3	14	25	6	17	28	9	20	1	12	23	4	15	26	7
2	A	20	1	12	23	4	15	26	7	18	29	10	21	2	13	24	5	16	27	8
3	B	21	2	13	24	5	16	27	8	19	0	11	22	3	14	25	6	17	28	9
4	C	22	3	14	25	6	17	28	9	20	1	12	23	4	15	26	7	18	29	10
5	D	23	4	15	26	7	18	29	10	21	2	13	24	5	16	27	8	19	0	11
6	E	24	5	16	27	8	19	0	11	22	3	14	25	6	17	28	9	20	1	12
7	F	25	6	17	28	9	20	1	12	23	4	15	26	7	18	29	10	21	2	13
8	G	26	7	18	29	10	21	2	13	24	5	16	27	8	19	0	11	22	3	14
9	A	27	8	19	0	11	22	3	14	25	6	17	28	9	20	1	12	23	4	15
10	B	28	9	20	1	12	23	4	15	26	7	18	29	10	21	2	13	24	5	16
11	C	29	10	21	2	13	24	5	16	27	8	19	0	11	22	3	14	25	6	17
12	D	0	11	22	3	14	25	6	17	28	9	20	1	12	23	4	15	26	7	18
13	E	1	12	23	4	15	26	7	18	29	10	21	2	13	24	5	16	27	8	19
14	F	2	13	24	5	16	27	8	19	0	11	22	3	14	25	6	17	28	9	20
15	G	3	14	25	6	17	28	9	20	1	12	23	4	15	26	7	18	29	10	21
16	A	4	15	26	7	18	29	10	21	2	13	24	5	16	27	8	19	0	11	22
17	B	5	16	27	8	19	0	11	22	3	14	25	6	17	28	9	20	1	12	23
17	B	5	16	27	8	19	0	11	22	3	14	25	6	17	28	9	20	1	12	23
17	B	5	16	27	8	19	0	11	22	3	14	25	6	17	28	9	20	1	12	23
18	C	6	17	28	9	20	1	12	23	4	15	26	7	18	29	10	21	2	13	24
18	C	7	18	29	10	21	2	13	24	5	16	27	8	19	0	11	22	3	14	25

Let this Table front p. 110.

The Use of the foregoing two Tables.

To find the Month and Days of the Month, to which the Golden Numbers ought to be prefixed in the Calendar, in any given Year of our Lord, consisting of entire Hundred Years, and in all the intermediate Years, betwixt that and the next Hundredth Year following, look in the second Column of Table I for the given Year, consisting of entire Hundreds, and note the Number or Cypher which stands against it in the third Column; then in Table II, look for the same Number in the Column under any given Golden Number, which when you have found, guide your Eye Side-ways to the Left Hand, and in the first Column you will find the Month and Day to which that Golden Number ought to be prefixed in the Calendar, during that Period of one Hundred Years.

EXAMPLE.

1. It appears by Table I, that the Year 1700 has the Number 1 standing against it, by which it is to be understood, that all the intermediate Years, between that and the Year 1800, have the same Number 1 belonging to them.
2. Begin with the Golden Number 1. in Table II. and look down that Column for the Number of the Year, *viz.* 1, against which, on the Left Hand, stands *April 13*.
3. Look down the Column, under the Golden Number 2, for the same Number 1, and you will find it against *April 2*.
4. Look down the Column, under the Golden Number 3, for the same Number 1, and you will find it stand against *March 22, &c.* and thus you have another Way of making the Table for the Paschal Full Moons, as in the Table of the Golden Numbers, &c. p. 102 and consequently of placing them against the several Days from *March 22*, to *April 18* inclusive, as in the Table to find *Easter-Day* till the Year 1899, p. 103.

Of the NEW MOON, and the MOON'S AGE.

DEFINITION.

THE New Moon is the Conjunction of the Sun and Moon under the same Degree of the same Sign of the Zodiac: And from that Time to the full her Light increaseth, and she is on the East Side of the Sun, and setteth after him. The Full Moon is the Opposition of the Sun and Moon, which happens

happens when they are in the same Degree of Signs diametrically opposite, and from that Time to the New Moon, her Light decreaseth, and she is on the West Side of the Sun, and sitteth before him.

Note 1, From the Conjunction of the Sun and Moon oftentimes proceeds an Eclipse of the Sun: For the New Moon is nothing else but her Interposition, or coming between the Sun and the Earth, and then her enlightened Part is turned from the Earth towards the Sun; and when all three happen in a right Line, then the Moon hides the Light of the Sun, or Part of its Light from the Earth, and this is an Eclipse of the Sun.



An Eclipse

of the Sun.



2. From the Opposition of the Sun and Moon, oftentimes proceeds an Eclipse of the Moon: For the Full Moon is nothing else but the Interposition of the Earth between the Moon and the Sun, and then the Moon hath all her enlightened Part turned towards the Earth, and when all three happen in a right Line, the Shadow of the Earth falls upon the Moon, and depriveth her either of her whole Light, or else of Part of her Light, and this is called an Eclipse of the Moon.



An Eclipse

of the Moon.

3. When Part only of the Sun or Moon is eclipsed, such an Eclipse is said to be partial; but when the whole of either of them is eclipsed, that Eclipse is called Total.



R U L E.

Janus 0, 2, 1, 2, 3, 4, 5, 6,

8, 8, 10, 10, these to the Epact fix:

The Sum, bate 30, to the Month Day add,

Or take from 30, Age or Change is had.

Explanation. Every Month has one of the foregoing Numbers belonging to it; as,

Jan.

Jan. 0, Feb. 2, Mar. 1, Apr. 2, May 3, June 4,
July 5, Aug. 6, Sept. 8, Oct. 8, Nov. 10, Dec. 10, Therefore

1. To the *Epaet* add the Day of the Month, and the Number of the Month : The Sum, if it exceeds not 30, is her Age, if it be more than 30, subtract 30 from it, and the Remainder is her Age.

2. To the *Epaet* add the Number of the Month, and subtract that Sum from 30, the Remainder is the New Moon : But if that Sum exceed 30, subtract it from 60, and the Remainder is the New Moon. Add 15 to the New Moon, shews the Day of the next Full Moon. Or,

If the New Moon happens on any Day of the Month above the 14th, subtract 15 from it, shews the last Full Moon.

Note, The Numbers of the Months arise from the Moon's Age, on the first Day of each Month, when the Solar and Lunar Years begin together, and are called Monthly Epaets.

EXAMPLES.

1. What is the Moon's Age February 18, 1764?

<i>Epaet</i>	-	-	26	
<i>Number</i>	-	-	2	
<i>Day</i>	-	-	18	
				46
<i>Subtract</i>	-	-	30	
				16 Days old.

Note, When the Age of the Moon exceeds the Day of the Month, it shews that the last New Moon happened in the Month next preceding.

2. On what Day in February 1764, will there be a New Moon?

<i>Epaet</i>	-	-	26	30
<i>Number</i>	-	-	2	28
			28	2d Day of February.

Note, If to the Day of the Month you add what the Moon's Age wants of 30, that Sum will be the next New Moon.

Ex. In

114 MISCELLANEOUS ARITHMETIC.

Ex. In February 18, 1764, the Moon was 16 Days old, when will be the next New Moon?

$$\begin{array}{r}
 30 \\
 16 \text{ Moon's Age.} \\
 \hline
 14 \\
 18 \\
 \hline
 \text{Subtract } 32 \\
 30 \\
 \hline
 2^{\text{d}} \text{ Day of March.}
 \end{array}$$

What Days will the New and Full Moon happen on in April, 1764?

$$\begin{array}{r}
 \text{Exact} - 26 \\
 \text{Number} - 2 \\
 \hline
 28 \\
 \hline
 \end{array}
 \qquad
 \begin{array}{r}
 30 \\
 28 \\
 \hline
 \text{New Moon } 2^{\text{d}} \text{ Day of April.} \\
 15 \\
 \hline
 \text{Full Moon } 17^{\text{th}} \text{ Day of April.}
 \end{array}$$

Note, This Way of finding the New and Full Moons, is not exactly true; but as it seldom differs above Half a Day from the true Conjunction, or Opposition, it is sufficient for common Use.

OF the MOON'S SOUTHING.

DEFINITION.

WHEN the Moon comes to the great Meridian, or Twelve o'Clock Hour Line of any Place, she is then due South, with Respect to that Place: And this is called the *Moon's Southing*.

The Time of the New Moon's *Southing* is Twelve at Noon; and from the New to the Full Moon, the *Southing* is after Noon, that is, some time between Noon and Midnight, but every Day 48 Minutes later than the former.

The Time of the Full Moon's *Southing* is Twelve at Midnight; and from the Full to the New Moon, the *Southing* is in the Morning, that is, some time between Midnight and the Noon next following, but every Day 48 Minutes later, as before.

RULE.

R U L E.

Multiply the Moon's Age by 12, and divide that Product by 15, the Quotient gives Hours: If any thing remains, multiply it by 60, and divide again by 15, the Quotient gives Minutes.

E X A M P L E S.

1. What is the Moon's Southing for *February 8, 1764?*

Moon's Age 6 Days

$$\begin{array}{r}
 12 \\
 \hline
 15 \overline{) 72} (4 \text{ Hrs.} \\
 \underline{60} \\
 12 \\
 \underline{60} \\
 15 \overline{) 720} (48 \text{ Min.} \\
 \underline{60} \\
 \underline{120} \\
 \underline{120} \\
 0
 \end{array}$$

Ans. 4 hrs. 48 min. Afternoon.

2. What is the Moon's Southing for *February 18, 1764?*

Moon's Age 16 Days

$$\begin{array}{r}
 12 \\
 \hline
 15 \overline{) 192} (12 \text{ Hrs.} \\
 \underline{15} \\
 42 \\
 \underline{30} \\
 12 \\
 \underline{60} \\
 15 \overline{) 720} (48 \text{ Min.} \\
 \underline{60} \\
 \underline{120} \\
 \underline{120} \\
 0
 \end{array}$$

Ans. 48 Min. after Midnight.

Note 1, The common Day is from Midnight to Midnight; but the Astronomical Day is from Noon to Noon; and always begins 12 Hours sooner than the common Day.

2. If the Southing is less than 12 Hours, it is the Time of the Southing in the Afternoon of the given common Day, as in the first Example.
3. If the Southing is more than 12 Hours, it is so much after the Noon of the given common Day, from which if 12 be subtracted, the Remainder is the Morning next following, as in the second Example.
4. Because the Moon moves 12° every Day more than the Sun, therefore the Lunar Days, or Moon's Age, are multiplied by 12, to shew the whole Number of Degrees she moves more than the Sun, during her given Age: Then because 15° make an Hour of Time, therefore those Degrees are divided by 15, to shew the Number of Hours: The Remainder, if any, being so many Fifteenths of an Hour, is multiplied by 60, and divided again by 15, to shew the Minutes. All which is thus shortened.

R U L E.

Multiply the Moon's Age by 4, and that Product divide by 5, the Quotient is Hours, and the Remainder, so many times 12 Minutes. Or,

Multiply the Moon's Age by 0.8 because 4 divided by 5, is $= 0.8$ the whole Number is the Product in Hours, and the Decimal so many times 6 Minutes.

E X A M P L E.

What is the Moon's Southing for February 18, 1764?

Moon's Age 16 Days

$$\begin{array}{r}
 4 \\
 \hline
 5 \overline{) 64} (12 \text{ Hrs.} \\
 4 \\
 \hline
 12 \\
 \hline
 48 \text{ Min.} \\
 \hline
 \end{array}$$

Or thus.

Moon's Age 16 Days

$$\begin{array}{r}
 .8 \\
 \hline
 \text{Hrs. } 12.8 \\
 6 \\
 \hline
 \text{Min. } 48 \\
 \hline
 \end{array}$$

A T A B L E

A TABLE shewing the Time of the Moon's coming to the South, any Day of her Age.

Moon's Age.		Moon's Southing.	
Days.		H.	M.
1	16	0	48
2	17	1	46
3	18	2	24
4	19	3	12
5	20	4	0
6	21	4	48
7	22	5	36
8	23	6	24
9	24	7	12
10	25	8	0
11	26	8	48
12	27	9	36
13	28	10	24
14	29	11	12
15	30	12	0

The Construction of this Table.

This is no more than a continual Addition of 48 Minutes of Time (the common Difference between every Day's Southing) to every Southing, which produces the Hours and Minutes.

The Days are set double, or in two Columns, because the same Time answers to both, only with this Difference, that during the Moon's *Increase*, the Time is in the Afternoon; and during the *Decrease*, it is in the Morning.

The Use of the Table.

It was shewed before, that the New Moon souths at Noon, and the Full Moon at Midnight. Now if it be required to know when the Moon souths the first Day after the New

Moon; the Answer is, by the Table 0^h. 48^m. that is, 48 Minutes after 12 at Noon: If the Southing be required on the 16th Day, which is one Day past the Full; the Answer is 48 Minutes past 12 at Midnight, or in the Morning, &c.

To find the Time of High Water at any Port in GREAT BRITAIN.

R U L E.

To the Moon's Southing add the Time of High Water at the given Port on the Full and Change Days, and the Sum is the Time of High Water at that Port.

A TABLE

A TABLE of the Time of High Water on the Full and Change Days, at the several Ports in *England*, and other Places elsewhere.

		H. M.			H. M.
Abbevrak,	France	4 30	Camfer, a	} Dutchld.	1 30
Aberdeen,	Scotland	0 45	Sand,		
Aldborough,	England	9 45	C. Cantin,	Barbary	12 0
I. Alderney,	England	12 0	Carthagena,	Spain	8 11
R. Amazons,	Terra Fir	6 0	Cathness Point, or	} Scot.	9 0
I. Ameyland,	Dutchld.	7 30	Dinnet Head		
Amsterdam,	Dutchld.	3 0	Cherbourg,	France	7 0
St. Andrews,	Scotland	2 15	C. Clear,	Ireland	4 30
I. Anholt,	Denmk.	12 0	Concarneau,	France	3 0
Antwerp,	Flanders	6 0	Conquet,	France	3 0
Archangel,	Russia	6 0	I. Coquet,	England	3 0
Baltimore,	Ireland	4 30	Cork,	Ireland	4 30
C. Barfleur,	France	8 0	C. Corse,	Guinea	3 30
I. de Bas,	France	3 45	Cromer,	England	6 0
Bayonne,	France	3 30	Dartmouth,	England	5 15
Beachy Head,	England	12 0	St. David's Hd.	Wales	6 0
Bell-Isle,	France	1 30	Diep,	France	9 45
I. Bermudas,	Baha. Is.	7 0	Dort,	Dutchld.	8 0
Berwick,	England	1 30	Dover,	England	12 0
Blakeney,	England	6 0	Downs,	England	2 15
C. Blanco,	Negrol.	9 45	Dublin,	Ireland	8 15
Blanchart Race,	France	12 0	Dunbar,	Scotland	4 30
Blavet, or	} France	1 30	Dundee,	Scotland	2 15
Port Louis			Dungarvan,	Ireland	4 30
C. Bodajor,	Negrol.	12 0	Dungeness,	England	9 45
Bordeaux,	France	3 0	Dunkirk,	France	12 0
Boulogne,	France	10 30	Dunnofe,	I. Wight	9 45
Bremen,	Germany	6 0	Edinburgh,	Scotland	4 30
Breesound, a	} Dutchld.	4 30	Edystone,	England	7 30
Sand			R. Elbe's Mouth,	Germ.	12 0
Brest,	France	3 45	Embsen,	Germ.	12 0
Bridlington Bay	England	3 45	R. Eme's Mouth	Germ.	7 30
Bristol,	England	6 45	Enchuyfen,	Dutch.	12 0
Buchaness,	Scotland	3 0	Estaples,	France	11 0
Cadiz,	Spain	4 30	Falmouth,	England	4 30
Caen,	France	9 0	Flamborough	} Engl.	3 0
Calais,	France	4 30	Head		
I. Caldy,	England	5 15	C. Florida.	Florida	7 30
				Flushing	

	H. M.		H. M.
Flushing,	Dutchld. 0 45	Naze,	Norway 11 15
L. Fly,	Dutchld. 7 30	Needles,	England 9 45
N. Foreland,	} England 9 45	Newcastle,	England 5 15
S. Foreland		Nieuport,	Flanders 12 0
Foulness,	England 6 45	Nore,	England 12 0
Foye,	England 5 15	North Cape,	Lapland 3 0
R. Garronne,	France 3 0	Ollone,	France 3 45
Gibraltar,	Spain 12 0	Orfordness,	England 9 45
Granville,	France 7 0	Orkney Isles	} Scotland 3 0
Graveline,	France 12 0	Limits	
Gravesend,	England 1 30	Ostend,	Flanders 12 0
Groin or C.	} Spain 3 0	St. Paul de Leon,	France 4 0
Corunna		Plymouth,	England 6 0
I. Guernsey,	England 0 45	Portland,	England 12 0
Hamburgh,	Germany 6 0	Quebec,	Canada 6 0
Harlem,	Dutchld. 9 0	I. Ree,	France 3 0
Hartlepool,	England 3 0	Robin Hood's	} England 3 0
Harwich,	England 11 15	Bay	
Havre de Grace,	France 9 0	Rochelle,	France 3 45
C. Good Hope,	Caffreria 3 0	Rocheſter,	England 0 45
Hull,	England 6 0	Rotterdam,	Dutchld. 3 0
R. Humber's	} England 4 30	Rouen,	France 3 45
Mouth,		Rye,	England 11 15
St. John de Luz,	France 3 30	Scarborough	} England 3 45
I. Kildain,	France 7 30	Head	
Kinfale,	Ireland 4 30	Scilly Isles,	England 3 45
Land's End,	England 7 30	R. Senegal,	Negrod. 10 30
I. Lambay,	Ireland 8 15	Seven Stones,	England 4 30
Leith,	Scotland 4 30	R. Severn Ent.	England 4 30
Leostoff,	England 9 45	R. Seyne Ent.	France 10 30
Lisbon,	Portugal 2 15	Sheerness,	England 1 0
Lizard,	England 7 30	I. Shetland	} Scotland 3 0
R. Loire,	France 3 0	Limits -	
London,	England 3 0	Shoreham,	England 9 45
I. Lundy,	England 5 15	Southampton	- - - 12 0
Lynn,	England 6 0	Spurn - - -	- - - 5 15
St. Maloes,	France 6 0	Start Point -	- - - 6 45
I. Man, W. End,	England 9 0	Stockton - - -	- - - 5 15
Margate,	England 11 15	R. Tee's Mouth	- - - 3 0
Memiffan,	France 3 30	Tinmouth - - -	- - - 3 0
Milford,	Wales 5 15	Torbay - - -	- - - 5 15
Mounts Bay,	England 4 30	Waterford,	Ireland 4 30
Nantes,	France 3 0	Wells,	England 6 0
		Weymouth	

	H. M.		H. M.
Weymouth, England	- 6 0	Wintertonness	- - - 9 0
Whitby	- - - 3 0	Yarmouth	- - - 9 45
I. Wight E. End	- - 12 0	Youghall, Ireland	4 30
Winchelsea	- - - 0 45		

OBSERVATIONS concerning the Ebbing and Flowing of the Tide, at and near *London*.

1. **B**elow-Bridge the Water ebbs seven Hours, and flows five Hours, *i. e.* it is seven Hours going down, and five Hours going up.

2. Above-Bridge, the Water ebbs eight Hours, and flows four Hours, *i. e.* it is eight Hours going down, and but four Hours going up.

3. When the Water is at the lowest, then it is called low Water.

4. When the Water begins to rise, it is called *young Flood*: And when it is almost at the highest, then it is called *old Flood*.

5. When the Water is quite at the highest, it is called *high Water*.

6. When the Water begins to fall, it is then past high Water, and is called *Ebb Water*.

7. The Falling and Rising of the Water, is the Ebbing and Flowing of the Tide.

EXAMPLE.

1. What Time will it be high Water at *London*, February 18, 1764?

	H. M.
Moon's Southing	0 48 in the Morning
Add - - -	3 0

* High Water at 3 48 in the Morning

* Note, This is too late; and as a Mistake may happen by making the Moon a Day older than she really is; it will also occasion a Mistake in her Southing. The Time of High Water at London-Bridge, on the Full and Change Days, has always been said to be at Three; but whoever will make the Observation, will find that Hour too late also. Hence this Method of finding the Time of High Water is not to be depended on for Exactness.

2. What

2. What Time will it be high Water at *Rocheſter*, February 18, 1764? *Anſw.* 1 h. 33 m. in the Morning.
3. What Time will it be high Water at *Graveſend*, February 18, 1764? *Anſw.* 2 h. 18 m. in the Morning.

To find the HOUR of the NIGHT by the
MOON on a SUN-DIAL.

R U L E.

1. **F**IND the Moon's Southing for the given Day.
2. If the Shadow happens before the Hour of 12, ſubtract the Time that it wants of 12, from the Southing: Or,
3. If the Shadow happens after the Hour of 12, add the Time that it makes after 12, to the Southing, and the Difference, or Sum, will be the Hour of the Night required.

E X A M P L E S.

1. I demand the Hour of the Night, when the Shadow falls on the 11th Hour, February 18, 1764?

	H. M.
Moon's Southing	12 48
Subtract	- - 1 0
Answer - - -	11 48 at Night.

2. I demand the Hour of the Night when the Shadow falls $\frac{3}{4}$ after 2 on the abovesaid Night? *Anſw.* 3 h. 33 min. in the Morning.

3. I demand the Hour of the Night, when the Shadow falls on the 12th Hour? *Anſw.* 12 h. 48 m. equal to 100 Southing.

R U L E S to judge of the Weather by the
B A R O M E T E R.

1. **T**HE riſing of the *Mercury* preſages, in general, fair, and its falling, foul Weather.
2. In very hot Weather, the falling of the *Mercury* foreſhews Thunder.
3. In Winter the riſing preſages Froſt: But in a continued Froſt it preſages Snow.

F

4. When

4. When foul Weather happens soon after the falling of the *Mercury*, expect but little of it; and so on the contrary of fair Weather.

5. When the *Mercury* continues to rise for some Time before the foul Weather is over, expect a Continuance of fair Weather to follow.

6. In fair Weather when the *Mercury* continues to fall before Rain comes, you may expect a great deal of Wet; and probably high Winds.

7. The unsettled Motion of the *Mercury* denotes uncertain and changeable Weather.

8. It has been found, by long Experience, that in these Northern Parts of the World, the rising of the *Mercury* forebodes fair Weather after foul, and also after Easterly or Northerly Winds; and that the falling thereof, on the contrary, signifies Southerly or Westerly Winds, or both. And in a Storm, it has been experienced, in high Latitudes, that when the *Mercury* begins to rise, it is a sure Sign that the Storm then begins to abate; and this both to the Northward and Southward of the Equator.



Miscellaneous Arithmetic :

OR A FULL

ACCOUNT of the NEW CALENDAR, &c.

PART IV.

OF LOGARITHMETIC.

 *LOGARITHMS* are artificial Numbers, made to correspond with natural Numbers, in such Manner, that the Addition of the former does exactly answer to the Multiplication of the latter, and the Subtraction of the former to the Division of the latter.

The Indices of all *Logarithms* are the principal *Logarithms* answering to their correspondent prime Numbers; and shew the Distance of the natural Numbers from the Units Place. Thus,

<i>Prime Numbers.</i>	<i>Logarithms.</i>
1 - - - - -	0.0000000
10 - - - - -	1.0000000
100 - - - - -	2.0000000
1000 - - - - -	3.0000000
10000 - - - - -	4.0000000

Hence it appears, that if a natural Number has but one Figure, the Index of its correspondent *Logarithm* is 0: If it has two Figures, the Index is 1; If it has three Figures, the Index is 2; &c. Also,

If 0 is the *Logarithm* of 1, and 1 is the *Logarithm* of 10, then all the *Logarithms* belonging to the natural Numbers between 1 and 10, are Decimals less than 1. Again,

If 1 is the *Logarithm* of 10, and 2 is the *Logarithm* of 100, then all the *Logarithms* belonging to the natural Numbers between 10 and 100, are a 1 with Decimal Parts annexed to it.

124 MISCELLANEOUS ARITHMETIC.

Indices are of two Kinds, *viz.* Affirmative and Negative. The Affirmative are those which are appropriated to whole Numbers; but the Negative to Decimal Fractions and Defective *Logarithms*.

The Affirmative Indices need no Signs; but the Negative have always this Sign - prefixt to them, because they are less than an Unit or 1.

All Numbers, whether Integers or Decimals, expressed by the same Figures, have the same *Logarithm*, except the Index, which is variable in Proportion to the Distance of the natural Number from Units Place. Thus,

<i>Natural Numbers.</i>	<i>Logarithms.</i>
737 ¹ .	3.8675264
737. ¹	2.8675264
73.7 ¹	1.8675264
7.37 ¹	0.8675264
.737 ¹	-1.8675264
.0737 ¹	-2.8675264
.00737 ¹	-3.8675264
.000737 ¹	-4.8675264

Note, There is a Method of using the Complements of Negative Indices, instead of the true negative Indices, by taking them from 10, and then those Logarithms, with their Indices, will stand thus,

<i>Nat. Numbers.</i>	<i>Logarithms.</i>
.737 ¹	-9.8675264
.0737 ¹	-8.8675264
.00737 ¹	-7.8675264
.000737 ¹	-6.8675264

I shall use them both Ways for the Learners Improvement, as Occasion requires.

ADDITION OF INDICES.

Addition adds like Indices, but compares unlike.

RULE.

When two Indices unlike, are compared, keep the Mark of the greater Number in the Sum.

EXAMPLES.

$$\begin{array}{r}
 \text{Add } \left\{ \begin{array}{cccccccccccc} 3 & -3 & 3 & -3 & -10 & -10 & 10 & 8 & -8 & 9 & 9 & -9 & 9 & -9 \\ 4 & 4 & -4 & -4 & -10 & 10 & -9 & 6 & 6 & 5 & -5 & -5 & 4 & -4 \end{array} \right. \\
 \hline
 7 & 1 & -1 & -7 \\
 \hline
 \end{array}$$

Add

$$\text{Add } \left\{ \begin{array}{cccccccc} & & & & 1 & 3 & 4 & 7 & 4 \\ & & & 1 & 4 & -7 & 4 & 2 & 7 & -3 & -7 & 3 \\ -7 & -7 & 7 & 6 & -6 & -6 & -6 & -6 & -5 & -9 & -6 \\ \hline 2 & -2 & 2 & -2 & -9 & 9 & -9 & 6 & 7 & 4 & 9 & -3 \end{array} \right.$$

SUBDUCTION OF INDICES.

Subduction compares like, and adds unlike Indices.

RULE.

In Subduction, always change the Nature of the lower Index, and then add them as in Addition.

Note 1, From any given Number to subtract or take away another Number, is to add the Want of it.

2. From any given Number to subtract or take away the Want of another Number, is add that Number to it.

EXAMPLES.

$$\begin{array}{r} \text{From } 3 \ -3 \ 3 \ -3 \ 9 \ -9 \ 9 \ -9 \ 5 \ -5 \ 5 \ -5 \ 8 \ 1 \ 1 \\ \text{Take } 2 \ 2 \ -2 \ -2 \ 5 \ 5 \ -5 \ -5 \ 9 \ 9 \ -9 \ -9 \ -9 \ 3 \ 4 \\ \hline 1 \ -5 \ 5 \ -1 \end{array}$$

$$\begin{array}{r} \text{From } 9 \ 8 \ -8 \ 8 \ 6 \ -6 \ -6 \ 1 \ 6 \ 3 \ -3 \ -5 \ -5 \ 7 \\ \text{Take } -7 \ 6 \ 6 \ -6 \ 8 \ 8 \ -8 \ -5 \ -9 \ 4 \ 9 \ 5 \ -6 \ 6 \\ \hline \end{array}$$

$$\begin{array}{r} \text{From } 5 \ 6 \ 7 \ 2 \ 4 \ -4 \ -4 \ 4 \ 7 \ 6 \ 5 \ -7 \ -6 \ -5 \\ \text{Take } -4 \ -9 \ 2 \ 7 \ -3 \ -3 \ 3 \ 3 \ -4 \ -3 \ -2 \ 4 \ -2 \ 3 \\ \hline \end{array}$$

To find the LOGARITHM of any given Number.

EXAMPLES.

1. What is the Logarithm of 72?

Enter the Table of Logarithms, and against 72 you have the Logarithm 1.8573325

F 3

2. What

2. What is the Logarithm of 84?
3. What is the Logarithm of 176?
4. What is the Logarithm of 4768?

Note, This Number having four Figures, you must look for the three first Figures, viz. 476 among the whole Numbers, as before, and for the last Figure, viz. 8, at the Top of the Page; then guiding your Finger across the Page from 476, till you come to the Column which hath 8 over it, in that Place is the Logarithm required, viz. .6783362; and as your whole Number consists of 4 Places; so the Index must be 3, and then the Logarithm will stand thus, 3.6783362

5. What is the Logarithm of 6746?
6. What is the Logarithm of 4.8?

Note, When the given Number is either a Decimal or a Mixt Number, the Logarithm for that Number is the same as if it were a whole Number, the Index only being variable, according to the Nature of the Number given, as in the Observation on 7371 foregoing, p. 124.

7. What is the Logarithm of .123? ²⁶⁴
8. What is the Logarithm of .4721?
9. What is the Logarithm of 4.121?
10. What is the Logarithm of 47.12?
11. What is the Logarithm of 312.7?

If the Number given exceeds the Limits of the Table of Logarithms, that is, if it consists of 5, 6 or more Places, then the Logarithm must be found by the following general

R U L E.

1. Find the Logarithm of the first four Figures without its Index, as above.
2. Find the next greater Logarithm.
3. Find the Difference between those two Logarithms.
4. Multiply that Difference with the other Figure or Figures of the given Number.
5. Cut off so many Figures of that Product as you multiply by.
6. Add the remaining Figures of that Product to the Logarithm of the first four Figures.
7. To that Sum prefix the proper Index, and you will have the Logarithm required.

E X A M-

EXAMPLES.

12. What is the Logarithm of 39294?

The Logarithm next greater than that of 3929 is .5943926

The Logarithm of 3929 is - - - - - .5942820

The Difference is - - - - - 1106

Multiply by the last Figure - - - - - 4

Cut off the last Figure - - - - - 44214

The Remainder is 442, which is the Part proportional to be added to the Logarithm of 3929, thus

.5942820

442

.5943262

To which prefix the proper Index, and it makes 4.5943262, the true Logarithm.

13. What is the Logarithm of 37271256?

Next greater Logarithm than that of 3727 is .5714759

The Logarithm of 3727 is - - - - - .5713594

Difference - - - - - 1165

Multiply - - - - - 1256

Product - - - - - 14613240

.5713594

146

7.57131740 = the Logarithm of 37271256.

14. What is the Logarithm of 47684.?

15. What is the Logarithm of 3698.7?

16. What is the Logarithm of 1374.21?

17. What is the Logarithm of 9817.694?

To find the NUMBER to a given Logarithm.

EXAMPLES.

1. **W**HAT is the Number of this Logarithm 0.5331363?

Omit the Index, and seek among the Logarithms for the given Logarithm, against which stands 341, and over the given Logarithm, at the Top, is the Number 3, which shews the Number to be 3413. Then, because the Index is 0, it imports the first Figure of that Number to be a whole Number, and the rest Decimals; therefore the true Number is 3.413.

2. What is the Number of this Logarithm 0.5910646?
3. What is the Number of this Logarithm 1.8692317?
4. What is the Number of this Logarithm 2.3560259?
5. What is the Number of this Logarithm 3.5249151?

Note, When you cannot find the exact Logarithm in the Table, and it appears by the Index, that the natural Number belonging to it is a Decimal, or a mixt Number, having but one or two Figures in the whole Number, you may take the nearest Logarithm to the Logarithm given, whether greater or less, and that will be sufficient; because if the natural Number should be increased to 5, 6, or more Places, they are still but Decimals removed farther from the Units Place; as in the following

EXAMPLES.

6. What is the Number of this Logarithm 0.5943218?

Look in the first Page of the Table of Logarithms, and you will find .5910646, which is too little, and .6020600, which is too much; so that you may conclude it should be a Number between 3.9 and 4.0, in this Case turn to the greater Logarithms, and you will find .5942820, which is the nearest Logarithm the Table can exhibit: Then for its correspondent Number, against it stands 392, and over it, at the Top, stands the Figure 9, which shews the natural Number to be 3929: But because the Index of the given Logarithm is 0, it imports the first Figure only to be a whole Number, and the rest Decimals; and then the true Number is 3.929

7. What is the Number of this Logarithm 0.3126712?
8. What is the Number of this Logarithm 0.4867126?
9. What is the Number of this Logarithm 0.5712671?
10. What is the Number of this Logarithm 0.6438127?

But if the given Number, without its Index, cannot be exactly found in the Table, and the Index imports its natural Number to consist of 5, 6 or more Places, that Number must be found by the following

R U L E.

R U L E.

1. Find the next less Logarithm to the Logarithm given, which is the Logarithm of the first four Figures of the Number required.

2. Subtract that Logarithm from the Logarithm given.

3. Annex so many Ciphers to the Remainder, as there are remaining Figures in the whole Number.

4. Divide this Number, with its annexed Cipher or Ciphers, by the Difference between those two Logarithms, which are next greater and next less than the Logarithm given.

5. Annex the Quotient last found to the four Figures first found, and they will make the natural Number required.

E X A M P L E S.

11. What is the natural Number of this Logarithm 4.5943262?

Here the Number sought consists of 5 Places, as appears by the Index 4.

The Logarithm given is - - - - - .5943262

The next Logarithm (which is the Logarithm of the }
first four Figures sought, viz. 3929) is - - } .5942820

The Difference is - - - - - 442

Annex one Cipher, because there is but one Figure to find, and it makes 4420. Again,

The next greater Logarithm than the Logarithm }
given is - - - - - } .5943926

The next less Logarithm than the Logarithm given }
is - - - - - } .5942820

Diff. 1106

Then 1106)4420(4 nearly.

Therefore finding the first four Figures to be 3929, annex the 4 last found, and it makes 39294, the Number required.

Note, The Truth of this will best appear from Tables of large Numbers; as Sherwin's.

12. What is the natural Number of this Logarithm 4.7623471?

13. What is the natural Number of this Logarithm 4.8712381?

14. What is the natural Number of this Logarithm 5.7123476?

To find the LOGARITHM of a VULGAR FRACTION.

RULE.

Subtract the Logarithm of the Denominator from the Logarithm of the Numerator, and the Remainder is the Logarithm of the Fraction desired.

EXAMPLES.

1. What is the Logarithm of $\frac{3}{4}$?

From 3	0.4771213
Take 4	0.6020600
Answer	-1.8750613

By Decimals.

1. 4)3.00(.75

2. The Logarithm of .75 is .8750613 to which if a Negative Index be prefixed, because the Decimal .75 is but one Remove below Unity, it will stand thus -1.8750613

2. What is the Logarithm of $\frac{11}{13}$?

From 11	1.0413927
Take 13	1.1139434
Answer	-1.9274493

By Decimals.

1. 13)11.0000000(.84615384

2. The Logarithm of 8461 is - - - - .9274217
The next greater Logarithm is - - - - .9274730

The Difference is - - - - - 513

3. Multiply the Difference by the four last Figures 5384

The Product is - - - - - 2761992

4. The Logarithm of 8461, as before, is - - .9274217
To which add - - - - - 276

The Sum is the Answer, as before - - - - -1.9274493

Note,

Note 1, Mr. Chambers in his Cyclopædia, printed in 1750, says, To find the Logarithm of a Fraction: Subtract the Logarithm of the Numerator from the Logarithm of the Denominator; and the Reason he assigns for it is this, That a Fraction being the Quotient of the Denominator divided by the Numerator, its Logarithm must be the Difference of the Logarithms of those two, i. e. the two given Numbers. The Example is the Fraction $\frac{7}{3}$, which he thus works,

$$\text{Log. of } 7 = 0.8450980$$

$$\text{Log. of } 3 = 0.4771213$$

$$\text{Log. of } \frac{7}{3} = 0.3679767$$

But this is extremely wrong, for the Logarithm of $\frac{7}{3}$, found as above, is, in Fact, the Logarithm of $2\frac{1}{3} = 2.3333 +$ the Logarithm 0.3679767 . Beside; a Fraction, that is, a Decimal Fraction is not the Quotient of the Denominator divided by the Numerator, but the Quotient of the Numerator divided by the Denominator. Hence if (of $\frac{7}{3}$) 7 is divided by 3, the Quotient will be $2.3333 +$ as above, which is the Decimal of $2\frac{1}{3}$; but the Quotient of 3 divided by 7 is $.42857 +$ which is the true Decimal Fraction.

2. I chose to mention this, because some having Chambers's Dictionary, may insist that the Rule there laid down must be just, because given by so great an Author; but it is certainly a very great Oversight; and the more so, because given in Words at Length; and whoever lent the helping Hand in that (for it is certain Mr. Chambers did not do all) was so hasty in the Performance, that he took the Wrong for the Right, and so, Neck and Heel, it was brought into the Body of that Work, and passed for genuine.

3. What is the Logarithm of $\frac{4}{3}$?
4. What is the Logarithm of $\frac{7}{12}$?
5. What is the Logarithm of $\frac{3\frac{1}{2}}{4\frac{1}{2}}$?
6. What is the Logarithm of $4\frac{7}{8}$?
7. What is the Logarithm of $19\frac{8}{9}$?
8. What is the Logarithm of $17\frac{1}{2}$ of $\frac{2}{3}$?

MULTIPLICATION by LOGARITHMS.

RULE.

Add the Logarithms of the given Numbers together, and their Sum will be the Logarithm of the Product of the given Factors, Regard being had to the true ordering of the Indices.

CASE I.

If the Indices are both affirmative, their Sum, with what arises from the Addition of the Logarithms, will be an affirmative Index.

EXAM-

132 MISCELLANEOUS ARITHMETIC.

EXAMPLES.

	Num.	Logarithms.		Num.	Logarithms.
<i>Factors</i>	$\left\{ \begin{array}{l} 36 \\ 12 \end{array} \right.$	$\begin{array}{l} 1.5563025 \\ 1.0791812 \end{array}$		$\left\{ \begin{array}{l} 3.6 \\ 1.2 \end{array} \right.$	
<i>Product</i>	<u>432</u>	<u>2.6354837</u>		<u>4.32</u>	<u>0.6354837</u>

<i>Factors</i>	$\left\{ \begin{array}{l} 46 \\ 72 \end{array} \right.$			$\left\{ \begin{array}{l} 7.4 \\ 14.1 \end{array} \right.$	
<i>Product</i>	<u>3312</u>	<u>3.5200903</u>		<u>104.34</u>	<u>2.0184508</u>

<i>Factors</i>	$\left\{ \begin{array}{l} 876.1 \\ 19.2 \end{array} \right.$			$\left\{ \begin{array}{l} 14.8 \\ 96.1 \end{array} \right.$	
<i>Prod.</i>	<u>16821.12</u>	<u>4.2258549</u>		<u>1422.28</u>	<u>3.1529851</u>

CASE 2.

If the Indices are both Negative, their Sum (notwithstanding what arises from the Addition of the *Logarithms*, which is always affirmative) will be a negative Index.

EXAMPLES.

	Num.	Logarithms.		Num.	Logarithms.
<i>Factors</i>	$\left\{ \begin{array}{l} .76 \\ .38 \end{array} \right.$	$\begin{array}{l} -1. \\ -1. \end{array}$		$\left\{ \begin{array}{l} .336 \\ .228 \end{array} \right.$	$\begin{array}{l} -1. \\ -1. \end{array}$
<i>Product</i>	<u>.2688</u>	<u>-1.4605972</u>		<u>.076608</u>	<u>-2.8842741</u>

	$\left\{ \begin{array}{l} .0347 \\ .0236 \end{array} \right.$			$\begin{array}{l} .0000034 \\ .0000023 \end{array}$	
	<u>.00081892</u>	<u>-4.9132415</u>		<u>.000000000000782</u>	<u>-12.8932068</u>

<i>Factors</i>	$\left\{ \begin{array}{l} .000047 \\ .000016 \end{array} \right.$		} This is exactly the same with its Complement in all Respects, as hereafter.		
<i>Product</i>	<u>000000000752</u>	<u>-10.8762179</u>			

CASE

C A S E 3.

When the Indices are one Affirmative, and the other Negative, their Sum, with what is carried from the Logarithms, will be either an affirmative or a negative Index, according to the Nature of the greater Figure or Index in the Factors.

E X A M P L E S.

	Num.	Logarithms.	Num.	Logarithms.
<i>Factors</i>	$\left\{ \begin{array}{l} 738 \\ .09 \end{array} \right.$		$\left\{ \begin{array}{l} 34 \\ .0007 \end{array} \right.$	
<i>Product</i>	<u>66.42</u>	<u>1.8222989</u>	<u>.0238</u>	<u>-2.3765769</u>

Note, If nothing should be carried from the Logarithms, and their Indices be even, as in the first Example following; or if 1 being carried from the Logarithms to the affirmative Index, makes them even, as in the second Example, in either Case the Index of their Sum will be 0.

E X A M P L E S.

	Num.	Logarithms.	Num.	Logarithms.
<i>Factors</i>	$\left\{ \begin{array}{l} 36 \\ .23 \end{array} \right.$	$\left\{ \begin{array}{l} 1. \\ -1. \end{array} \right.$	$\left\{ \begin{array}{l} 25 \\ .076 \end{array} \right.$	$\left\{ \begin{array}{l} 1. \\ -2. \end{array} \right.$
<i>Product</i>	<u>8.28</u>	<u>0.9180303</u>	<u>1.900</u>	<u>0.2787536</u>

2. By the Complements of the NEGATIVE INDICES.

C A S E I.

One Index affirmative, and the other negative.

R U L E.

If their Sum be 10, or above 10, then cast off 10, and the Remainder will be an affirmative Index; but if their Sum be less than 10, it will be a negative Index.

E X A M P L E S.

	Num.	Logarithms.	Num.	Logarithms.
<i>Factors</i>	$\left\{ \begin{array}{l} 75.64 \\ .75 \end{array} \right.$	$\left\{ \begin{array}{l} 1.8787515 \\ -9.8750613 \end{array} \right.$	$\left\{ \begin{array}{l} 756.4 \\ .0075 \end{array} \right.$	
<i>Product</i>	<u>56.73</u>	<u>1.7538128</u>	<u>5.673</u>	<u>0.7538128</u>
				Num.

134 MISCELLANEOUS ARITHMETIC.

	Num.	Logarithms.	Num.	Logarithms.
<i>Factors</i>	$\left\{ \begin{array}{l} 76.19 \\ .217 \end{array} \right.$		$\left\{ \begin{array}{l} 14.7 \\ .004 \end{array} \right.$	
<i>Pro.</i>	<u>16.53323</u>	<u>1.2183577</u>	<u>.0588</u>	<u>-8.7693773</u>
<i>Factors</i>	$\left\{ \begin{array}{l} .0044 \\ 71.09 \end{array} \right.$		$\left\{ \begin{array}{l} .00076 \\ 4.91 \end{array} \right.$	
<i>Product</i>	<u>.312796</u>	<u>-9.4952612</u>	<u>.0037316</u>	<u>-7.5718951</u>

CASE 2.

Both Indices Negative.

RULE.

1. If the Sum of the Indices be above 10, reject 10, and the Remainder will be a negative Index.

EXAMPLES.

	Num.	Logarithms.	Num.	Logarithms.
<i>Factors</i>	$\left\{ \begin{array}{l} .347 \\ .236 \end{array} \right.$	$\left\{ \begin{array}{l} -9.5403295 \\ -9.3729120 \end{array} \right.$	$\left\{ \begin{array}{l} .034 \\ .023 \end{array} \right.$	
<i>Product</i>	<u>.081892</u>	<u>-8.9132415</u>	<u>.000782</u>	<u>-6.8932067</u>
<i>Factors</i>	$\left\{ \begin{array}{l} .004 \\ .089 \end{array} \right.$		$\left\{ \begin{array}{l} .007 \\ .009 \end{array} \right.$	
<i>Product</i>	<u>.000356</u>	<u>-6.5514500</u>	<u>.000063</u>	<u>-5.7993405</u>

2. If the Sum of the Indices be just 10, that Sum will be a negative Index.

EXAMPLES.

	Num.	Logarithms.	
<i>Factors</i>	$\left\{ \begin{array}{l} .000047 \\ .000016 \end{array} \right.$	$\left\{ \begin{array}{l} -5.6720979 \\ -5.2041200 \end{array} \right.$	} This is the same as that in Case 2, in the true negative In- dices.
<i>Product</i>	<u>.000000000752</u>	<u>-10.8762179</u>	
<i>Factors</i>	$\left\{ \begin{array}{l} .00027 \\ .000003 \end{array} \right.$		
<i>Product</i>	<u>.00000000081</u>	<u>-10.9084851</u>	

3. If

MISCELLANEOUS ARITHMETIC. 135

3. If the Sum of the Indices be under 10, add 10 to it, and the Sum will be a negative Index.

EXAMPLES.

	Num.	Logarithms.
Factors {	.00000278	-4.4440448
	.00000176	-4.2455127
Product	.00000000000048928	-18.6895575

Factors {	.0000027	
	.0000076	
Product	.000000000002052	-19.3121774

Factors {	.00000084	
	.00000091	
Product	.0000000000007644	-17.8833207

Note 1, These two last Parts never come into common Practice, and but seldom in any other Shape.

2. The above Indices are the Complements of the true Indices taken from 30.

DIVISION by LOGARITHMS.

RULE.

Subtract the *Logarithm* of the Divisor from the *Logarithm* of the Dividend, and the Remainder is the *Logarithm* of the Quotient.

Note 1, When the Dividend is greater than the Divisor, the Index of the Quotient-Logarithm will be affirmative, though the Indices of the Logarithms of the given Numbers should be both negative.

2. When the Dividend is less than the Divisor, the Index of the Quotient-Logarithm will be negative.

1. By Affirmative Indices.

EXAMPLES.

	Num.	Logarithms.	Num.	Logarithms.
Dividend	432		432	
Divisor	12		36	
Quotient	36	1.5563025	12	1.0791812
				Dividend

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	Num.	Logarithms.	Num.	Logarithms.
Dividend	3312		104.34	
Divisor	72		7.4	
Quotient	46	1.6627578	14.1	1.1492191

2. By Negative Indices.

EXAMPLES.

	Num.	Logarithms.	Num.	Logarithms.
Dividend	.2888		.0588	
Divisor	.38		.004	
Quotient	.76	-1.8808136	14.7	1.1673173
Dividend	.076608		.00081892	
Divisor	.228		.0236	
Quotient	.336	-1.5263393	.0347	-2.5403295

3. By the Complements of the Negative Indices.

Note 1, There must be 10 added to the Index of the Logarithm of the Dividend, when Subtraction cannot be made without it.

2. When the Indices are both negative, and the Dividend the greater, then the less from the greater gives an affirmative Index, as in the 2d and 3d Examples.

3. When the Decimal is so small as to make the Index of the correspondent Logarithm above 9, then its Complement must be taken from 20, as in the last three Examples.

EXAMPLES.

	Num.	Logarithms.	Num.	Logarithms.
Dividend	.0037316	-7.	.782	-9.
Divisor	4.91	0.	.023	-8.
Quotient	.00076	-6.8808136	24.	1.5314789
Dividend	.0356	-8.	.000063	-5.
Divisor	.0089	-7.	.009	-7.
Quotient	4.	0.6020600	.007	-7.8450980

Dividend

	Num.	Logarithms.
Dividend	.000000000752	-10.
Divisor	.000016	-5.
Quotient	.000047	-5.6720979

Dividend	.00000000081
Divisor	.000003
Quotient	.00027
	-6.4313638

Dividend	.0000000000048928
Divisor	.00000176
Quotient	.00000278
	-4.4440448

To square a NUMBER by the LOGARITHMS.

RULE.

Multiply the Logarithm of the given Number by 2, the Product will be the Logarithm of the Square required.

1. By Affirmative Indices.

EXAMPLES.

	Num.	Log.		Num.	Log.
Sq. Root	12	1.0791812		3.8	
		2			
Sq.	144	2.1583624		14.44	1.1595672

2. By the true Negative Indices.

Note, If you bear any Tens to the Indices, they are affirmative, and are to be abated from the Product of the negative Indices.

EXAMPLES.

	Num.	Log.		Num.	Log.
Sq. Root	.47			.018	
Sq.	.2209	-1.3441958		.000324	-4.5105450

3. By

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2. By the Complements of the true Negative Indices.

Note, When the Negative Indices, being multiplied by 2, are above 10, then cast off 10, and the Remainder is a negative Index.

EXAMPLES.

	Num.	Log.		Num.	Log.
Sq. Root	.79			.064	
Sq.	.6241	-9.7952542		.004096	-7.6123600

To extract the SQUARE ROOT.

RULE.

Divide the given *Logarithm* by 2, the Quotient is the *Logarithm* of the Square Root required.

1. By Affirmative Indices.

EXAMPLES.

	Num.	2) Log.		Num.	Log.
Square	144	2.1583624		14.44	
Root	12	1.0791812		3.8	0.5797836

2. By the true Negative Indices.

Note 1. When the given *Logarithm* hath a negative Index, which cannot evenly be divided by 2, add to the said Index an Unit or 1, putting down the Quotient for a new Index.

2. The Unit added, as above, must be called 10 to the next Place of the Division.

3. The Unit that is added, is what was abated in finding the Square; therefore in every odd negative Index given with its *Logarithm* as a Square, an affirmative Unit must be imagined to have been taken from the Product of the negative Indices, according to the Rule in Addition of unlike Indices.

EXAMPLES.

	Num.	Log.		Num.	Log.
Square	.2209			.000324	
Root	.47	-1.6720979		.018	-2.2552725

3. By the Complements of the true negative Indices.

Add 10 to the given Index, and then divide as before.

Note, The 10 which is added, is the 10 which was cast away in finding the Square.

EXAMPLES.

	Num.	Log.		Num.	Log.
Square	.6241			.004096	
Root	.79	-9.8976271		.064	-8.8061800

To

To Cube a NUMBER by the LOGARITHMS.

Multiply the Logarithm of the given Cube Root by 3, the Product will be the Logarithm of the Cube required.

1. By Affirmative Indices.

EXAMPLES.

	Num.	Log.		Num.	Log.
C. ✓	9			7	
Cube	729	2.8627275		343	2.5352940

2. By the true Negative Indices.

Note, If you bear any tens to the Indices, they are affirmative, and are to be abated from the Product of the negative Indices.

EXAMPLES.

	Num.	Log.		Num.	Log.
C. ✓	.11			.91	
Cube	.001331	-3.1241781		.753571	-1.8771242

3. By the Complements of the true Negative Indices.

When the Negative Indices, being multiplied by 3, are above 20, then cast off 20, and the Remainder is a Negative Index.

EXAMPLES.

	Num.	Log.		Num.	Log.
C. ✓	.7			.08	
Cube	.343	-9.5352940		.000512	-6.7092700

To extract the CUBE ROOT.

RULE.

Divide the given Logarithm by 3, the Quotient will be the Logarithm of the Cube Root required.

1. By Affirmative Indices.

EXAMPLES.

	Num.	Log.		Num.	Log.
Cube	729			343	
C. ✓	9	0.9542425		7	0.8450980

2. By the true Negative Indices.

Note 1. When the given Logarithm has a negative Index which cannot be evenly divided by 3, add to the Index so many Units, as will make it capable of Division, putting down the Quotient for a new Index.

2. The Units added, as above, must be called so many tens to the next Place of the Division.

3. The Units that are added, are what were abated in finding the Cube: therefore in every odd negative Index given with its Logarithm as a Cube, an affirmative Unit or Units must be imagined to have been taken from the Product of the negative Indices, according to Addition of unlike Indices.

Cube

E X A M P L E S.

	Num.	Log.		Num.	Log.
Cube	.001331			.753571	
C. $\sqrt{}$	.11	-1.0413927		.91	-1.9590414

3. By the Complements of the true Negative Indices.

Note 1. Add 20 to the given Index, and then divide as before.

2. If any thing remains, call it 10 or 20 to the next Figure.

3. The 20 that is added, is the 20 that was cast away in finding the Cube.

E X A M P L E S.

	Num.	Log.		Num.	Log.
Cube	.343			.000512	
C. $\sqrt{}$	.7	-9.8450980		.08	-8.9030900

To find a MEAN PROPORTIONAL.

R U L E.

Add the Logarithms of the given Numbers together, and take their Half Sum for the Logarithm of the Number required.

E X A M P L E S.

1. What is the Mean Proportional between 4 and 9?

4	0.6020600
9	0.9542425
36(6	2)1.5563025
36	
0	0.7781512 = 6

2. What is the Mean Proportional between 3 and 12?

Ans^w. 6 or 0.7781512.

3. What is the Mean Proportional between 9 and 16?

Ans^w. 12 or 1.0791812.

4. What is the Mean Proportional between 7 and 10?

Ans^w. 8.3666+ or 0.9225490.

5. What is the Mean Proportional between 12 and 18?

Ans^w. 14.696+ or 1.1672268.

To find a FOURTH PROPORTIONAL.

1. In Direct Proportion.

R U L E.

Add the Logarithms of the second and third Terms together, and from that Sum subtract the Logarithm of the first Term, the Remainder is the Logarithm of the fourth Term.

E X A M -

EXAMPLES.

1. If 2oz. of Silk cost 2s. 6d. what cost 7lb.?

lb. oz.

7 = 112

2 0.3010300

30 1.4771213
112 2.0492180

3.5263393

1680 3.2253093

Ans. 1680d. = 7l.

Or thus.

2 0.3010300

2.5 0.3979400
112 2.0492180

2.4471580

140 2.1461280

Ans. 140s. = 7l.

2. If 45 Ells of Cloth cost 30l. what cost 84 Ells? Ans. 1.7481880 = 56l.

3. If 1lb. of any Commodity cost 1s. 2d. $\frac{3}{4}$, what cost 1C. wt.? Ans. 3.8200700 = 6608 qrs. = 6l. 17s. 8d.

2. In Inverse Proportion.

Add the Logarithms of the first and second Terms together, and from that Sum subtract the Logarithm of the third Term, the Remainder is the Logarithm of the fourth Term.

EXAMPLES.

1. If 60 Bricklayers can make a Wall in 45 Days, how many Days will 40 Bricklayers require to build the same? Ans. 1.8293038 = 67.5 Days.

2. How much Ground in Length, being 12 Perches broad, will make an Acre? Ans. 1.1249388 = 13.333+ Perches.

3. In Simple Interest.

1. What is the Simple Interest of 220l. for a Year, at 4 per Cent. per Ann.? Ans. 0.9444827 = 8.8l. = 8l. 16s.

2. What is the Simple Interest of 76l. for 2 Years, at 5 per Cent. per Ann.?

l. l. l. l.

100 : 10 : : 76 : 7.6

Ans. 0.8808136 = 7.6l. = 7l. 12s.

3. What is the Amount of 400l. for 12 Years, at 6 per Cent. per Ann. Simple Interest?

l. l. l. l.

100 : 172 : : 400 : 688

Ans. 2.8375884 = 688l.

4. In Compound Interest.

R U L E.

Multiply the Logarithm of the Amount of 1*l.* at the given Rate *per Cent.* with the Time : then to that Product add the Logarithm of the proposed Principal ; and their Sum will be the Logarithm of the Amount required — *Vide Sch. Assistant, p. 156, for the Amounts of 1*l.* at any proposed Rate.*

E X A M P L E S.

What Sum will 450*l.* amount to in 3 Years, at 5 *per Cent.* *per Ann.* Compound Interest ?

1.05	0.0211893	
	3	
	0.0635679	
450	2.6532125	
520.93	2.7167804	= 520 <i>l.</i> 18 <i>s.</i> 7 <i>d.</i> +

2. What Sum will 400*l.* amount to in 4 Years at 6 *per Cent.* *per Ann.* Compound Interest ? *Ans.* 2.7032836 = 504.99 = 504*l.* 19*s.* 9½*d.* +

3. What Sum will 480*l.* amount to in 6 Years at 5 *per Cent.* *per Ann.* Compound Interest ? *Ans.* 2.8083770 = 643.246 = 643*l.* 4*s.* 11*d.* +

4. What Sum will 500*l.* amount to in 4 Years, at 4½ *per Cent.* *per Ann.* Compound Interest ? *Ans.* 2.7712748 = 590.574 = 590*l.* 11*s.* 5*d.* ¾,

5. In Rebate or Discount at Simple Interest.

R U L E.

1. To the *Logarithm* of the Time add the *Logarithm* of the Ratio of the Rate *per Cent.* and note their Sum.

2. To that Sum add the *Logarithm* of the given Sum.

3. Find the Number answering to the Sum of the *Logarithms* of the Time and Ratio, and annex an Unit or 1 to it.

4. Find the *Logarithm* of this last Number, and subtract it from the Sum last found ; which Difference is the *Logarithm* of the Rebate.

5. Subtract the Rebate from the given Sum, the Remainder is the present Worth.

E X A M -

EXAMPLES.

1. What is the present Worth of 795*l.* 11*s.* 2*d.* for 11 Months at 6 per Cent.?

			<i>Logarithms.</i>
1	795 11 2 = 795.55833	=	2.90067 9
2	11 Months = .91666	=	-1.9622083
3	6 per Cent. = .06	=	-2.7781513

			<i>Logarithms.</i>
4			-1.9622083
			-2.7781513
			-2.7403596 = .054999
			2.9006719
			1.6410315
	1.054999 =		0.0232520
			1.6177795 = 41.474

5 795.55833
41.474

Answ. 754.08433 = 754 *l.* 1 *s.* 8 *d.*

2. What is the present Worth of 161*l.* 10*s.* for 19 Months at 5 per Cent. ? *Answ.* 149.653 = 149*l.* 13*s.* 0*d.* $\frac{3}{4}$ +

3. If a Legacy of 1000*l.* is left me the 24th July, 1764, to be paid on Christmas-Day following; what must I receive when I allow 6 per Cent. for present Payment? *Answ.* 975.154 = 975*l.* 3*s.* 0*d.* $\frac{3}{4}$ +

4. What is the present Worth of 4000*l.* payable in 9 Months, at $4\frac{3}{4}$ per Cent. ? *Answ.* 3862.085 = 3862*l.* 1*s.* 9*d.* $\frac{1}{2}$

6. In Equation of Payments at Simple Interest.

R U L E.

1. Find the *Rebate* for each Sum, and the Time of its Payment, as in the last Rule.

2. Add those *Rebates* together, and find the *Logarithm* of that Sum.

3. Add the *Logarithms* of the present Worth and Ratio together.

4. Subtract

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4. Subtract that Sum from the *Logarithm* of the Sum of all the *Rebates*.

5. The correspondent Number of this Difference is the equated Time required.

EXAMPLES.

1. *A* owes *B* 200*l.* to be paid as follows, *viz.* 100*l.* at 2 Months, and 100*l.* at 4 Months; but they agree to make but one Payment of the Whole, Rebate being made at 6 per Cent. I demand the true equated Time?

1	First Rebate	0.99234	} found as in the last Rule
	Second Rebate	1.96074	
	Sum	2.95308	= 0.4702751
2	Present Worth	197.04692	= 2.2945696
3	Ratio	.06	= -2.7781519
			} add
4	From the first Logarithm subtract	1.0727215	Sum
			-1.3975536 = .24978
5		.24978	
		12	
		2.99736	
		30	
		29.92080	
		24	
		3 68320	
		18 4160	
		22.09920	
		60	
		5.95200	

Answ. 2*m.* 29*d.* 22*hrs.* 5*min.* which in this Case may very well be called 3 Months.

2. A Merchant hath owing to him 300*l.* to be paid as follows, *viz.* 50*l.* at 2 Months, 100*l.* at 5 Months, and the rest at 8 Months; but it is agreed to have but one Payment of the Whole, Rebate being made at 5 per Cent. I demand the equated Time? *Answ.* 5*m.* 29*d.* 9*hrs.* 18*m.* or 6 Months nearly.

3. *F* owes to *H* 1000 *l.* whereof 200 *l.* is to be paid present; 400 *l.* at 5 Months; and the rest at 10 Months; but they agree to have but one Payment of the Whole, at the Rate of 4 *per Cent.* Rebate; I demand the true equated Time?
Ans. 181 Days — or 6 Months, 1 Day.

4. A Man owes to a Merchant 1200 *l.* to be paid as follows, *viz.* 200 *l.* down; 500 *l.* at the End of 10 Months; and the rest at the End of 20 Months; and they agree to have but one Payment of the Whole, Rebate at 3 *per Cent.* I demand the true equated Time? *Ans.* 1 Year, 11 Days.

Note, Rebate and Equation of Payments at Compound Interest, not being practical, are omitted as useless.

To find the ARTIFICIAL SINE, TANGENT, or SECANT to any Number of DEGREES and MINUTES.

R U L E.

If the Degrees only, or Degrees and Minutes given, be less than 45 Degrees, look for the given Degrees at the Top of the Page, and reckon the Minutes downward: If they are more than 45 Degrees, look for the given Degrees at the Bottom, and reckon the Minutes upwards.

E X A M P L E S.

1. What is the Sine, Tangent and Secant of $13^{\circ} 30'$?

Ans. Sine — 9.3681853
 Tangent 9.3803537
 Secant — 10.0121685

2. What is the Sine, Tangent and Secant of $49^{\circ} 17'$?

Ans. Sine — 9.8796375
 Tangent 10.0651775
 Secant — 10.1855400

Note, The Complement of any Degree and Minute is the Remainder of the same from 90 Degrees: And the Complement of the Sine, Tangent, or Secant of any given Degree, is the Sine, Tangent or Secant of that Remainder.

E X A M P L E S.

3. What are the Complements of the Sine, Tangent, and Secant of $13^{\circ} 30'$?

Ans. Sine-complement — 9.9878315
 Tangent-complement 10.6196463
 Secant-complement — 10.6318147

G

4. What

4. What are the Complements of the Sine, Tangent, and Secant of $49^{\circ} 17'$?

Ans. Sine-complement - 9.8144600

Tangent-complement 9.9348225

Secant-complement - 10.1203625

Note, *They are also called Co-sine, Co-tangent, and Co-secant.*

To find the ARITHMETICAL COMPLEMENT of any LOGARITHM.

1. For the Logarithm of any Number.

RULE.

Subtract the given Logarithm from 10, the Remainder is the Arithmetical Complement.

EXAMPLES.

1. What is the Arithmetical Complement of the Logarithm of 417?

$$\begin{array}{r} 10.0000000 \\ 417 = 2.6201361 \\ \hline \end{array}$$

Ans. Ar. Com. 7.3798639

2. What is the Arithmetical Complement of the Logarithm of 978? *Ans.* 7.0096611.

2. For the Logarithm of any Sine, Tangent, or Secant.

If the Characteristic of the given Logarithm, with what was borrowed in Subtraction, should make 10, or more than 10, that Sum must be taken from 20.

EXAMPLES.

1. What is the Arithmetical Complement of the Sine of $16^{\circ} 10'$?

$$\begin{array}{r} 20.0000000 \\ \text{Sine } 9.4447197 \\ \hline \end{array}$$

Ar. Comp. 10.5552803 = the Secant of $73^{\circ} 50'$.

2. What is the Arithmetical Complement of the Sine of $26^{\circ} 19'$? *Ans.* 10.3532710 = the Secant of $63^{\circ} 41'$.

3. What

3. What is the Arithmetical Complement of the Tangent of $63^{\circ}. 12'.$?

$$\begin{array}{r} 20.0000000 \\ \text{Tangent} \quad 10.2965914 \\ \hline \end{array}$$

Ar. Comp. $9.7034086 = \text{the Tangent of } 26^{\circ}. 48'.$

4. What is the Arithmetical Complement of the Tangent of $54^{\circ}. 27'.$ *Answ.* $9.8540694 = \text{the Tangent of } 35^{\circ}. 33'.$

5. What is the Arithmetical Complement of the Secant of $73^{\circ}. 50'.$?

$$\begin{array}{r} 20.0000000 \\ \text{Secant} \quad 10.5552803 \\ \hline \end{array}$$

Ar. Comp. $9.4447197 = \text{the Sine of } 16^{\circ}. 10'.$

6. What is the Arithmetical Complement of the Secant of $63^{\circ}. 41'.$? *Answ.* $9.6467290 = \text{the Sine of } 26^{\circ}. 19'.$

Note 1, *The Complement Arithmetical of the Sine of any given Number of Degrees, is the Secant of the Complement of those Degrees.*

2. *The Complement Arithmetical of the Secant of any given Number of Degrees, is the Sine of the Complement of those Degrees.*

3. *The Complement Arithmetical of the Tangent of any given Number of Degrees is the Co-tangent of those Degrees.*

To find the DEGREES answering to any ARTIFICIAL SINE, TANGENT, OR SECANT.

EXAMPLES.

1. What are the Degrees and Minutes answering to the Sine of 9.3681853 ?

Look in the Table of Sines for the given Logarithm, and against it stands $13^{\circ}. 30'.$

Note, *If the given Logarithm is found in the Column whose Title is at the Top, the Degrees that belong to it, are at the Top also, and the Minutes are reckoned downward; but if the Title is at the Bottom, the Degrees that belong to it are also at the Bottom, and the Minutes are reckoned upward.*

2. What are the Degrees and Minutes answering to the Sine 9.9836643 ?

3. What are the Degrees answering to the Sine 9.9469372 ?

To find the SECONDS, when the LOGARITHM cannot be found in the TABLE exactly.

R U L E.

1. Subtract the next lesser Sine from that which is greater than the Sine given.
2. Subtract the next lesser Sine from the Sine given.
3. As the greater Difference
Is to the lesser Difference;
So is 60
To the Seconds required.

1. For SINES.

E X A M P L E S.

1. What are the Degrees, Minutes and Seconds answering to the Sine of 9.5001639?

$$\begin{array}{r}
 \text{The next greater Sine is } 9.5003421 \\
 \text{--- lesser Sine is } 9.4999633 \\
 \hline
 3788
 \end{array}$$

$$\begin{array}{r}
 \text{The Sine given is } - - 9.500\ 639 \\
 \text{next lesser Sine is } - 9.4999633 \\
 \hline
 2006
 \end{array}$$

$$3788 : 2006 :: 60 : 32 \text{ nearly.}$$

The Sine given answers to $18^{\circ} . 26' . 32''$.

2. What are the Degrees, Minutes and Seconds answering to the Sine 9.7673821? *Ans.* $35^{\circ} . 49' . 28'' . \frac{3750}{1750}$.
3. What are the Degrees, Minutes and Seconds answering to the Sine 6.5763127? *Ans.* $0^{\circ} , 1' . 22'' . \frac{132536}{301030}$.

2 For TANGENTS.

1. What are the Degrees, Minutes and Seconds answering to the Tangent 9.8765492? *Ans.* $35^{\circ} . 57' . 51''$.
2. What are the Degrees, Minutes and Seconds answering to the Tangent 10.7694237? *Ans.* $80^{\circ} . 20' . 57'' . \frac{294}{9638}$.

3. For SECANTS.

1. What are the Degrees, Minutes and Seconds answering to the Secant 10.7685321? *Ans.* $80^{\circ} . 11' . 20''$.
2. What are the Degrees, Minutes and Seconds answering to the Secant 10.4738927? *Ans.* $7^{\circ} . 22' . 39'' . \frac{663}{3343}$.

Note, When the true negative Indices are very large, as -7, -8, -9, or the Complements are very small, as -1, -2, -3, the Decimals are removed so very far from Unity, as that they scarcely ever occur in Practice, and therefore Operations of such Numbers are omitted as useless in this Place especially.

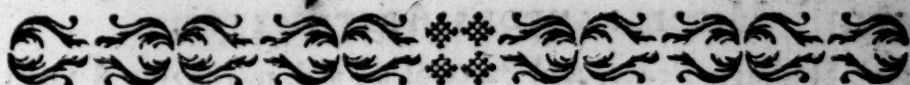
T A B L E S of M O N Y multiplied by M O N Y ;

Shewing the particular Products in P E N C E, F A R T H I N G S,

And P A R T S of a F A R T H I N G.

TABLE 1.				TABLE 2.				TABLE 3.				TABLE 4.								TABLE 5.								TABLE 6.																	
s. X s. 20 = 1s.				s. X d. 20 = 1d.				s. X qrs. 20 = 1q.				d. X d. 60 = 1qr.								d. X qrs. 240 = 1qr.								qrs. X qrs. 960 = $\frac{1}{4}$																	
s.	d.	qr.			ths	d.	qrs. 10		ths	ths	qr.	10	6		ths	ths	qr.	10	6		ths	ths	qr.	10	6		ths	ths	qr.	10	24		ths	ths	qr.	10	96								
20	=	1	0	0		20	=	1	0		20	=	1		60	=	1		40	=	0	6	4	20	=	0	3	2	33	=	0	1	9	13	=	0	0	13	9	=	0	0	9		
19	=	0	11	1	$\frac{6}{10}$	19	=	0	3	8	19	=	0	9	3	59	=	0	9	5	39	=	0	6	3	19	=	0	3	1	32	=	0	1	8	12	=	0	0	12	8	=	0	0	8
18	=	0	10	3	$\frac{2}{10}$	18	=	0	3	6	18	=	0	9		58	=	0	9	4	38	=	0	6	2	18	=	0	3		31	=	0	1	7	11	=	0	0	11	7	=	0	0	7
17	=	0	10	0	$\frac{8}{10}$	17	=	0	3	4	17	=	0	8	3	57	=	0	9	3	37	=	0	6	1	17	=	0	2	5	30	=	0	1	6	10	=	0	0	10	6	=	0	0	6
16	=	0	9	2	$\frac{4}{10}$	16	=	0	3	2	16	=	0	8		56	=	0	9	2	36	=	0	6		16	=	0	2	4	29	=	0	1	5	9	=	0	0	9	5	=	0	0	5
15	=	0	9	0		15	=	0	3		15	=	0	7	3	55	=	0	9	1	35	=	0	5	5	15	=	0	2	3	28	=	0	1	4	8	=	0	0	8	4	=	0	0	4
14	=	0	8	1	$\frac{6}{10}$	14	=	0	2	8	14	=	0	7		54	=	0	9		34	=	0	5	4	14	=	0	2	2	27	=	0	1	3	7	=	0	0	7	3	=	0	0	3
13	=	0	7	3	$\frac{2}{10}$	13	=	0	2	6	13	=	0	6	3	53	=	0	8	5	33	=	0	5	3	13	=	0	2	1	26	=	0	1	2	6	=	0	0	6	2	=	0	0	2
12	=	0	7	0	$\frac{8}{10}$	12	=	0	2	4	12	=	0	6		52	=	0	8	4	32	=	0	5	2	12	=	0	2		25	=	0	1	1	5	=	0	0	5	1	=	0	0	1
11	=	0	6	2	$\frac{4}{10}$	11	=	0	2	2	11	=	0	5	3	51	=	0	8	3	31	=	0	5	1	11	=	0	1	5	24	=	0	1		4	=	0	0	4					
10	=	0	6	0		10	=	0	2		10	=	0	5		50	=	0	8	2	30	=	0	5		10	=	0	1	4	23	=	0	0	23	3	=	0	0	3					
9	=	0	5	1	$\frac{6}{10}$	9	=	0	1	8	9	=	0	4	3	49	=	0	8	1	29	=	0	4	5	9	=	0	1	3	22	=	0	0	22	2	=	0	0	2					
8	=	0	4	3	$\frac{2}{10}$	8	=	0	1	6	8	=	0	4		48	=	0	8		28	=	0	4	4	8	=	0	1	2	21	=	0	0	21	1	=	0	0	1					
7	=	0	4	0	$\frac{8}{10}$	7	=	0	1	4	7	=	0	3	5	47	=	0	7	5	27	=	0	4	3	7	=	0	1	1	20	=	0	0	20										
6	=	0	3	2	$\frac{4}{10}$	6	=	0	1	2	6	=	0	3		46	=	0	7	4	26	=	0	4	2	6	=	0	1		19	=	0	0	19										
5	=	0	3	0		5	=	0	1		5	=	0	2	3	45	=	0	7	3	25	=	0	4	1	5	=	0	0	5	18	=	0	0	18										
4	=	0	2	1	$\frac{6}{10}$	4	=	0	0	8	4	=	0	2		44	=	0	7	2	24	=	0	4		4	=	0	0	4	17	=	0	0	17										
3	=	0	1	3	$\frac{2}{10}$	3	=	0	0	6	3	=	0	1	3	43	=	0	7	1	23	=	0	3	5	3	=	0	0	3	16	=	0	0	16										
2	=	0	1	0	$\frac{8}{10}$	2	=	0	0	4	2	=	0	1		42	=	0	7		22	=	0	3	4	2	=	0	0	2	15	=	0	0	15										
1	=	0	0	2	$\frac{4}{10}$	1	=	0	0	2	1	=	0	0	3	41	=	0	6	5	21	=	0	3	3	1	=	0	0	1	14	=	0	0	14										

Let this Table front p. 149.



Miscellaneous Arithmetic :

OR A FULL
ACCOUNT of the NEW CALENDAR, &c.

PART V.

Of the ARITHMETIC of MONY.

I. MULTIPLICATION of MONY by MONY.

The TABLE.

1. £'s. by £'s. give £'s.
2. — S. — S.
3. — D. — D.
4. — qrs. — qrs.
5. S. by S. $20 = 1 \text{ s.}$ $5 = 3 \text{ d.}$ & $1 = 2 \text{ qrs.}$ $\frac{4}{10}$.
6. — D. $20 = 1 \text{ d.}$ $5 = \frac{1}{4}$ & $1 = \frac{2}{10}$ of $\frac{1}{4}$.
7. — qrs. $20 = \frac{1}{4}$ $2 = \frac{1}{10}$ of $\frac{1}{4}$ & $1 = \frac{1}{2}$ of $\frac{1}{10}$ of $\frac{1}{4}$
 $= \frac{3}{8}$ of $\frac{1}{10}$ of $\frac{1}{4}$.
8. D. by D. $240 = 1 \text{ d.}$ $60 = \frac{1}{4}$ $6 = \frac{1}{10}$ of $\frac{1}{4}$ & $1 = \frac{1}{8}$
of $\frac{1}{10}$ of $\frac{1}{4}$.
9. D. by qrs. $240 = \frac{1}{4}$ $24 = \frac{1}{10}$ of $\frac{1}{4}$ & $1 = \frac{1}{24}$ of $\frac{1}{10}$ of $\frac{1}{4}$.
10. qrs. by qrs. $960 = \frac{1}{4}$ $96 = \frac{1}{10}$ of $\frac{1}{4}$ & $1 = \frac{1}{96}$ of $\frac{1}{10}$
of $\frac{1}{4} = \frac{1}{18}$ of $\frac{1}{8}$ of $\frac{1}{10}$ of $\frac{1}{4}$.

1. Of POUNDS and SHILLINGS multiplied by POUNDS and SHILLINGS.

EXAMPLE 1.

	l.	s.
Multiply	7	4
By	3	8
	21	12
	2	17 7 0 $\frac{4}{5}$
Product	24	9 7 0 $\frac{4}{5}$

1. Here I multiply the 7*l.* 4*s.* first by 3*l.* (which give Pounds and Shillings for the Product) saying 3 times 4 is 12, which set down in the Place of Shillings; and 3 times 7 is 21, which set down in the Place of Pounds.

2. In the next Place I multiply the same 7*l.* 4*s.* by the 8*s.* (which
G 3 give

150 MISCELLANEOUS ARITHMETIC.

give Shillings, Pence, and Parts of a Farthing) saying 8 times 4 is 32, set down 12 (in a By-Place) and carry 1; then 8 times 7 is 56, and 1 that I carried is 57s. or 2*l.* 17s. which set down.

3. To find the Value of the 12 just mentioned, you may do it by Practice, thus

When Shillings are multiplied by Shillings, 20 make 1 Shilling, consequently 10 must be the Half of 20, and 2 the Fifth of 10.

$$\begin{array}{r|l|l|l}
 & & \text{20} = 1 & \\
 \hline
 10 & \frac{1}{2} & 0 & 6 \\
 2 & \frac{1}{5} & 0 & 1 \text{ } 0\frac{4}{5} \\
 \hline
 & & 0 & 7 \text{ } 0\frac{4}{5} \\
 \hline
 \end{array}$$

and this 7*d.* 0*grs.* $\frac{4}{5}$, is the Value of the 12, and to be annexed to the 2*l.* 17s. which makes 2*l.* 17s. 7*d.* 0*grs.* $\frac{4}{5}$; then add them as in Addition of Money, the Total is the Product.

PROOF.

1. By inverting the Factors.

$$\begin{array}{r}
 \begin{array}{r} \text{Multiply} \\ \text{By} \end{array} \begin{array}{r} \text{3} \\ 7 \end{array} \begin{array}{r} \text{8} \\ 4 \end{array} \\
 \hline
 23 \text{ } 16 \\
 13 \text{ } 7 \text{ } 0 \text{ } \frac{8}{16} \\
 \hline
 24 \text{ } 9 \text{ } 7 \text{ } 0 \text{ } \frac{8}{16} \\
 \hline
 \end{array}$$

2. By Practice.

$$\begin{array}{r|l|l|l|l|l}
 & & \text{20} = 1 & & & \\
 \hline
 4 & \frac{1}{2} & 7 & 4 \\
 & & 3 & 8 \\
 \hline
 4 & \frac{1}{2} & 21 & 12 \\
 & & 1 & 8 & 9 & 2 \text{ } \frac{2}{3} \\
 & & 1 & 8 & 9 & 2 \text{ } \frac{2}{3} \\
 \hline
 & & 24 & 9 & 7 & 0 \text{ } \frac{4}{3} \\
 \hline
 \end{array}$$

3. By

3. By Vulgar Fractions.

Multiply $\overset{l.}{7} \overset{s.}{4}$ by $\overset{l.}{3} \overset{s.}{8}$

1.

$$\overset{s.}{4} = \frac{4}{20} = \frac{1}{5} \text{ and } \overset{s.}{8} = \frac{8}{20} = \frac{2}{5}.$$

2.

$$\overset{l.}{7\frac{1}{5}} = \frac{36}{5} \text{ and } \overset{l.}{3\frac{2}{5}} = \frac{17}{5}.$$

3.

$$\frac{36}{5} \times \frac{17}{5} = \frac{612}{25}.$$

4.

$$25)612(24\frac{1}{5}$$

50

112

100

12

20

$$25)240(9\frac{6}{5}$$

225

15

12

$$25)180(7\frac{2}{5}$$

175

5

4

$$25)20(0\frac{4}{5}$$

Note, $\frac{20}{25} = \frac{4}{5}.$

MISCELLANEOUS ARITHMETIC.

4. By Decimals.

l. s. l. s.
 7 4 = 7.2 and 3 8 = 3.4

$$\begin{array}{r}
 7.2 \\
 3.4 \\
 \hline
 288 \\
 216 \\
 \hline
 £24.48 \\
 20 \\
 \hline
 s. 9.60 \\
 12 \\
 \hline
 D. 7.20 \\
 4 \\
 \hline
 0.80 \\
 \hline
 \end{array}$$

Note 1, 0.8 of a Farthing, or $\frac{8}{10}$ is $\frac{4}{5}$.

2. The foregoing Trouble may, in a great Measure, be saved, by using the annexed Tables; however, in the mean Time, it cannot be amiss to understand what has been done, though no other Use be made of it.

EXAMPLE 2.

					l.	s.
					7	16
					12	19
1.	7l. X 12l.	=	- - - -	84	0	
2.	16s. X 12l.	=	192s. =	9	12	
3.	7l. X 19s.	=	133s. =	6	13	
4.	16s. X 19s.	=	304 =	0	15	
	and 4 over.	-		0	0	
					2	1
						$\frac{6}{10}$
	Product			101	0	$\frac{6}{10}$
					2	1
						$\frac{6}{10}$

EXAMPLE 3.

				<i>l.</i>	<i>s.</i>
	<i>Multiply</i>	9	12		
	<i>By</i>	9	12		
1.	9 <i>l.</i> × 9 <i>l.</i> =	-	-	81	0
2.	12 <i>s.</i> × 9 <i>l.</i> =	108 <i>s.</i>	-	5	8
3.	9 <i>l.</i> × 12 <i>s.</i> =	108 <i>s.</i>	-	5	8
4.	12 <i>s.</i> × 12 <i>s.</i> =	144	=		7
	and 4 over =			0	2 1 $\frac{6}{10}$
	<i>Product</i>	92	3	2	1 $\frac{6}{10}$

More Examples for Practice.

<table> <tr><td><i>l.</i></td><td><i>s.</i></td></tr> <tr><td><i>Multiply</i> 4</td><td>9</td></tr> <tr><td><i>By</i> 7</td><td>16</td></tr> <tr><td colspan="2"> </td></tr> <tr><td><i>Prod.</i> 34</td><td>14 3 1 $\frac{6}{10}$</td></tr> </table>	<i>l.</i>	<i>s.</i>	<i>Multiply</i> 4	9	<i>By</i> 7	16			<i>Prod.</i> 34	14 3 1 $\frac{6}{10}$	<table> <tr><td><i>l.</i></td><td><i>s.</i></td></tr> <tr><td>12</td><td>8</td></tr> <tr><td>3</td><td>14</td></tr> <tr><td colspan="2"> </td></tr> <tr><td>45</td><td>17 7 0 $\frac{8}{10}$</td></tr> </table>	<i>l.</i>	<i>s.</i>	12	8	3	14			45	17 7 0 $\frac{8}{10}$	<table> <tr><td><i>l.</i></td><td><i>s.</i></td></tr> <tr><td>7</td><td>12</td></tr> <tr><td>8</td><td>11</td></tr> <tr><td colspan="2"> </td></tr> <tr><td>64</td><td>19 7 0 $\frac{8}{10}$</td></tr> </table>	<i>l.</i>	<i>s.</i>	7	12	8	11			64	19 7 0 $\frac{8}{10}$
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<i>l.</i>	<i>s.</i>																															
<i>Multiply</i> 12	15																															
<i>By</i> 10	14																															
<i>Prod.</i> 136	8 6																															
<i>l.</i>	<i>s.</i>																															
8	16																															
3	12																															
31	11 7 0 $\frac{8}{10}$																															
<i>l.</i>	<i>s.</i>																															
10	14																															
1	16																															
19	5 2 1 $\frac{6}{10}$																															

<table> <tr><td><i>l.</i></td><td><i>s.</i></td></tr> <tr><td><i>Multiply</i> 2</td><td>10</td></tr> <tr><td><i>By</i> 4</td><td>12</td></tr> <tr><td colspan="2"> </td></tr> <tr><td><i>Prod.</i> 11</td><td>10</td></tr> </table>	<i>l.</i>	<i>s.</i>	<i>Multiply</i> 2	10	<i>By</i> 4	12			<i>Prod.</i> 11	10	<table> <tr><td><i>l.</i></td><td><i>s.</i></td></tr> <tr><td>7</td><td>4</td></tr> <tr><td>2</td><td>19</td></tr> <tr><td colspan="2"> </td></tr> <tr><td>21</td><td>4 9 2 $\frac{4}{10}$</td></tr> </table>	<i>l.</i>	<i>s.</i>	7	4	2	19			21	4 9 2 $\frac{4}{10}$	<table> <tr><td><i>l.</i></td><td><i>s.</i></td></tr> <tr><td>3</td><td>19</td></tr> <tr><td>5</td><td>16</td></tr> <tr><td colspan="2"> </td></tr> <tr><td>22</td><td>18 2 1 $\frac{6}{10}$</td></tr> </table>	<i>l.</i>	<i>s.</i>	3	19	5	16			22	18 2 1 $\frac{6}{10}$
<i>l.</i>	<i>s.</i>																															
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<i>l.</i>	<i>s.</i>																															
3	19																															
5	16																															
22	18 2 1 $\frac{6}{10}$																															

Of SHILLINGS and PENCE multiplied by SHILLINGS and PENCE ; a Pound being the Integer.

EXAMPLE I.

			s.	d.
	Multiply	12	4	
	By	6	10	
1.	12s. X 6s. = 72 = 3 twenties =	-	3	0
	and 12 over = $\frac{12}{20}$ of a Shilling =	0	7	0 $\frac{8}{10}$
2.	4d. X 6s. = 24 = 1 twenty =	-	0	1 0
	and 4 over = $\frac{4}{20}$ of a Penny =	-	0	0 0 $\frac{8}{10}$
3.	12s. X 10d. = 120 = 6 twenties =	-	0	6 0
4.	4d. X 10d. = 40 = $\frac{40}{20}$ of a Far. =	0	0	0 $\frac{6}{10}$ $\frac{4}{8}$
Product		£4	2	2 $\frac{2}{10}$ $\frac{4}{8}$

I think the above Explanation of the Operation is full as clear as that which went next before, and contained a larger Quantity of Words: If there be any Difficulty, it must proceed from the want of knowing, when Shillings are multiplied by Shillings, how 20 must make 1 Shilling; and this I will explain in the following Manner.

1. As a Pound is the Integer, and 20s. make 1 Pound, it is to be understood that any Number of Shillings are so many twentieth Parts of a Pound; consequently 1s. must be = $\frac{1}{20}$ of a Pound.

2. If $\frac{1}{20}$ l. be multiplied by $\frac{1}{20}$ l. the Product will be = $\frac{1}{400}$ l.

Thus $\frac{1}{20} \times \frac{1}{20} = \frac{1}{400}$ l.

3. As $\frac{1}{400}$ l. is less than a Penny, a Pound making but 240d. therefore let the Number of Farthings in a Pound, viz. 960, be divided by 400, the Quotient will be 2 qrs. $\frac{2}{5}$.

Thus 4|00)9|60(2

$\frac{160}{400} = \frac{16}{40} = \frac{2}{5}$.

4. If 2 qrs. $\frac{2}{5}$ be multiplied by 20, the Product will be = 48 Farthings, which is just 1 Shilling,

1. Thus $2\frac{2}{5} = \frac{12}{5}$.

2. $\frac{12}{5} \times \frac{20}{1} = \frac{240}{5}$.

3. 5)240(48 qrs. = 1s.

Hence it appears that when Shillings are multiplied by Shillings, 1 Pound being the Integer, 20 must go for 1 Shilling.

The

The same Thing appears also by Decimals, thus;

The Decimal Parts of a *l.* = 1 *s.* make .05.

Then .05	lastly 2.4
.05	20
.0025	grs. 48.9
960	
1500	
225	
grs. 2.4000	

But methinks I hear my Reader say, He understands by the foregoing Explication, how, when Shillings are multiplied by Shillings, that 20 must go for 1 Shilling, but is still at a Loss, when Shillings and Pence are multiplied together, to know how 20 must go for a Penny. Now this may be known by observing what follows, *viz.*

1. Every Pound contains 240 *d.* and therefore any Number of Pence are so many two hundred and fortieth Parts of a Pound, consequently 1 *s.* or 12 *d.* must make $\frac{12}{240}$ of a *l.* and 1 Penny $\frac{1}{240}$ of a Pound.

2. Multiply $\frac{12}{240}$ and $\frac{1}{240}$ together, and they will produce $\frac{12}{57600}$.

Thus, $\frac{12}{240} \times \frac{1}{240} = \frac{12}{57600} = \frac{1}{4800}$.

3. As Farthings are the smallest of our Mony, and 960 *grs.* make a *l.* so that Number should be divided by 4800, but as it cannot, a Fraction must be made of it, thus, $\frac{960}{4800}$ which reduced to its lowest Terms, is $= \frac{1}{5}$ of a Farthing.

4. Multiply $\frac{1}{5}$ by 20, the Product will be four Farthings.

Thus, $\frac{1}{5} \times 20 = \frac{20}{5} = 4$ of a Farthing.

Then, 5)20(4 Farthings = 1 Penny.

The same by Decimals.

4800)960.0(.2 of a Farthing
 960.0
 ———
 0
 —

4. Multiply

2. By Practice.

s.	l.	s.	d.
5	$\frac{1}{4}$	0 12	4
1	$\frac{1}{5}$	0 3	1
6d	$\frac{1}{2}$	0 0	7 $\frac{1}{4}$.6
4	$\frac{1}{3}$	0 0	3 $\frac{1}{2}$.8
		0 0	2 $\frac{1}{4}$.86+
		0 4	2 $\frac{1}{2}$.26

Note 1. There is a small Difference in the Fraction, owing to a Defect in the Decimal.

2. If the Operation had been inverted, and the Parts of 12 s. 4 d. been taken from 6 s. 10 d. it would be the same.

3. By Vulgar Fractions.

1. 12 s. 4 d. = $\frac{148}{240}$.
2. 6 s. 10 d. = $\frac{82}{40}$.
3. $\frac{148}{240} \times \frac{82}{40} = \frac{12136}{9600}$ l.
4. 12136
20

$$576100)2427120(4s.$$

$$\underline{2304}$$

$$12320$$

$$\underline{12}$$

$$576100)1478140(2d.$$

$$\underline{1152}$$

$$32640$$

$$\underline{4}$$

$$576100)1305160(2qrs.$$

$$\underline{1152}$$

$$15360$$

$$\underline{57600}$$

Note, $\frac{15360}{57600} = \frac{16}{60}$; and if $\frac{4}{5}$ of $\frac{1}{10}$ and $\frac{2}{10}$ are added together, they will make $\frac{16}{60}$ also.

4. By

4. By Decimals.

$$\begin{array}{r|l}
 12 & 4. \\
 \hline
 20 & 12.333+ \\
 \hline
 & .616+ = 12s. 4d.
 \end{array}$$

$$\begin{array}{r|l}
 12 & 10. \\
 \hline
 20 & 6.833+ \\
 \hline
 & .341+ = 6s. 10d.
 \end{array}$$

$$.616 \times .342 = .210672 \text{ of a } l.$$

$$\begin{array}{r}
 20 \\
 \hline
 s. 4.21344 \\
 12 \\
 \hline
 d. 2.56128 \\
 4 \\
 \hline
 qrs. 2.24592
 \end{array}$$

Note, The Remainder will not be exact in the Fractional Part, because of the several Defects in the Decimal Divisions above, which is the Reason why .341 is changed into .342.

EXAMPLE 2.

$$\begin{array}{r}
 \text{Multiply} \quad s. \quad d. \\
 \text{By} \quad 7 \quad 10 \\
 \quad \quad 6 \quad 5 \\
 \hline
 \end{array}$$

$$\begin{array}{lcl}
 1. & 7s. \times 6s. = 42 = 2 \text{ twenties} = & - \quad 2 \quad 0 \\
 & \text{and 2 over} = & - \quad - \quad - \quad - \quad - \quad 0 \quad 1 \quad 0 \quad \frac{8}{10} \\
 2. & 10d. \times 6s. = 60 = 3 \text{ twenties} = & - \quad 0 \quad 3 \quad 0 \\
 3. & 7s. \times 5d. = 35 = 1 \text{ twenty} = & - \quad 0 \quad 1 \quad 0 \\
 & \text{and 15 over} = & - \quad - \quad - \quad - \quad - \quad 0 \quad 0 \quad 3 \\
 4. & 10d. \times 5d. = 50 = & - \quad - \quad - \quad - \quad - \quad 0 \quad 0 \quad 0 \quad \frac{8}{10} \quad \frac{2}{8} \\
 & & \hline
 & \text{Product} \quad 2 \quad 6 \quad 0 \quad \frac{6}{10} \quad \frac{3}{8} \\
 & & \hline
 \end{array}$$

E X A M -

EXAMPLE 3.

		s.	d.
Multiply	8	9	
By	5	11	
1.	8 s. X 5 s. = 40 = 2 twenties =	-	2 0
2.	9 d. X 5 s. = 45 = 2 twenties =	-	0 2
	and 5 over =	-	0 0 1
3.	8 s. X 11 d. = 88 = 4 twenties =	-	0 4 0
	and 8 over =	-	0 0 1 $\frac{6}{10}$
4.	9 d. X 11 d. = 99 = 1 sixty =	-	0 0 1
	and 39 over =	-	0 0 0 $\frac{6}{10} \frac{3}{8}$
Product		2	7 0 $\frac{2}{10} \frac{3}{8}$

More Examples for Practice.

	s.	d.
Multiply	16	8
By	7	11
Product	6	7 0 $\frac{6}{10} \frac{4}{8}$

	s.	d.
Multiply	6	4
By	7	4
Product	2	3 3 $\frac{4}{10} \frac{4}{8}$

	s.	d.
Multiply	3	6
By	4	7
Product	0	9 2 $\frac{5}{10}$

	l.	s.	d.
Multiply	3	17	4
By	7	14	2
Product	29	16	1 1 $\frac{3}{10} \frac{2}{8}$

	l.	s.	d.
Multiply	4	10	8
By	7	4	9
Product	32	16	2 1 $\frac{6}{10}$

	s.	d.
Multiply	14	6
By	9	3
Product	6	8 1 $\frac{9}{10}$

	s.	d.
Multiply	12	6
By	3	8
Product	2	3 $\frac{1}{2}$

	s.	d.
Multiply	10	2
By	3	6
Product	1	9 1 $\frac{4}{10}$

	l.	s.	d.
Multiply	4	17	2
By	3	7	5
Product	16	7	6 1 $\frac{5}{10} \frac{4}{8}$

	l.	s.	d.
Multiply	3	12	7
By	2	12	1
Product	9	9	0 0 $\frac{9}{10} \frac{1}{8}$

3. PENCE and FARTHINGs multiplied by PENCE and FARTHINGs.

EXAMPLE I.

	Multiply	d.	
	By	10 $\frac{1}{2}$	9 $\frac{3}{4}$
1. 10d. X 9d. = 90 = 1 sixty = - o I and 30 over = - - - - o O $\frac{3}{8}$			
2. 2 qrs. X 9d. = 18 = - - - - o O O $\frac{18}{24}$ or $\frac{7\frac{1}{2}}{96}$			
3. 10d. X 3 qrs. = 30 = 1 twenty four = o O $\frac{1}{10}$ and 6 over = - - - - o O O $\frac{6}{24}$ or $\frac{\frac{3}{4}}{\frac{96}{96}}$			
4. 2 qrs. X 3 qrs. = 6 = $\frac{6}{96}$ of $\frac{1}{10}$ of $\frac{1}{4}$ = o O O $\frac{6}{96}$			
	Product	o 1 $\frac{7}{10}$	$\frac{6}{96}$

Note, The $\frac{18}{24}$ and $\frac{5}{24}$ are reduced to $\frac{72}{96}$ and $\frac{24}{96}$, to accommodate them to the $\frac{6}{96}$, because the $\frac{6}{96}$ could not be reduced to any Number of twenty-fourths.

Proof.

1. By Practice.

6	$\frac{7}{40}$	$d.$ $10 \frac{1}{2}$
3	$\frac{1}{2}$	$\circ 1.05$
$\frac{3}{4}$	$\frac{1}{4}$	$\circ 0.525$
		$\circ 0.13125$
		$\circ 1.70625$

Here 'tis plain, that 1.7 are the same as $1\frac{7}{10}$ above, and if the $.90625$ are equal to $\frac{6}{80}$, that must be right also.

$$96)6.00000(.00625$$

576

240

192

•480

480

Another

Another Way for the Fractions.

Add $\frac{7}{10}$ and $\frac{6}{98}$ of $\frac{1}{10}$ together.

$$\frac{6}{98} \text{ of } \frac{1}{10} = \frac{6}{980} = \frac{1}{160}$$

and $\frac{7}{10}$ are equal to $\frac{112}{160}$

$$\frac{112}{160} + \frac{1}{160} = \frac{113}{160}$$

$$16 \overline{) 113.0000} (.70625$$

112

100

96

40

32

80

80

0

Hence it is very plain, that 10 d. $\frac{1}{2}$ and 9 d. $\frac{3}{4}$, being multiplied together, will produce no more than 1 Farthing, and $\frac{7}{10}$ and $\frac{6}{98}$ of $\frac{1}{10}$; and also that it is the same with 1.70625.

2. By Vulgar Fractions.

d.

1. $10 \frac{1}{2} = \frac{42}{980} \text{ of a l.}$

2. $9 \frac{3}{4} = \frac{39}{980} \text{ of a l.}$

3. $\frac{42}{980} \times \frac{39}{980} = \frac{1638}{921600} = \frac{91}{51200}$

91

960 = the Farthings in 1 l.

546

819

$$51200 \overline{) 87360} (1 \text{ gr. } \frac{3616}{51200}$$

51200

36160

Here the Farthing appears with a Fraction to it; and if this Fraction $\frac{3616}{51200}$ is equal to $\frac{7}{10}$ and $\frac{6}{98}$ of $\frac{1}{10}$, it must be right this Way also.

In

162 MISCELLANEOUS ARITHMETIC.

In the foregoing Page, it appears that $\frac{7}{10}$ and $\frac{6}{50}$ of $\frac{1}{10}$, being added together, are $= \frac{11}{100}$, and whether this be increased by Multiplication, or the other decreased by Division, it matters not; both amount to the same Thing: therefore

Let $\frac{3616}{3120}$ be reduced to its lowest Parts.

$$8) \frac{3616}{3120} (\frac{452}{840} (\frac{113}{100} \text{ as before.}$$

d. 3. By Decimals.

1. $10 \frac{1}{2} = .043749$
2. $9 \frac{3}{4} = .040625$
3. $.043749 \times .040625 = .00177731$

$$\begin{array}{r}
 4. \quad .00177731 \\
 \quad \quad \quad 20 \\
 \hline
 \quad \quad .03554620 \\
 \quad \quad \quad 12 \\
 \hline
 \quad \quad .4265544 \\
 \quad \quad \quad 4 \\
 \hline
 \quad 1.7062176 \\
 \hline
 \end{array}$$

This is not exactly true, because some Decimal Divisions have no End; and stop where you will, there will be a Deficiency in the Quotient, because there are still some Figures wanting; and if to supply that Want, you make any one of them but one, or a single Unit more than it really should be, which is often done to save Trouble, then there will be a Redundancy. However, this is near enough.

EXAMPLE 2.

$$\begin{array}{r}
 \text{Multiply} \quad d. \quad 11 \frac{3}{4} \\
 \text{By} \quad 11 \frac{3}{4} \\
 \hline
 \end{array}$$

1. $11 d. \times 11 d. = 121 = 2 \text{ sixties} = 0 \ 2$
and 1 over $= - - - - 0 \ 0 \ 0 \ \frac{1}{6} = \frac{16}{96}$
2. $3 qrs. \times 11 d. = 33 = \frac{33}{24} = - 0 \ 0 \ \frac{1}{10} \ 0 \ \frac{9}{24} = \frac{36}{96}$
3. $11 d. \times 3 qrs. = 33 = \frac{33}{24} = - 0 \ 0 \ \frac{1}{10} \ 0 \ \frac{9}{24} = \frac{36}{96}$
4. $3 qrs. \times 3 qrs. = 9 = - - - 0 \ 0 \ 0 \ 0 \ 0 \ \frac{9}{96}$

$$\begin{array}{r}
 \text{Product} \quad 0 \ 2 \ \frac{3}{10} \quad \frac{1}{96} \\
 \hline
 \end{array}$$

EXAM-

EXAMPLE 3.

$$\begin{array}{r} \text{Multiply } 2 \frac{1}{2} \\ \text{By } 3 \frac{1}{4} \end{array}$$

1.	2 d.	X	3 d.	=	6	=	-	-	-	-	00	$\frac{1}{10}$	
2.	2 qrs.	X	3 d.	=	6	=	-	-	-	-	00	$\frac{6}{24} = \frac{1}{4}$	
3.	2 d.	X	1 qr.	=	2	=	-	-	-	-	00	$\frac{2}{24} = \frac{1}{12}$	
4.	2 qrs.	X	1 qr.	=	2	=	-	-	-	-	00	$\frac{2}{96}$	
											Product	$\frac{1}{10}$	$\frac{34}{96}$

More Examples for Practice.

	<i>d.</i>
<i>Multiply</i>	4 $\frac{1}{2}$
<i>By</i>	7 $\frac{1}{4}$
<i>Product</i>	00 $\frac{1}{16}$ $\frac{43}{96}$

d.

8	$\frac{1}{4}$
6	$\frac{3}{4}$
00	$\frac{27}{96}$

$$\begin{array}{r} d. \\ 9 \frac{1}{4} \\ 10 \frac{1}{2} \\ \hline 01 \frac{6}{10} \frac{18}{90} \end{array}$$

	<i>d.</i>	
<i>Multiply</i>	10	$\frac{3}{4}$
<i>By</i>	11	$\frac{1}{2}$
<i>Product</i>	0 2 0	$\frac{5}{9} \frac{8}{6}$

$$\begin{array}{r} 11 \frac{1}{2} \\ 7 \frac{3}{4} \\ \hline 19 \frac{5}{4} \\ \hline 19 \frac{1}{2} \end{array}$$

$$\begin{array}{r} d. \\ 3 \frac{1}{2} \\ 4 \frac{1}{4} \\ \hline 7 \frac{3}{4} \end{array}$$

	<i>l.</i>	<i>s.</i>	<i>d.</i>	
<i>Multiply</i>	12	10	6	$\frac{1}{2}$
<i>By</i>	4	11	8	$\frac{1}{4}$
<i>Product</i>	57	8	6	$3 \frac{6}{10} \frac{90}{98}$

<i>l.</i>	<i>s.</i>	<i>d.</i>	
7	8	6	$\frac{1}{4}$
9	7	8	$\frac{3}{4}$
69	14	10	$\frac{10}{16}$

	<i>l.</i>	<i>s.</i>	<i>d.</i>	
<i>Multiply</i>	24	11	8	$\frac{3}{4}$
<i>By</i>	12	16	7	$\frac{1}{4}$
<i>Product</i>	315	8	11	$3 \frac{4}{10} \frac{7}{96}$

<i>l.</i>	<i>s.</i>	<i>d.</i>	
46	10	8	$\frac{3}{4}$
13	12	8	$\frac{1}{2}$
634	10	10	2 $\frac{2}{10}$ $\frac{38}{96}$

	<i>l.</i>	<i>s.</i>	<i>d.</i>
<i>Multiply</i>	17	16	$9 \frac{1}{4}$
<i>By</i>	12	19	$7 \frac{1}{4}$
<i>Product</i>	231	10 11	$20 \frac{65}{96}$

<i>l.</i>	<i>s.</i>	<i>d.</i>	
10	11	8	$\frac{1}{4}$
12	10	4	$\frac{1}{2}$
132	10	03	$0 \frac{1}{96}$

2. DIVISION of MONY by MONY.

DIVISION of Mony by Mony, bears a very near Relation to Division of Feet, Inches and Seconds by Feet, Inches and Seconds; Regard being had to the Manner of multiplying Mony by Mony, as before.

1. Of dividing POUNDS, SHILLINGS, &c. by POUNDS and SHILLINGS.

EXAMPLE I.

	<i>l.</i>	<i>s.</i>	<i>d.</i>	<i>grs.</i>		<i>l.</i>	<i>s.</i>
Divide	24	9	7	0 $\frac{4}{5}$	by	3	8

<i>l.</i>	<i>s.</i>	<i>l.</i>	<i>s.</i>	<i>d.</i>	<i>gr.</i>	<i>l.</i>	<i>s.</i>
3	8	)	24	9	7	0 $\frac{4}{5}$	(7 4
3	l. 8 s.	×	7	l.	=	23	16
				13	7	0 $\frac{4}{5}$	
3	l. 8 s.	×	4	s.	=	- 13	7 0 $\frac{4}{5}$
0							

The Explanation.

1. Ask how many times 3 *l.* are contained in 24 *l.*
2. The Answer is 8.
3. But because 3 *l.* 8 *s.* multiplied by 8 *l.* would produce more than 24 *l.* therefore
4. Try 7 times, which set down in the Quotient.
5. Multiply the 3 *l.* 8 *s.* by it, and that gives 23 *l.* 16 *s.*
6. Set it down, and subtract it from the upper Line.
7. The Remainder is 13 *s.* 7 *d.* 0 *grs.* $\frac{4}{5}$.
8. Ask how many times 3 *l.* are contained in 13 *s.*
9. The Answer is 4 for 4 *s.*

Note, As Pounds and Shillings multiplied together produce Shillings; so Shillings being divided by Pounds give Shillings likewise.

10. Set down the 4 *s.* in the Quotient, and multiply the 3 *l.* 8 *s.* by it, the Product will give 13 *s.* 7 *d.* 0 *gr.* $\frac{4}{5}$; which makes nothing Remain.

Note, This Example is a Proof to the first Example in Multiplication.

E X A M -

EXAMPLE 2.

Divide $\begin{matrix} l. & s. & d. & qr. \\ 101 & 0 & 2 & 1 \frac{6}{10} \end{matrix}$ by $\begin{matrix} l. & s. \\ 12 & 19 \end{matrix}$

$$\begin{array}{r} \begin{matrix} l. & s. & l. & s. & d. & qr. & l. & s. \\ 12 & 19 & 101 & 0 & 2 & 1 \frac{6}{10} & 7 & 16 \end{matrix} \\ 12l. 19s. \times 7 \quad \begin{matrix} 90 & 13 \\ \hline 10 & 7 & 2 & 1 \frac{6}{10} \\ 10 & 7 & 2 & 1 \frac{6}{10} \\ \hline 0 \end{matrix} \end{array}$$

EXAMPLE 3.

Divide $\begin{matrix} l. & s. & d. & qr. \\ 92 & 3 & 2 & 1 \frac{6}{10} \end{matrix}$ by $\begin{matrix} l. & s. \\ 9 & 12 \end{matrix}$

$$\begin{array}{r} \begin{matrix} l. & s. & l. & s. & d. & qr. & l. & s. \\ 9 & 12 & 92 & 3 & 2 & 1 \frac{6}{10} & 9 & 12 \end{matrix} \\ 9l. 12s. \times 9l. \quad \begin{matrix} 86 & 8 \\ \hline 5 & 15 & 2 & 1 \frac{6}{10} \\ 5 & 15 & 2 & 1 \frac{6}{10} \\ \hline 0 \end{matrix} \end{array}$$

More Examples for Practice.

$$\begin{array}{l} \begin{matrix} l. & s. & l. & s. & d. & qr. \\ 7 & 16 & 34 & 14 & 3 & 1 \frac{6}{10} \end{matrix} (\\ 3 & 14 & 45 & 17 & 7 & 0 \frac{8}{10} (\\ 8 & 11 & 64 & 19 & 7 & 0 \frac{8}{10} (\\ 10 & 14 & 136 & 8 & 6 & (\\ 3 & 12 & 31 & 11 & 7 & 0 \frac{8}{10} (\\ 1 & 16 & 19 & 5 & 2 & 1 \frac{6}{10} (\\ 4 & 12 & 11 & 10 & (\\ 2 & 19 & 21 & 4 & 9 & 2 \frac{4}{10} (\\ 5 & 12 & 22 & 18 & 6 & 1 \frac{6}{10} (\end{array}$$

2. Of dividing SHILLINGS, PENCE, &c. by SHILLINGS and PENCE.

EXAMPLE 1.

$$\begin{array}{r} \text{s. d. grs.} \quad \text{s. d.} \\ \text{Divide } 4 \ 2 \ 2 \ \frac{2}{10} \ \frac{4}{8} \text{ by } 6 \ 10 \end{array}$$

$$\begin{array}{r} \text{s. d. s. d. grs.} \quad \text{s. d.} \\ 6 \ 10 \ 0 \ 2 \ 2 \ \frac{2}{10} \ \frac{4}{8} \ (12 \ 4 \\ 6 \text{ s. } 10 \text{ d. } \times 12 \text{ s.} = 4 \ 1 \ 0 \ \frac{8}{10} \end{array}$$

$$\begin{array}{r} 1 \ 1 \ \frac{4}{10} \ \frac{4}{8} \\ 1 \ 1 \ \frac{4}{10} \ \frac{4}{8} \\ \hline 0 \end{array}$$

$$6 \text{ s. } 10 \text{ d. } \times 4 \text{ d.} =$$

EXAMPLE 2.

$$\begin{array}{r} \text{s. d. gr.} \quad \text{s. d.} \\ \text{Divide } 2 \ 6 \ 0 \ \frac{6}{10} \ \frac{2}{8} \text{ by } 6 \ 5 \end{array}$$

$$\begin{array}{r} \text{s. d. s. d. gr.} \quad \text{s. d.} \\ 6 \ 5 \ 2 \ 6 \ 0 \ \frac{6}{10} \ \frac{2}{8} \ (7 \ 10 \\ 6 \text{ s. } 5 \text{ d. } \times 7 \text{ s.} = 2 \ 2 \ 3 \ \frac{8}{10} \end{array}$$

$$\begin{array}{r} 3 \ 0 \ \frac{8}{10} \ \frac{2}{8} \\ 3 \ 0 \ \frac{8}{10} \ \frac{2}{8} \\ \hline 0 \end{array}$$

$$6 \text{ s. } 5 \text{ d. } \times 10 \text{ d.} =$$

EXAMPLE 3.

$$\begin{array}{r} \text{s. d. gr.} \quad \text{s. d.} \\ \text{Divide } 2 \ 7 \ 0 \ \frac{2}{10} \ \frac{3}{8} \text{ by } 5 \ 11 \end{array}$$

$$\begin{array}{r} \text{s. d. s. d. gr.} \quad \text{s. d.} \\ 5 \ 11 \ 2 \ 7 \ 0 \ \frac{2}{10} \ \frac{3}{8} \ (8 \ 9 \\ 5 \text{ s. } 11 \text{ d. } \times 8 \text{ s.} = 2 \ 4 \ 1 \ \frac{6}{10} \end{array}$$

$$\begin{array}{r} 2 \ 2 \ \frac{6}{10} \ \frac{3}{8} \\ 2 \ 2 \ \frac{6}{10} \ \frac{3}{8} \\ \hline 0 \end{array}$$

$$5 \text{ s. } 11 \text{ d. } \times 9 \text{ d.}$$

More Examples for Practice.

<i>s.</i>	<i>d.</i>	<i>s.</i>	<i>d.</i>	<i>grs.</i>
7	11	6	7	0 $\frac{6}{10}$ $\frac{4}{8}$ (
14	6	6	8	1 $\frac{9}{10}$ (
7	4	2	3	3 $\frac{4}{10}$ $\frac{4}{8}$ (
3	8	2	3	2 (
4	7	0	9	2 $\frac{5}{10}$ (
3	6	1	9	1 $\frac{4}{10}$ (

<i>l.</i>	<i>s.</i>	<i>d.</i>	<i>l.</i>	<i>s.</i>	<i>d.</i>	<i>grs.</i>
7	14	2	29	16	1	1 $\frac{3}{10}$ $\frac{2}{8}$ (
3	7	5	16	7	6	1 $\frac{5}{10}$ $\frac{4}{8}$ (
7	4	9	32	16	2	1 $\frac{6}{10}$ (
2	12	1	9	9	0	0 $\frac{9}{10}$ $\frac{1}{8}$ (

3. Of Dividing PENCE, FARTHING, &c. by PENCE and FARTHING.

EXAMPLE 1.

gr. *d.*

Divide 1 $\frac{7}{10}$ $\frac{6}{96}$ by 9 $\frac{3}{4}$

d. *grs.* *gr.* *d.* *grs.*

$$9 \text{ } 3 \text{) } 1 \text{ } \frac{7}{10} \text{ } \frac{6}{96} \text{ (} 10 \text{ } 2$$

9d. *3grs.* $\times 10 =$ $1 \text{ } \frac{6}{10} \text{ } \frac{24}{96}$

9d. *3grs.* $\times 2grs. =$ $\frac{78}{96}$

0

EXAMPLE 2.

grs. *d.*

Divide 2 $\frac{3}{10}$ $\frac{1}{96}$ by 11 $\frac{3}{4}$

d. *d.* *grs.*

$$11 \text{ } \frac{3}{4} \text{) } 2 \text{ } \frac{3}{10} \text{ } \frac{1}{96} \text{ (} 11 \text{ } 3$$

11d. *3grs.* $\times 11d. =$ $2 \text{ } \frac{1}{10} \text{ } \frac{32}{96}$

11d. *3grs.* $\times 3grs. =$ $\frac{1}{10} \text{ } \frac{45}{96}$

0

EXAMPLE 3.

Divide $0 \frac{1}{10} \frac{34}{96}$ by $3 \frac{1}{4}$

$$\begin{array}{r}
 \begin{array}{r}
 d. \quad gr. \qquad \qquad d. \quad grs. \\
 3 \frac{1}{4}) 0 \frac{1}{10} \frac{34}{96} (2 \quad 2 \\
 \underline{10 \quad 96} \\
 26 \\
 96 \\
 26 \\
 96 \\
 \hline
 0
 \end{array} \\
 3d. 1gr. \times 2 = \qquad \qquad \qquad \\
 3d. 1gr. \times 2 \qquad \qquad \qquad
 \end{array}$$

More Examples for Practice.

d. gr.

$$7 \frac{1}{4}) 0 \frac{5}{10} \frac{42}{96} ($$

$$6 \frac{3}{4}) 0 \frac{9}{10} \frac{27}{96} ($$

$$10 \frac{1}{2}) 1 \frac{6}{10} \frac{18}{96} ($$

$$11 \frac{1}{2}) 2 \quad 0 \frac{58}{96} ($$

$$7 \frac{3}{4}) 1 \frac{4}{10} \frac{82}{96} ($$

$$4 \frac{1}{4}) 0 \frac{2}{10} \frac{46}{96} ($$

l. s. d. l. s. d. grs.

$$4 \ 11 \ 8 \ \frac{1}{4}) 57 \ 8 \ 6 \ 3 \ \frac{6}{10} \ \frac{99}{96} ($$

$$9 \ 7 \ 8 \ \frac{3}{4}) 69 \ 14 \ 1 \ 0 \ 0 \ \frac{39}{96} ($$

$$12 \ 16 \ 7 \ \frac{1}{4}) 315 \ 8 \ 11 \ 3 \ \frac{4}{10} \ \frac{7}{96} ($$

$$13 \ 12 \ 8 \ \frac{1}{2}) 634 \ 10 \ 10 \ 2 \ \frac{2}{10} \ \frac{38}{96} ($$

$$12 \ 19 \ 7 \ \frac{1}{4}) 231 \ 10 \ 11 \ 2 \ 0 \ \frac{65}{96} ($$

$$12 \ 10 \ 4 \ \frac{1}{2}) 132 \ 10 \ 0 \ 3 \ 0 \ \frac{18}{96} ($$

3. Of the SINGLE RULE OF THREE, wrought only by MONEY.

I. Of DIRECT PROPORTION.

1. If I give 7*l.* for the Interest of 100*l.* 10*s.* for a Year, how much must I give for the Interest of 30*l.* for the same Time?

$$\begin{array}{cccc} l. & s. & l. & l. \\ 100 & 10 & : & 7 :: 30 \end{array}$$

$$\begin{array}{r} 7 \text{ l. s. d.} \\ 100 \text{ } 10 \text{) } 210 \text{ (} 2 \text{ } 1 \text{ } 9\frac{1}{4} \end{array}$$

$$\begin{array}{r} 201 \text{ s. d.} \\ 9 \text{ } 0 \text{ } 0 \\ 5 \text{ } 0 \text{ } 6 \\ 3 \text{ } 19 \text{ } 6 \\ 3 \text{ } 15 \text{ } 4\frac{1}{2} \end{array}$$

$$\begin{array}{r} 4 \text{ } 1 \text{ } \frac{1}{2} \\ 2 \text{ } 1 \text{ } 0 \text{ } \frac{5}{10} \\ 2 \text{ } 0 \text{ } \frac{1}{4} \text{ } \frac{5}{10} \end{array}$$

$$\begin{array}{r} l. \text{ s. d. gr.} \quad s. \text{ d. gr.} \\ \text{Answ. } 2 \text{ } 1 \text{ } 9 \text{ } 1 \quad 2 \text{ } 0 \text{ } 1 \text{ } \frac{5}{10} \end{array}$$

The Proof by the common Way.

$$\begin{array}{r} l. \text{ s. l. l.} \\ 100 \text{ } 10 : 7 :: 30 \\ \hline 20 \quad 20 \\ 2010 \quad 600 \end{array}$$

$$\begin{array}{r} 7 \\ 2010 \text{) } 42010 \text{ (} 2 \text{ l.} \end{array}$$

$$\begin{array}{r} 402 \\ 18 \end{array}$$

$$\begin{array}{r} 20 \\ 201 \text{) } 360 \text{ (} 1 \text{ s.} \end{array}$$

$$\begin{array}{r} 201 \\ 159 \\ 12 \end{array}$$

$$\begin{array}{r} 201 \text{) } 1908 \text{ (} 9 \text{ d.} \\ 1809 \end{array}$$

$$\begin{array}{r} 99 \\ 4 \end{array}$$

$$201 \text{) } 396 \text{ (} 1 \text{ gr.}$$

$$\begin{array}{r} 201 \\ 195 \end{array}$$

Answ. 2*l.* 1*s.* 9*a.* 1*qr.* $\frac{195}{201}$

H

2. By

2. By Vulgar Fractions.

$$\begin{array}{r} l. \quad l. \quad l. \\ 100 \frac{1}{2} : 7 :: 30 \end{array}$$

$$\frac{7}{1} \times \frac{30}{1} = \frac{210}{1}$$

$$100 \frac{1}{2} = \frac{201}{2}$$

$$\frac{201}{2}) \frac{210}{1} (\frac{420}{201}$$

$$201) 420 (2 l.$$

$$\underline{402}$$

$$18$$

$$\underline{20}$$

$$201) 360 (1 s.$$

$$\underline{201}$$

159 Gr. as before.

3. By Decimals.

$$\begin{array}{r} l. \quad l. \quad l. \\ 100.5 : 7 :: 30 \end{array}$$

$$\underline{7}$$

$$100.5) 210.0000000 (2.0895522 +$$

$$\underline{2010}$$

$$9000$$

$$\underline{8040}$$

$$9600$$

$$\underline{9040}$$

$$5550$$

$$\underline{5025}$$

$$5250$$

$$\underline{5025}$$

$$2250$$

$$\underline{2010}$$

$$2400$$

$$\underline{2010}$$

$$\underline{390}$$

Again.

$$l. 2.0895522$$

$$\underline{20}$$

$$s. 1.7910440$$

$$\underline{12}$$

$$d. 9.4925280$$

$$\underline{4}$$

$$gr. 1.970112$$

If

MISCELLANEOUS ARITHMETIC. 191

* If the Fraction, viz. $\frac{195}{201}$, at the Bottom of the first Way of proving the Question, be reduced to a Decimal, it will appear to be the same as above nearly, viz.

$$\begin{array}{r} 201 \overline{) 195.0(.9701 \text{ near enough.}} \\ \underline{1809} \\ 1410 \\ \underline{1407} \\ 300 \\ \underline{201} \\ 99 \end{array}$$

But some Readers may yet be at a Loss to account for the Numbers which are placed Fractionwise at the End of the Answer, and therefore not be able to reconcile $\frac{2s. 0d. 1qr. \frac{5}{10}}{100 \ 10 \ 0}$ with the Fraction $\frac{195}{201}$, which is nevertheless the same in Value exactly, as appears by the following short Operation.

1. $2s. 0d. 1qr. \frac{5}{10} = 97.5 \text{ qrs.}$
2. $100l. 10s. = 100.5l.$
3. $\frac{97.5}{100.5}$ being multiplied by one common Multiplier, as 2 will be $= \frac{195}{201}$.

2. A Tradesman in a particular Branch of Business, having in one Week received 121l. 17s. 6d. found, upon Examination, that 48l. 13s. of that Sum was clear Gain; what was the Gain per Cent.?

l.	s.	d.		l.	s.	d.
121	17	6		48	13	0
				73	4	6

l.	s.	d.	l.	s.	d.	l.
73	4	6	48	13	0	100
			l.	s.	d.	100
73	4	6	4865	0	66	8 9 $\frac{1}{4}$
			4393	10		
			471	10		
			439	7	d.	qr.
			32	3	0	0
			29	5	9	2 $\frac{4}{10}$
			2	17	2	1 $\frac{6}{10}$
			2	14	11	0 $\frac{1}{10}$
			2	3	1	$\frac{5}{10}$
			1	6	1	$\frac{2}{10}$
			9	0	2	$\frac{18}{10}$

H 2

d. qr.	9	0	$\frac{2}{10}$	$\frac{18}{10}$	$\frac{18}{10}$	$\frac{18}{10}$
l. s. d. qr.	66	8	9	1	73	4 6
Answ.						

MISCELLANEOUS ARITHMETIC.

1. Proof by common Arithmetic.

<i>l.</i>	<i>s.</i>	<i>d.</i>	<i>l.</i>	<i>s.</i>	<i>l.</i>
73	4	6 : 48	13	:	100
20		20			20
1464		973			2000
12					12
17574					24000
					973
					72
					168
					216
					210
17574	23352000	(13218			
		66	8	9 $\frac{1}{4}$	+
		57780			
		52722			
		50580			
		35148			
		154320			
		140592			
		13728			
		12			
17574	164736	(9			
	158166				
	6570				
	4				
17574	26280	(1			
	17574				
	8706				

<i>l.</i>	<i>s.</i>	<i>d.</i>	<i>qr.</i>
Ans/w. 66	8	9	1
			8706
			17574

2. By

2. By Vulgar Fractions.

$$l. \quad l. \quad l. \\ 73 \frac{9}{40} : 48 \frac{13}{20} :: 100$$

$$48 \frac{13}{20} = \frac{973}{20}$$

$$\frac{973}{20} \times \frac{100}{1} = 97300$$

$$73 \frac{9}{40} = \frac{2929}{40}$$

$$\frac{2929}{40} \div \frac{97300}{20} = \frac{3892000}{58380}$$

$$585810)3892000(66l.$$

$$35148$$

$$37720$$

$$35148$$

$$2572$$

$$20$$

$$5858)51440(8s.$$

$$46864$$

$$4576$$

$$12$$

$$5858)54912(9d.$$

$$52722$$

$$2190$$

$$4$$

$$5858)8760(1qr.$$

$$5858$$

$$2902$$

$$Ans. \quad l. \quad s. \quad d. \quad qr. \\ 66 \quad 8 \quad 9 \quad 1 \frac{2902}{5858}$$

3. By Decimals.

$$\begin{array}{ccc} l. & l. & l. \\ 73.225 & : 48.65 & : : 100 \\ & 100 & \end{array}$$

$$\begin{array}{r} 73.225)4865.000(66.43905769 \\ \underline{439350} \end{array}$$

$$\begin{array}{r} 471500 \\ \underline{439350} \end{array}$$

$$\begin{array}{r} 321500 \\ \underline{292900} \end{array}$$

$$\begin{array}{r} 286000 \\ \underline{219675} \end{array}$$

$$\begin{array}{r} 663250 \\ \underline{659025} \end{array}$$

$$\begin{array}{r} 422500 \\ \underline{366125} \end{array}$$

$$\begin{array}{r} 563750 \\ \underline{512575} \end{array}$$

$$\begin{array}{r} 511750 \\ \underline{439350} \end{array}$$

$$\begin{array}{r} 724000 \\ \underline{659025} \end{array}$$

$$\begin{array}{r} 64975 \end{array}$$

Again.

$$\begin{array}{r} l. 66.43905769 \\ \underline{20} \end{array}$$

$$\begin{array}{r} s. 8.7811538 \\ \underline{12} \end{array}$$

$$\begin{array}{r} d. 9.3738456 \\ \underline{4} \end{array}$$

$$\begin{array}{r} gr. 1.4953824 \\ \underline{} \end{array}$$

$$\begin{array}{cccc} l. & s. & d. & gr. \\ \text{Answ. } 66 & 8 & 9 & 1.4953 \end{array}$$

Note, The Fractions are all equal to each other.

MISCELLANEOUS ARITHMETIC. 175

A Merchant being indebted to *A* 40*l.* 12*s.* 6*d.* to *B* 70*l.* 8*s.* 10*d.* to *C* 84*l.* 19*s.* 4*d.* and to *D* 178*l.* 18*s.* 6*d.* $\frac{1}{2}$, compounds with them for 12*s.* in the Pound; how much must each Person receive?

$$\begin{array}{r}
 \begin{array}{ccc} l. & s. & d. \\ 1 & : 12 & :: 40 \ 12 \ 6 \\ & & 12 \end{array} \\
 \hline
 24 \ 0 \ 0 \\
 \begin{array}{r} 7 \ 2 \ 1 \ \frac{6}{10} \\ 3 \ 2 \ \frac{4}{10} \end{array} \\
 \hline
 24 \ 7 \ 6 \text{ for A.}
 \end{array}$$

$$\begin{array}{r}
 \begin{array}{ccc} l. & s. & d. \\ 1 & : 12 & :: 70 \ 8 \ 10 \\ & & 12 \end{array} \\
 \hline
 42 \ 0 \ 0 \\
 \begin{array}{r} 4 \ 9 \ 2 \ \frac{4}{10} \\ 6 \end{array} \\
 \hline
 42 \ 5 \ 3 \ 2 \ \frac{4}{10} \text{ for B.}
 \end{array}$$

$$\begin{array}{r}
 \begin{array}{ccc} l. & s. & d. \\ 1 & : 12 & :: 84 \ 19 \ 4 \\ & & 12 \end{array} \\
 \hline
 50 \ 8 \ 0 \\
 \begin{array}{r} 11 \ 3 \\ 1 \ 3 \ \frac{2}{10} \\ 2 \ 1 \ \frac{6}{10} \end{array} \\
 \hline
 50 \ 19 \ 7 \ 0 \ \frac{8}{10} \text{ for C.}
 \end{array}$$

$$\begin{array}{r}
 \begin{array}{ccc} l. & s. & d. \\ 1 & : 12 & :: 178 \ 18 \ 6 \frac{1}{2} \\ & & 12 \end{array} \\
 \hline
 106 \ 16 \ 0 \\
 \begin{array}{r} 10 \ 9 \ 2 \ \frac{4}{10} \\ 3 \ 2 \ \frac{4}{10} \\ 1 \ \frac{2}{10} \end{array} \\
 \hline
 107 \ 7 \ 1 \ \frac{1}{2} \text{ for D.}
 \end{array}$$

Proof by the common Way.

<i>l.</i>	<i>s.</i>	<i>l.</i>	<i>s.</i>	<i>d.</i>
1	:	12	:	:
		40	12	6
		20		
		812		
		12		
		9750		
		12		

<i>l.</i>	<i>s.</i>	<i>d.</i>
24	10	117000
48	17	2476
		96

210

192

180

168

12

12

24)144(6

144

l. *s.* *d.**Ans.* 24 7 6 for A.Note, Division is made by 240, because 240 d. are equal to 1*l.*

By Practice.

By Decimals.

<i>s.</i>	<i>l.</i>	<i>s.</i>	<i>d.</i>	<i>s.</i>
10	40	12	6	at 12 per <i>l.</i>
2	20	6	3	
	4	1	3	
	24	7	6	

40.625

.6

l. 24.3570

20

s. 7.500

12

d. 6.0

MISCELLANEOUS ARITHMETIC.

177

$$l. \quad s. \quad d. \quad l. \quad s. \quad d.$$

$$1 : 12 :: 70 \quad 8 \quad 10$$

$$\begin{array}{r} 20 \\ 1408 \\ 12 \\ \hline 16906 \end{array}$$

$$24 \overline{) 102028712} (8415(42 \quad 5 \quad 3 \quad 2 \quad \frac{96}{240}$$

$$\begin{array}{r} 192 \\ 108 \\ 96 \\ \hline 127 \\ 120 \\ \hline 72 \\ 12 \end{array}$$

$$24 \overline{) 108614} (3d.$$

$$\begin{array}{r} 72 \\ 144 \\ 4 \end{array}$$

$$24 \overline{) 105716} (2 \text{ grs.}$$

$$\begin{array}{r} 48 \\ 96 \end{array}$$

Ans. 42 l. 5 s. 3 d. 2 grs. $\frac{96}{240}$ for B.

By Practice.

By Decimals.

10	$\frac{1}{2}$	70	8	10	at 12 per l.
2	$\frac{1}{3}$	35	4	5	
		7	0	10	$\frac{1}{2} \quad \frac{2}{5}$
		42	5	3	$\frac{1}{2} \quad \frac{2}{5} \text{ or } \frac{4}{10}$

$$\begin{array}{r} 70.441666+ \\ .6 \\ \hline l. 42.2649996 \\ 20 \\ \hline s. 5.2999920 \\ 12 \\ \hline d. 3.599904 \\ 4 \\ \hline grs. 2.399616 \end{array}$$

Note, The first Decimal Fraction above, being a little imperfect (which is the Decimal of a l. equivalent to 8 s. 10 d.) is the Reason why the Decimal .399+ is short of .4

MISCELLANEOUS ARITHMETIC.

$$l. \quad s. \quad l. \quad s. \quad d.$$

$$1 : 12 :: 84 \quad 19 \quad 4$$

20

1699

12

20392

12

$$24 \overline{) 102447014} (10119(50 \quad 19 \quad 7.2$$

24

47

24

230

216

144

12

$$24 \overline{) 102447014} (10119(50 \quad 19 \quad 7.2$$

168

48

Ans. 50 l. 19 s. 7.2 d. for C.

By Practice.

$$l. \quad s. \quad d. \quad s.$$

$$10 \quad \frac{1}{2} \quad 84 \quad 19 \quad 4 \text{ at } 12 \text{ per } l.$$

2

 $\frac{1}{5}$

42

9

8

8

9

11

0.8

50

19

7

c.8

By Decimals.

$$84.9666\frac{1}{5}$$

.6

$$l. \quad 50.97996$$

20

$$s. \quad 19.5992$$

12

$$d. \quad 7.1904$$

Note, The first Decimal being a little defective is the Reason why the last is not quite .2, though very near it.

l. s. d. l. s. d.
 $1 : 12 :: 178 \text{ } 18 \text{ } 6\frac{1}{2}$

$$\begin{array}{r} 20 \\ \hline 3578 \\ 12 \\ \hline 42942 \\ 4 \\ \hline 171770 \end{array}$$

$$\begin{array}{r} 12 \text{ } 210 \text{ } l. \text{ } s. \text{ } d. \\ 9610)20612410(21417(107 \text{ } 7 \text{ } 1\frac{1}{2} \\ 192 \end{array}$$

$$\begin{array}{r} 141 \\ 96 \\ \hline 452 \\ 384 \\ \hline 684 \\ 672 \\ \hline 12 \\ 12 \\ \hline 96)144(1 \text{ } D. \\ 96 \\ \hline 48 \\ 4 \\ \hline 96)192(2 \text{ } qrs. \\ 192 \\ \hline 0 \end{array}$$

Answ. 107*l.* 7*s.* 1*d.* $\frac{1}{2}$ for D.

By Practice.

By Decimals.

	<i>l.</i>	<i>s.</i>	<i>d.</i>	<i>s.</i>
10 $\frac{1}{2}$	178	18	$6\frac{1}{2}$	at 12 per <i>l.</i>
2 $\frac{1}{5}$	89	9	$3\frac{1}{4}$	
	17	17	$10\frac{1}{4}$	
	107	7	$1\frac{1}{2}$	

$$\begin{array}{r} 178.927\frac{1}{2} \\ .6 \\ \hline l. 107.3562 \\ 20 \\ \hline s. 7.1240 \\ 12 \\ \hline 1.488 \\ 4 \\ \hline gr. 1.952 \end{array}$$

Note, The first Decimal being not exact, occasions the last to be a little defective also.

180 MISCELLANEOUS ARITHMETIC.

4. My Factor sends me Word, that he has bought Goods, upon my Account, to the Value of 517*l.* 18*s.* 9*d.* what does his Commission come to, at $2\frac{1}{4}$ per Cent. ?

$$\begin{array}{r} \textit{l.} \quad \textit{l.} \quad \textit{s.} \quad \textit{l.} \quad \textit{s.} \quad \textit{d.} \\ 100 : 2 \quad 5 :: 517 \quad 18 \quad 9 \\ \hline 2 \quad 5 \end{array}$$

$$\begin{array}{r} 1035 \quad 17 \quad 6 \\ 129 \quad 5 \quad 0 \\ \hline 4 \quad 6 \\ \hline 2\frac{1}{4} \\ \hline 100) 1165 \quad 7 \quad 2\frac{1}{4} (11 \quad 13 \quad 0\frac{3}{4} \\ 1000 \\ \hline 165 \\ 100 \\ \hline 65 \quad 7 \\ 65 \quad 0 \\ \hline 7 \quad 2\frac{1}{4} \\ 6 \quad 3 \\ \hline 11\frac{1}{4} \end{array}$$

$$\begin{array}{r} \textit{l.} \quad \textit{s.} \quad \textit{d.} \\ 11 \quad 13 \quad 0\frac{3}{4} \\ \hline 10 \quad 13 \quad 0\frac{3}{4} \\ \hline 1 \quad 0 \quad 0 \end{array}$$

PROOF.
1. By whole Numbers.

$$\begin{array}{r} \textit{l.} \quad \textit{s.} \quad \textit{d.} \\ 5 \quad \frac{1}{4} \quad | \quad 517 \quad 18 \quad 9 \\ \hline 1035 \quad 17 \quad 6 \\ 129 \quad 9 \quad 8\frac{1}{4} \\ \hline \textit{l.} \quad 1165 \quad 7 \quad 2\frac{1}{4} \\ 20 \\ \hline \textit{s.} \quad 13 \quad 07 \\ 12 \\ \hline \textit{d.} \quad 0186 \\ 4 \\ \hline \textit{qrs.} \quad 3145 \end{array}$$

$$\text{Answ. } 11 \textit{l.} \quad 13 \textit{s.} \quad 0 \textit{d.} \quad 3 \textit{qrs.} \quad \frac{45}{100}$$

Or thus.

<i>l.</i>	<i>l.</i>	<i>s.</i>	<i>l.</i>	<i>s.</i>	<i>d.</i>
100	: 2	5	:: 517	18	9
<u>240</u>	<u>20</u>		<u>20</u>		
24000	40		10358		
			<u>12</u>		

124305

45

621525

497220

	<i>l.</i>	<i>s.</i>	<i>d.</i>
24 000)55931725(2313(11 13			$0\frac{3}{4}$
48			

79

72

73

72

1725

12

20700

4

24|000)821800(3

72

10800

Ans. 11 *l.* 13 *s.* 0 *d.* $\frac{3}{4}$ $\frac{108}{240} = \frac{45}{100}$

$12) \frac{108}{240} (\frac{9}{20} \& \frac{9}{20} \times 5 = \frac{45}{100}$

2. By Vulgar Fractions.

<i>l.</i>	<i>l.</i>	<i>l.</i>
100	: 2 $\frac{5}{20}$	:: 517 $\frac{225}{240}$

$2 \frac{5}{20} = \frac{45}{20}$

$517 \frac{225}{240} = \frac{124305}{240}$

$\frac{45}{20} \times \frac{124305}{240} = \frac{5593725}{4800}$

$\frac{100}{1}) 5593725 (5593725$

MISCELLANEOUS ARITHMETIC.

48|0000)55913725(11 l.

48

79

48

313725

20

48|0000)62714500(13 s.

48

147

144

345

12

4140

4

48|00)165160(3 qrs.

144

216

Answ. 11 l. 13 s. 0 d. $\frac{3}{4}$ $\frac{216}{480}$.

3. By Decimals.

l. l. l.

100 : 2.25 :: 517.9375

2.25

25896875

10358750

10358750

l. 11.65359375

20

s. 13.07187500

12

d. 0.862500

4

qrs. 3.4500

Answ. 11 l. 13 s. 0 d. 3.45 qrs.

MISCELLANEOUS ARITHMETIC. 183

5. A Tradesman stands indebted to several Persons, as follows, viz. to A 50*l.* 17*s.* 6*d.* to B 119*l.* 14*s.* 8*d.* to C 401*l.* 10*s.* 6*d.* and to D 141*l.* 19*s.* Now, as his whole Estate amounts to no more than 327*l.* 15*s.* 10*d.* $\frac{1}{2}$, how must it be divided among his Creditors, that each Man may have a Share in Proportion to the Debt due to him?

	<i>l.</i>	<i>s.</i>	<i>d.</i>
A-	50	17	6
B-	119	14	8
C-	401	10	6
D-	141	19	0
	714	1	8

$$\begin{array}{r}
 \textit{l. s. d.} \quad \textit{l. s. d.} \quad \textit{l. s. d.} \\
 714 \quad 1 \quad 8 : 327 \quad 15 \quad 10\frac{1}{2} :: 50 \quad 17 \quad 6 \\
 \quad \quad \quad 50 \quad 17 \quad 6
 \end{array}$$

$$\begin{array}{r}
 \text{By } 50 \textit{l.} \quad 16389 \quad 13 \quad 9 \\
 \quad \quad \quad 277 \quad 19 \quad 0 \\
 \text{By } 17 \textit{s.} \quad \left\{ \begin{array}{l} 12 \quad 9 \\ \quad 8 \quad \frac{1}{2} \\ \quad \quad \frac{1}{4} \quad \frac{7}{10} \end{array} \right. \\
 \text{By } 6 \textit{d.} \quad \left\{ \begin{array}{l} 8 \quad 3 \quad 6 \\ \quad \quad 4 \quad \frac{1}{2} \\ \quad \quad \quad \frac{1}{4} \quad 0 \quad \frac{48}{90} \end{array} \right.
 \end{array}$$

$$\begin{array}{r}
 \textit{l. s. d.} \quad \textit{l. s. d.} \\
 714 \quad 1 \quad 8 \quad 8) 16676 \quad 10 \quad 1 \quad \frac{1}{2} \quad \frac{7}{10} \quad \frac{48}{90} (23 \quad 7 \quad 0\frac{3}{4} \\
 \quad \quad \quad 14281 \quad 13 \quad 4 \\
 \quad \quad \quad \hline
 \quad \quad \quad 2394 \quad 16 \quad 9 \\
 \quad \quad \quad 2142 \quad 5 \quad 0 \\
 \quad \quad \quad \hline
 \quad \quad \quad 252 \quad 11 \quad 9 \\
 \quad \quad \quad 249 \quad 18 \quad 7 \\
 \quad \quad \quad \hline
 \quad \quad \quad 2 \quad 13 \quad 2 \quad \frac{1}{2} \quad \frac{7}{10} \quad \frac{48}{90} \\
 \quad \quad \quad 2 \quad 4 \quad 7 \quad \frac{1}{2} \quad \frac{7}{10} \quad \frac{48}{90} \\
 \quad \quad \quad \hline
 \quad \quad \quad 8 \quad 7 \quad 0 \quad \frac{1}{10}
 \end{array}$$

Ans. 23*l.* 7*s.* 0*d.* $\frac{3}{4}$ $\frac{0 \textit{l. } 8 \textit{s. } 7 \textit{d. } 0 \textit{qrs. } \frac{5}{10}}{714 \quad 1 \quad 8}$ for A.

714 $l.$ 1 $s.$ 8 : 327 $l.$ 15 $s.$ 10 $\frac{1}{2}$:: 119 $l.$ 14 $s.$ 8
 119 $l.$ 14 $s.$ 8

By 119 $l.$ 39007 9 1 $\frac{1}{2}$

By 14 $s.$ { 228 18 0
 10 6
 7
 0 $\frac{1}{4}$ $\frac{4}{10}$

By 8 $d.$ { 10 18 0
 6
 0 $\frac{1}{4}$ $\frac{3}{10}$ $\frac{8}{24}$

$l.$ $s.$ $d.$ $l.$ $s.$ $d.$
 714 1 8) 39247 16 9 0 $\frac{8}{10}$ (54 19 3
 35704 3 4

3543 13 5
 2856 6 8

687 6 9
 678 7 7

8 19 2 0 $\frac{8}{10}$
 8 18 6 $\frac{1}{4}$

7 $\frac{3}{4}$ $\frac{8}{10}$

$l.$ $s.$ $d.$ $l.$ $s.$ $d.$
 Anfw. 54 19 3 $\frac{0}{714}$ $\frac{0}{1}$ $\frac{7 \frac{3}{4} \frac{8}{10}}{8}$ for B.

MISCELLANEOUS ARITHMETIC.

184

$$\begin{array}{r} l. \quad s. \quad d. \quad l. \quad s. \quad d. \quad l. \quad s. \quad d. \\ 714 \quad 1 \quad 8 : 327 \quad 15 \quad 10\frac{1}{2} :: 401 \quad 10 \quad 6 \\ \quad \quad \quad 401 \quad 10 \quad 6 \end{array}$$

By 401 l. 131445 5 10 $\frac{1}{2}$

By 10 s. } 163 10 0

By 6 d. } 7 6

8 3 5

4 0 $\frac{1}{4}$

0 0 $\frac{1}{2}$

0 0 $\frac{1}{24}$

$$\begin{array}{r} l. \quad s. \quad d. \quad l. \quad s. \quad d. \\ 714 \quad 1 \quad 8) 131617 \quad 7 \quad 8 \quad \frac{1}{8} \quad 0 \quad \frac{13}{84} (184 \quad 6 \quad 3\frac{1}{4} \\ \quad \quad \quad 71408 \quad 6 \quad 8 \end{array}$$

60209 1 0

57126 13 4

3082 7 8

2856 6 8

226 1 0

214 4 6

11 16 6 $\frac{1}{2}$

8 18 6 $\frac{1}{4}$

2 18 0 $\frac{1}{4}$ 0 $\frac{12}{24}$

2 4 7 $\frac{1}{2}$ $\frac{2}{10}$ $\frac{12}{24}$

13 4 $\frac{1}{2}$ $\frac{8}{10}$

Ans. 184 6 3 $\frac{1}{4}$ $\frac{l. \quad s. \quad d.}{0 \quad 13 \quad 4 \quad \frac{1}{2} \quad \frac{8}{10}}$ for C.

MISCELLANEOUS ARITHMETIC.

$$\begin{array}{r} l. \quad s. \quad d. \quad l. \quad s. \quad d. \quad l. \quad s. \\ 714 \quad 1 \quad 8 : 327 \quad 15 \quad 10\frac{1}{2} :: 141 \quad 19 \\ \quad \quad \quad 141 \quad 19 \end{array}$$

$$\text{By } 141 l. \quad \begin{array}{r} 46218 \quad 18 \quad 4\frac{1}{2} \\ 310 \quad 13 \\ 14 \quad 3 \end{array}$$

$$\text{By } 19 s. \quad \left. \begin{array}{r} 9 \quad 1\frac{1}{2} \\ 9 \quad \frac{1}{4} \quad \frac{9}{10} \end{array} \right\}$$

$$\begin{array}{r} l. \quad s. \quad d. \quad l. \quad s. \quad d. \\ 714 \quad 1 \quad 8) 46530 \quad 6 \quad 5 \quad \frac{1}{4} \quad \frac{9}{10} (65 \quad 3 \quad 2\frac{1}{2} \\ \quad \quad \quad 42825 \end{array}$$

$$\begin{array}{r} 3685 \quad 6 \quad 5 \\ 3570 \quad 8 \quad 4 \end{array}$$

$$\begin{array}{r} 114 \quad 18 \quad 1 \\ 107 \quad 2 \quad 3 \end{array}$$

$$\begin{array}{r} 7 \quad 15 \quad 10 \quad \frac{1}{4} \quad \frac{9}{10} \\ 5 \quad 19 \quad 0 \quad 0 \quad \frac{6}{10} \quad \frac{4}{8} \end{array}$$

$$\begin{array}{r} 1 \quad 16 \quad 10 \quad \frac{1}{4} \quad \frac{2}{10} \quad \frac{2}{8} \\ 1 \quad 9 \quad 9 \quad 0 \quad \frac{1}{10} \quad \frac{4}{8} \end{array}$$

$$\begin{array}{r} 7 \quad 1 \quad \frac{1}{4} \quad 0 \quad \frac{4}{8} \end{array}$$

$$\text{Answ. } \begin{array}{r} l. \quad s. \quad d. \\ 65 \quad 3 \quad 2\frac{1}{2} \end{array} \quad \begin{array}{r} l. \quad s. \quad d. \\ 0 \quad 7 \quad 1 \quad \frac{1}{4} \quad 0 \quad \frac{4}{8} \end{array} \text{ for D.}$$

Remainders.

$$\begin{array}{r} l. \quad s. \quad d. \\ A \quad 23 \quad 7 \quad 0\frac{3}{4} \end{array}$$

$$\begin{array}{r} B \quad 54 \quad 19 \quad 3 \end{array}$$

$$\begin{array}{r} C \quad 184 \quad 6 \quad 3\frac{3}{4} \end{array}$$

$$\begin{array}{r} D \quad 65 \quad 3 \quad 2\frac{1}{2} \end{array}$$

Remainder

$$\begin{array}{r} 327 \quad 15 \quad 10\frac{1}{2} \end{array}$$

$$\begin{array}{r} l. \quad s. \quad d. \quad gr. \end{array}$$

$$\begin{array}{r} 0 \quad 8 \quad 7 \quad 0 \quad \frac{5}{10} \end{array}$$

$$\begin{array}{r} 0 \quad 0 \quad 7 \quad 3 \quad \frac{8}{10} \end{array}$$

$$\begin{array}{r} 0 \quad 13 \quad 4 \quad 2 \quad \frac{8}{10} \end{array}$$

$$\begin{array}{r} 0 \quad 7 \quad 1 \quad 1 \quad 0 \quad \frac{4}{8} \end{array}$$

$$\begin{array}{r} l. \quad s. \quad d. \\ 714 \quad 1 \quad 8) 1 \quad 9 \quad 9 \quad 0 \quad \frac{1}{10} \quad \frac{4}{8} (2 \text{ qrs} \\ \quad \quad \quad 1 \quad 9 \quad 9 \quad 0 \quad \frac{1}{10} \quad \frac{4}{8} \end{array}$$

0
—

The Proof by common Arithmetic.

<i>l.</i>	<i>s.</i>	<i>d.</i>	<i>l.</i>	<i>s.</i>	<i>d.</i>	<i>l.</i>	<i>s.</i>	<i>d.</i>
714	1	8	327	15	10 $\frac{1}{2}$	50	17	6
20			20			20		
14281			6555			1017		
12			12			12		
171380			78670			12210		
			4			314682		
			314682			24420		
						97680		
						73260		
						48840		
						12210		
						36330		
						4		
			1713810	38422672210	(22419	3		
			34276			12)5604		
			41466					
			34276			210)4617		
			71907			£23 7 0 $\frac{1}{2}$		
			68552					
			33552					
			17138					
			164142					
			154242					
			99000					

A

$\begin{array}{r} l. \quad s. \quad d. \quad l. \quad s. \quad d. \quad l. \quad s. \quad d. \\ 714 \quad 1 \quad 8 : 327 \quad 15 \quad 10\frac{1}{2} : : 119 \quad 14 \quad 8 \\ \quad 20 \quad \quad \quad 20 \quad \quad \quad 20 \end{array}$

14281
 12

6555
 12

2394
 12

171380

78670
 4

28736
314682

314682

57472
 229888

172416

114944

28736

86208

1713810)90427019512(52764
85690

12)13191 3

47370

34276

210)10919

130941

119966

£54 19 3

109759

102828

69315

68552

7632

B

<i>l.</i>	<i>s.</i>	<i>d.</i>	<i>l.</i>	<i>s.</i>	<i>d.</i>	<i>l.</i>	<i>s.</i>	<i>d.</i>
714	1	8	327	15	10 $\frac{1}{2}$	401	10	6
20			20			20		
<u>14281</u>			<u>6555</u>			<u>8030</u>		
12			12			12		
<u>171380</u>			<u>78670</u>			<u>96366</u>		
			4			<u>314682</u>		
			<u>314682</u>			<u>192732</u>		
						770928		
						578196		
						385464		
						96366		
						289098		
						<u>4</u>		
			1713810	303246456112		(176943	3	
			<u>17138</u>			<u>12)44235</u>	3	
			<u>131866</u>			<u>210)36816</u>		
			<u>119966</u>			<u>£184 6</u>	<u>3$\frac{3}{4}$</u>	
			<u>119004</u>					
			<u>102828</u>					
			<u>161765</u>					
			<u>154242</u>					
			<u>75236</u>					
			<u>68552</u>					
			<u>66841</u>					
			<u>51414</u>					
			<u>154272</u>					

C

l. s. d. l. s. d. l. s.
 714 1 8 : 327 15 10 $\frac{1}{2}$:: 141 19
 20 20 20

14281
 12

171380

6555
 12

78670

4

314682

2839
 12

34068

314682

68136

272544

204408

136272

34068

102204

171380) 107205863716 (62554 2

102828

43778

34276

95026

85690

93363

85690

76737

68552

81856

12) 15638 2

20) 13013

£65 3 2 $\frac{1}{2}$

D

l. s. d.
 A 23 7 c $\frac{3}{4}$
 B 54 19 3
 C 184 6 3 $\frac{3}{4}$
 D 65 3 2 $\frac{1}{2}$
 Remainder $\frac{1}{2}$

£327 15 10 $\frac{1}{2}$

Remainders.

99000

7632

154272

81856

171380) 342760 (2 qrs

342760

0

6. Five Merchants traded together: *A* put into the common Stock 721*l.* 14*s.* 6*d.* $\frac{1}{2}$, for 11 Months; *B* put in 400*l.* 12*s.* 8*d.* $\frac{3}{4}$, for 17 Months; *C* put in 326*l.* 12*s.* 5*d.* $\frac{1}{4}$, for 18 Months; *D* put in 536*l.* 14*s.* 9*d.* $\frac{1}{2}$, for 13 Months; and *E* put in 239*l.* 17*s.* 4*d.* $\frac{1}{2}$, for 15 Months; now the whole Gain being 987*l.* 16*s.* 5*d.* $\frac{3}{4}$, how much was due to each Trader?

A *l.* *s.* *d.*
721 14 6 $\frac{1}{2}$

7938 19 14 $\frac{1}{2}$

B *l.* *s.* *d.*
400 12 8 $\frac{3}{4}$

1602 10 11 $\frac{1}{4}$

6410 3 8 $\frac{3}{4}$

6810 16 4 $\frac{3}{4}$

C *l.* *s.* *d.*
326 12 5 $\frac{1}{4}$

1959 14 7 $\frac{1}{2}$

5879 3 10 $\frac{1}{2}$

D *l.* *s.* *d.*
536 14 9 $\frac{1}{2}$

2146 19 2 $\frac{1}{2}$

6440 17 6 $\frac{1}{2}$

6977 12 3 $\frac{1}{2}$

E *l.* *s.* *d.*
239 17 4 $\frac{1}{2}$

1199 6 10 $\frac{1}{2}$

3598 0 7 $\frac{1}{2}$

By the Parts of 13.

By the Parts of 15.

By the Parts of 17.

By the Parts of 18.

	<i>l.</i>	<i>s.</i>	<i>d.</i>
<i>A</i>	7938	19	11 $\frac{1}{2}$
<i>B</i>	6810	16	4 $\frac{3}{4}$
<i>C</i>	5879	3	10 $\frac{1}{2}$
<i>D</i>	6977	12	3 $\frac{1}{2}$
<i>E</i>	3598	0	7 $\frac{1}{2}$
	31204	13	1 $\frac{1}{4}$

$$\begin{array}{rcl} l. & s. & d. \\ 31204 & 13 & 1\frac{3}{4} : 987 \end{array} \quad \begin{array}{rcl} l. & s. & d. \\ 16 & 5\frac{3}{4} & :: 7938 \end{array} \quad \begin{array}{rcl} l. & s. & d. \\ 19 & 11\frac{1}{2} & \end{array}$$

$$7938 \ 19 \ 11\frac{1}{2}$$

$$987 \times 7938 = \left\{ \begin{array}{l} 7896 \\ 2961 \\ 8883 \\ 6909 \end{array} \right.$$

$$\begin{array}{rcl} 7938 l. \times 16 s. & - & 6350 \ 8 \ 0 \\ \hline \quad \times 5 d. & - & 165 \ 7 \ 6 \\ \hline \quad \times 3 qrs. & - & 24 \ 16 \ 1 \ 2 \\ 987 l. \times 19 s. & - & 937 \ 13 \ 0 \ 0 \\ \hline \quad \times 11 d. & - & 45 \ 4 \ 9 \ 0 \\ \hline \quad \times 2 qrs. & - & 2 \ 1 \ 1 \ 2 \\ 16 s. \times 19 s. & - & - \ 15 \ 2 \ 1 \ \frac{6}{10} \\ \hline \quad \times 11 d. & - & - \ 8 \ 3 \ \frac{2}{10} \\ \hline \quad \times 2 qrs. & - & - \ 1 \ \frac{6}{10} \\ 19 s. \times 5 d. & - & - \ 4 \ 3 \\ \hline \quad \times 3 qrs. & - & - \ 2 \ \frac{8}{10} \ \frac{1}{2} = 4\frac{8}{6} \\ 5 d. \times 11 d. & - & - \ 9 \ \frac{1}{10} \ \frac{1}{6} = 1\frac{6}{6} \\ \hline \quad \times 2 qrs. & - & - \ 10 \ \frac{1}{6} \ \frac{4}{6} = 2\frac{4}{6} \\ 11 d. \times 3 qrs. & - & - \ 1 \ \frac{1}{10} \ \frac{3}{6} = 3\frac{6}{6} \\ 3 \times 2 qrs. & - & - \ 2 \ \frac{1}{6} \ \frac{6}{6} = 2\frac{6}{6} \end{array}$$

$$\text{£}7842332 \ 6 \ 11 \ 1 \ \frac{3}{10} \ \frac{50}{96}$$

$$\begin{array}{rcl} l. & s. & d. \\ 31204 & 13 & 1\frac{3}{4} \end{array} \quad \begin{array}{rcl} l. & s. & d. \text{ qr.} \\ 7842332 & 6 \ 11 \ 1 & \frac{3}{10} \ \frac{50}{96} \end{array} \quad \begin{array}{rcl} l. & s. & d. \\ (251 & 6 & 4\frac{1}{2} \end{array}$$

$$6240931 \ 9 \ 2$$

$$1601400 \ 17 \ 9 \ 1$$

$$1560232 \ 17 \ 3 \ 2$$

$$41168 \ 0 \ 5 \ 3$$

$$31204 \ 13 \ 1 \ 3$$

$$9963 \ 7 \ 4 \ 0 \ \frac{1}{10}$$

$$9361 \ 7 \ 11 \ 1 \ \frac{3}{10}$$

$$601 \ 19 \ 4 \ 3 \ 0 \ \frac{50}{96}$$

$$520 \ 1 \ 6 \ 2 \ \frac{5}{10} \ \frac{16}{96}$$

$$81 \ 17 \ 10 \ 0 \ \frac{5}{10} \ \frac{14}{96}$$

$$65 \ 0 \ 2 \ 1 \ \frac{3}{10} \ \frac{14}{96}$$

$$10 \ 17 \ 7 \ 3 \ \frac{3}{10} \ \frac{20}{96}$$

$$\begin{array}{rcl} l. & s. & d. \\ \text{Answ. } 251 & 6 & 4\frac{1}{2} \end{array} \quad \begin{array}{rcl} l. & s. & d. \text{ qr.} \\ 16 \ 17 \ 7 & 3 & \frac{2}{10} \ \frac{20}{96} \end{array} \quad \text{for A.}$$

$$31204 \ 13 \ 1 \ 3$$

MISCELLANEOUS ARITHMETIC.

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$$\begin{array}{rcl} \text{l.} & \text{s.} & \text{d.} \\ 31204 & 13 & 1\frac{3}{4} : 987 \text{ } 16 \text{ } 5\frac{3}{4} :: 6810 \text{ } 16 \text{ } 4\frac{3}{4} \\ & & 6810 \text{ } 16 \text{ } 4\frac{3}{4} \end{array}$$

$$\begin{array}{rcl} 987 \times 6810 & \left\{ \begin{array}{l} 9870 \\ 7896 \\ 5922 \end{array} \right. \\ 6810 \text{ l.} \times 16 \text{ s.} & - & 5448 \\ \text{---} \times 5 \text{ d.} & - & 141 \text{ } 17 \text{ } 6 \\ \text{---} \times 3 \text{ qrs.} & - & 21 \text{ } 5 \text{ } 2 \text{ } 2 \\ 987 \text{ l.} \times 16 \text{ s.} & - & 789 \text{ } 12 \text{ } 0 \text{ } 0 \\ \text{---} \times 4 \text{ d.} & - & 16 \text{ } 9 \text{ } 0 \text{ } 0 \\ \text{---} \times 3 \text{ qrs.} & - & 3 \text{ } 1 \text{ } 8 \text{ } 1 \\ 16 \text{ s.} \times 16 \text{ s.} & - & 12 \text{ } 9 \text{ } 2 \text{ } \frac{4}{10} \\ \text{---} \times 4 \text{ d.} & - & 3 \text{ } 0 \text{ } \frac{8}{10} \\ \text{---} \times 3 \text{ qrs.} & - & 2 \text{ } \frac{4}{10} \\ 16 \text{ s.} \times 5 \text{ d.} & - & 4 \text{ } 0 \\ \text{---} \times 3 \text{ qrs.} & - & 2 \text{ } \frac{4}{10} \\ 5 \text{ d.} \times 4 \text{ d.} & - & \frac{3}{10} \text{ } \frac{2}{6} = \frac{8}{24} = \frac{13}{96} \\ \text{---} \times 3 \text{ qrs.} & - & \frac{15}{24} = \frac{5}{8} \\ 4 \text{ d.} \times 3 \text{ qrs.} & - & \frac{12}{24} = \frac{1}{2} \\ 3 \text{ qrs.} \times 3 \text{ qrs.} & - & \frac{9}{96} \end{array}$$

$$\text{£}6727890 \text{ } 19 \text{ } 3 \text{ } 3 \text{ } \frac{4}{10} \text{ } \frac{53}{96}$$

$$\begin{array}{rcl} \text{l.} & \text{s.} & \text{d.} \\ 31204 & 13 & 1\frac{3}{4}) 6727890 \text{ } 19 \text{ } 3 \text{ } 3 \text{ } \frac{4}{10} \text{ } \frac{53}{96} (215 \text{ } 12 \text{ } 1\frac{1}{4} \\ & & 6240931 \text{ } 9 \text{ } 2 \\ & & \text{---} \\ & & 486959 \text{ } 10 \text{ } 1 \text{ } 3 \\ & & 312046 \text{ } 11 \text{ } 5 \text{ } 2 \\ & & \text{---} \\ & & 174912 \text{ } 18 \text{ } 8 \text{ } 1 \\ & & 156023 \text{ } 5 \text{ } 8 \text{ } 3 \\ & & \text{---} \\ & & 18889 \text{ } 12 \text{ } 11 \text{ } 2 \text{ } \frac{4}{10} \\ & & 18722 \text{ } 15 \text{ } 10 \text{ } 2 \text{ } \frac{6}{10} \\ & & \text{---} \\ & & 166 \text{ } 17 \text{ } 0 \text{ } 3 \text{ } \frac{8}{10} \text{ } \frac{53}{96} \\ & & 130 \text{ } 0 \text{ } 4 \text{ } 2 \text{ } \frac{6}{10} \text{ } \frac{28}{96} \\ & & \text{---} \\ & & 36 \text{ } 16 \text{ } 8 \text{ } 1 \text{ } \frac{2}{10} \text{ } \frac{25}{96} \\ & & 32 \text{ } 10 \text{ } 1 \text{ } 0 \text{ } \frac{6}{10} \text{ } \frac{53}{96} \\ & & \text{---} \\ & & 4 \text{ } 6 \text{ } 7 \text{ } 0 \text{ } \frac{5}{10} \text{ } \frac{66}{96} \end{array}$$

$$\begin{array}{rcl} \text{l.} & \text{s.} & \text{d.} \\ \text{Ans'd.} & 215 & 12 \text{ } 1\frac{1}{4} \\ & & \text{---} \\ & & 31204 \text{ } 13 \text{ } 1 \text{ } \frac{3}{4} \end{array} \text{ for B.}$$

$$\begin{array}{rcl}
 \text{l.} & \text{s.} & \text{d.} \\
 31204 & 13 & 1\frac{3}{4} : 987 \text{ } 16 \text{ } 5\frac{3}{4} :: 5879 \text{ } 3 \text{ } 10\frac{1}{2} \\
 & & \underline{5879 \text{ } 3 \text{ } 10\frac{1}{2}}
 \end{array}$$

$$\begin{array}{rcl}
 \text{l.} & \text{l.} & \left\{ \begin{array}{l} 8883 \\ 6909 \\ 7896 \\ 4935 \end{array} \right. \\
 987 \times 5879 & & \\
 \hline
 \text{---} \times 3 \text{ s.} & - & 148 \text{ } 1 \text{ } 0 \\
 \text{---} \times 10 \text{ d.} & - & 41 \text{ } 2 \text{ } 6 \\
 \text{---} \times 2 \text{ qrs.} & - & 2 \text{ } 1 \text{ } 1 \text{ } 2 \\
 5879 \text{ l.} \times 16 \text{ s.} & - & 4703 \text{ } 4 \text{ } 0 \text{ } 0 \\
 \text{---} \times 5 \text{ d.} & - & 122 \text{ } 9 \text{ } 7 \text{ } 0 \\
 \text{---} \times 3 \text{ qrs.} & - & 18 \text{ } 7 \text{ } 5 \text{ } 1 \\
 16 \text{ s.} \times 3 \text{ s.} & - & 2 \text{ } 4 \text{ } 3 \text{ } \frac{2}{10} \\
 \text{---} \times 10 \text{ d.} & - & 8 \text{ } 0 \\
 \text{---} \times 2 \text{ qrs.} & - & 1 \text{ } \frac{6}{10} \\
 3 \text{ s.} \times 5 \text{ d.} & - & 3 \\
 \text{---} \times 3 \text{ qrs.} & - & \frac{4}{10} \quad \frac{3}{6} = \frac{12}{24} = \frac{48}{96} \\
 5 \text{ d.} \times 10 \text{ d.} & - & \frac{8}{10} \quad \frac{2}{6} = \frac{8}{24} = \frac{32}{96} \\
 \text{---} \times 2 \text{ qrs.} & - & \frac{1}{10} \quad \frac{2}{6} = \frac{24}{96} \\
 10 \text{ d.} \times 3 \text{ qrs.} & - & \frac{1}{10} \quad \frac{6}{24} = \frac{24}{96} \\
 3 \text{ qrs.} \times 2 \text{ qrs.} & - & \frac{6}{96}
 \end{array}$$

$$\begin{array}{rcl}
 \text{£}5807608 & 8 \text{ } 10 \text{ } 0 \text{ } \frac{2}{10} & \frac{54}{96}
 \end{array}$$

$$\begin{array}{rcl}
 \text{l.} & \text{s.} & \text{d.} \\
 31204 & 13 & 1\frac{3}{4}) 5807608 \text{ } 8 \text{ } 10 \text{ } 0 \text{ } \frac{2}{10} \text{ } \frac{54}{96} (186 \text{ } 2 \text{ } 3
 \end{array}$$

$$\begin{array}{rcl}
 3120465 & 14 & 7 \\
 2687142 & 14 & 3 \\
 2496372 & 11 & 8 \\
 \hline
 190770 & 2 & 7 \text{ } 0 \\
 187227 & 18 & 10 \text{ } 2 \\
 \hline
 3542 & 3 & 8 \text{ } 2 \text{ } \frac{2}{10} \\
 3120 & 9 & 3 \text{ } 3 \text{ } \frac{1}{10} \\
 \hline
 422 & 14 & 4 \text{ } 3 \text{ } \frac{1}{10} \text{ } \frac{54}{96} \\
 390 & 1 & 1 \text{ } 3 \text{ } \frac{8}{10} \text{ } \frac{84}{96} \\
 \hline
 31 & 13 & 2 \text{ } 3 \text{ } \frac{2}{10} \text{ } \frac{66}{96}
 \end{array}$$

$$\begin{array}{rcl}
 \text{l.} & \text{s.} & \text{d.} \\
 \text{Ans. } 186 & 2 & 3 \\
 \hline
 31 & 13 & 2 \text{ } 3 \text{ } \frac{2}{10} \text{ } \frac{66}{96} \text{ for C.} \\
 31204 & 13 & 1 \text{ } 3
 \end{array}$$

MISCELLANEOUS ARITHMETIC. 195

$$\begin{array}{rcl}
 l. & s. & d. \\
 31204 & 13 & 1\frac{3}{4} : 987 \ 16 \ 5\frac{3}{4} :: 6977 \ 12 \ 3\frac{1}{2} \\
 & & 6977 \ 12 \ 3\frac{1}{2}
 \end{array}$$

$$\begin{array}{l}
 l. \quad l. \\
 987 \times 6977 \left\{ \begin{array}{l} 6909 \\ 6909 \\ 8883 \\ 5922 \end{array} \right.
 \end{array}$$

—	X 12s.	—	592	4					
—	X 3d.	—	12	6	9				
—	X 2qrs.	—	2	1	1	2			
6977l.	X 16s.	—	5881	12	0	0			
—	X 5d.	—	145	7	1	0			
—	X 3qrs.	—	21	16	0	3			
16s.	X 12s.	—	—	9	7	0	$\frac{8}{10}$		
—	X 3d.	—	—	—	2	1	$\frac{6}{10}$		
—	X 2qrs.	—	—	—	—	1	$\frac{6}{10}$		
12s.	X 5d.	—	—	—	—	3	0		
—	X 3qrs.	—	—	—	—	1	$\frac{8}{10}$		
5d.	X 3d.	—	—	—	—	—	$\frac{2}{10}$	$\frac{3}{6} = \frac{12}{24} = \frac{48}{96}$	
—	X 2qrs.	—	—	—	—	—	—	$\frac{10}{24} = \frac{40}{96}$	
3d.	X 3qrs.	—	—	—	—	—	—	$\frac{9}{24} = \frac{36}{96}$	
3qrs.	X 2qrs.	—	—	—	—	—	—	$\frac{6}{24} = \frac{24}{96}$	

$$\begin{array}{r}
 \pounds 6892654 \ 17 \ 1 \ 3 \ \frac{1}{10} \qquad \frac{34}{96}
 \end{array}$$

$$\begin{array}{rcl}
 l. & s. & d. \\
 31204 & 13 & 1\frac{3}{4} : 6892654 \ 17 \ 1 \ \frac{3}{4} \ \frac{1}{10} \ \frac{34}{96} (220 \ 17 \ 8\frac{1}{2})
 \end{array}$$

6240931	9	2			
651723	7	11			
624093	2	11			
27630	5	0	3	$\frac{1}{10}$	$\frac{34}{96}$
26523	19	2	0	$\frac{3}{10}$	$\frac{48}{96}$
1106	5	10	2	$\frac{7}{10}$	$\frac{82}{96}$
1040	3	1	1		$\frac{32}{96}$
66	2	9	1	$\frac{7}{10}$	$\frac{50}{96}$
65	0	2	1	$\frac{3}{10}$	$\frac{14}{96}$
1	2	7	0	$\frac{4}{10}$	$\frac{36}{96}$

$$\begin{array}{rcl}
 l. & s. & d. \\
 \text{Anfw. } 220 \ 17 \ 8\frac{1}{2} & & \\
 & l. & s. & d. & qrs. \\
 & 1 & 2 & 7 & 0 & \frac{4}{10} & \frac{36}{96} \text{ for D.} \\
 & 31204 & 13 & 1 & 3 \\
 & 1 & 2
 \end{array}$$

196 MISCELLANEOUS ARITHMETIC.

$$\begin{array}{rclclcl} l. & s. & d. & l. & s. & d. & l. & s. & d. \\ 31204 & 13 & 1\frac{3}{4} : 987 & 16 & 5\frac{3}{4} : : 3598 & 0 & 7\frac{1}{2} \\ & & 3598 & 0 & 7\frac{1}{2} & & & & \end{array}$$

$$\begin{array}{rcl} l. & l. & \\ 987 \times 3598 & \left\{ \begin{array}{l} 7896 \\ 8883 \\ 4935 \\ 2961 \end{array} \right. & \end{array}$$

$$\begin{array}{rclclcl} \text{---} & \times & 7d. & - & 28 & 15 & 9 \\ \text{---} & \times & 2qrs. & - & 2 & 1 & 1 & 2 \\ 3598l. & \times & 16s. & - & 2878 & 8 & 0 & 0 \\ \text{---} & \times & 5d. & - & 74 & 19 & 2 & 0 \\ \text{---} & \times & 3qrs. & - & 11 & 4 & 10 & 2 \\ 16s. & \times & 7d. & - & - & - & 5 & 2 & \frac{4}{10} \\ \text{---} & \times & 2qrs. & - & - & - & - & 1 & \frac{6}{10} \\ 7d. & \times & 5d. & - & - & - & - & - & \frac{5}{10} \\ \text{---} & \times & 3qrs. & - & - & - & - & - & \frac{5}{10} \\ 5d. & \times & 2qrs. & - & - & - & - & - & \frac{5}{10} \\ 3qrs. & \times & 2qrs. & - & - & - & - & - & \frac{5}{10} \end{array}$$

$$\begin{array}{rclclcl} l. & s. & d. & l. & s. & d. & qrs. & l. & s. & d. \\ 31204 & 13 & 1\frac{3}{4} & 3554221 & 9 & 5 & 0 & \frac{7}{10} & \frac{18}{96} & (113 & 18 & 0 \end{array}$$

$$\begin{array}{rcl} 3120465 & 14 & 7 \\ 433755 & 14 & 10 & 0 \\ 312046 & 11 & 5 & 2 \\ 121709 & 3 & 4 & 2 \\ 93613 & 10 & 5 & 1 \\ 28095 & 3 & 11 & 1 & \frac{7}{10} & \frac{18}{96} \\ 28084 & 3 & 9 & 3 & \frac{9}{10} \\ 11 & 0 & 1 & 1 & \frac{8}{10} & \frac{18}{96} \end{array}$$

$$\begin{array}{rclclcl} l. & s. & d. & l. & s. & d. & qrs. \\ \text{Anfw.} & 113 & 18 & 0 & 11 & 0 & 1 & 1 & \frac{8}{10} & \frac{18}{96} & \text{for E.} \\ & 31204 & 13 & 1 & 3 \end{array}$$

$$\begin{array}{rcl} l. & s. & d. \\ A & 251 & 6 & 4\frac{1}{2} \\ B & 215 & 12 & 1\frac{3}{4} \\ C & 186 & 2 & 3 \\ D & 220 & 17 & 8\frac{1}{2} \\ E & 113 & 18 & 0 \\ \text{Remainder} & & & \frac{1}{2} \\ 987 & 16 & 5\frac{1}{2} \end{array}$$

Remainders.

$$\begin{array}{rclclcl} l. & s. & d. & qrs. & l. & s. & d. & qrs. \\ 16 & 17 & 7 & 3 & \frac{2}{10} & \frac{20}{96} \\ 4 & 6 & 7 & 0 & \frac{5}{10} & \frac{66}{96} \\ 31 & 13 & 2 & 3 & \frac{2}{10} & \frac{66}{96} \\ 1 & 2 & 7 & 0 & \frac{4}{10} & \frac{36}{96} \\ 11 & 0 & 1 & 1 & \frac{8}{10} & \frac{18}{96} \\ 31204 & 13 & 1\frac{3}{4} & 65 & 0 & 2 & 1 & \frac{3}{10} & \frac{14}{96} & (2 \\ 65 & 0 & 2 & 1 & \frac{3}{10} & \frac{14}{96} \end{array}$$

0

MISCELLANEOUS ARITHMETIC.

197

The Proof by common Arithmetic.

A *l.* *s.* *d.*
 721 14 6½
 20

14434
 12

173214
 4

692858
 11

7621438

B *l.* *s.* *d.*
 400 12 8¼
 20

8012
 12

96152
 4

384611
 17

6538387

C *l.* *s.* *d.*
 326 12 5¼
 20

6532
 12

78389
 4

313557
 18

5644026

A 7621438
 B 6538387
 C 5644026
 D 6698510
 E 3454110

29956471

D *l.* *s.* *d.*
 536 14 9½
 20

10734
 12

128817
 4

515270
 13

6698510

E *l.* *s.* *d.*
 239 17 4½
 20

4797
 12

57568
 4

230274
 15

3454110

Whole Gain.

l. *s.* *d.*
 987 16 5¼
 20

19756
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237077
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948311

grs. & time. *grs.* *grs & time.*

29956471 : 948311 :: 7621438

948311

7621438

7621438

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60971504

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68592942

4

29956471)7227493491218 (241266

59912942

12)60316 $\frac{1}{2}$

123619929

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210)50216 (4

37940451

£251 6 4 $\frac{1}{2}$

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79839802

59912942

199268601

179738826

195297758

179738826

15558932

A

MISCELLANEOUS ARITHMETIC.

199

$\text{grs. } \& \text{ time.} \quad \text{grs.} \quad \text{grs. } \& \text{ time.}$
 $29956471 : 948311 : : 6538387$
 948311

6538387
6538387
19615161
52307096
26153548
58845483

29956471)6200424314357(206981
59912942

209130114
179738826

$$12) 51745 \frac{1}{4}$$

210)43112 1

293912883
269608239

£215 12 1 $\frac{3}{4}$

243046445
239651768

33946777
29956471

3990306

grs. & time. *grs.* *grs. & time.*

29956471 : 948311 : : 5644026
948311

5644026

5644026

16932078

45152208

22576104

50796234

29956471) 5352291940086(178668

29956471

12)44667

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210(37212 3

259691870

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239651768

29179458

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29956471 : 948311 : : 6698510
948311

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20095530

53588080

26794040

60286590

29956471)6352270716610 (212050

59912942

36097651

29956471

61411806

59912942

149886461

149782355

1041060

$$12)53012 \quad \frac{1}{2}$$

210)44117 8

£220 17 8½

MISCELLANEOUS ARITHMETIC.

grs. & time. grs. grs. & time.

29956471 : 948311 : : 3454110
948311

3454110
3454110
10362330
27632880
13816440
31086990

29956471) 3275570508210 (109344
29956471
12) 27336
279923408
269608239 210) 22718
103151692 £113 18
89869413

E

132822791
119825884
129969070
119825884
10143186

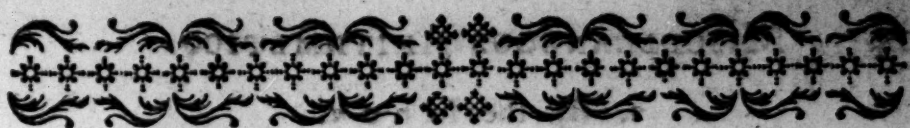
	i.	s.	d.
A	251	6	4 $\frac{1}{2}$
B	215	12	1 $\frac{3}{4}$
C	186	2	3
D	220	17	8 $\frac{1}{2}$
E	113	18	0
Remainder			$\frac{1}{2}$
	£987	16	5 $\frac{3}{4}$

Remainders.

15558932
3990306
29179458
1041060
10143186

29956471) 59912942 (2 grs.
59912942

0



Miscellaneous Arithmetic :

OR A FULL

ACCOUNT of the NEW CALENDAR, &c.

PART VI.

OBSERVATIONS on the WEATHER,

Taken from the

Reverend Mr. P O I N T E R, and the
Shepherd of *Banbury*, &c.

Whereby any Person may judge, near the Time, what
Changes of Weather are approaching.

1. By the S U N.

1. * * * * * F the Sun, at his Rising, looks fair and clear,
* * * * * it denotes a fair Day, but if yellow, red, or
* I * * * * * deadish, the Air is thickening; and there will
* * * * * be foul Weather.

2. When the Sun Beams are red and short
at the Rising, Rain proceeds.

3. When Clouds or Mists make a Circle about the Sun, by
how much the greater the Circle is, by so much the greater
will be the Tempest; and if there be two Circles, the Tem-
pest will still be the greater.

4. If the Sun sets red, it denotes the next to be a fair Day.

5. If the Sun shines uncommonly warm in the Winter, it
threatens Rain; and so much the sooner, by how much the
nearer such warm Weather happens to the Winter Solstice.

2. By

2. By the M O O N.

1. If the Clouds or Mist make a Circle about the Moon, by how much the greater the Circle is, by so much the greater will the Tempest be; and if there be two Circles the Tempest will still be the greater.

2. When the Moon riseth bright, and shines with a pure clear Colour, 'tis a Sign of fair Weather; if red, it signifies Wind; and if blackish, Rain.

3. If the Horns of the new Moon appear bright and sharp, they denote fair Weather, but if blunt otherwise.

3. By the C L O U D S.

1. Clouds that are lofty, and appearing white, like Fleeces of Wool, scattered in the Sky, are a Sign of fair Weather.

2. Clouds appearing like Rocks or Towers, signify great Rain.

3. If small Clouds grow bigger and bigger in an Hour or two, they signify a great deal of Rain.

4. If great Clouds separate, waste off, and grow smaller and smaller, this signifies fair Weather.

5. When Clouds rise in the West, they shew Rain.

6. If Clouds look red at the Sun-rise, there will be a very great Tempest.

7. If the Clouds are low at the Sun-set, and look with a brownish red, it shews Wind or Rain the succeeding Day.

8. If the Clouds are driven from the Sun-rising, and pass away to the West, it is a Sign of fair Weather.

9. When the Wind has been South two or three Days, either in Summer or Harvest, and it grows very hot, and you see the Clouds rise with great white Tops like Towers, as if one were upon the Top of another, and join'd together with black on the lower Side, there will be Thunder and Rain suddenly.

10. When Clouds pass in the Air pretty fast, there is Wind aloft; and though it be not perceivable at that Time below, it will be, in all Probability, shortly; and sometimes be attended with Rain. There is also foul Weather at Sea, in that Quarter from whence the Clouds came.

4. By the M I S T S.

1. If the Mists arise out of the Ponds and Rivers, and there vanish away (*i. e.* are either exhal'd or subside) they signify fair Weather.

2. But

2. But if from thence they are attracted to the Tops of Hills, 'tis like there will be Rain, either the same Day, or commonly within two or three Days.

3. If before Sun-rising it be a general Mist (both on the Hills and Vales) near the full Moon, it signifies fair Weather.

4. But if such a Mist be in the New of the Moon, it signifies Rain in the Old of the Moon; and in the Old of the Moon it signifies Rain in the New.

5. By the W I N D S.

1. It has been an Observation made by some that have been very curious Observers of the Weather for many Years, that in eight Years Time there is as much South and West Wind, as North and East Wind; and consequently as many wet Years as dry.

2. When the Wind turns to the North-East Point, and continues two Days without Rain, and turns not Southward the third Day, nor rains, then it is like to continue North-East for eight or nine Days without Rain, and then return into the South.

3. If the Wind turns out of the South to the North-East again, and continues in that Point without Rain for two Days, and turns not South the third Day, nor rains the third Day, it is like to continue North-East for two Months, or three for the most Part. The Wind will finish these Turns towards the North in three Weeks.

4. When the Wind has been in the North for two Months, or more, for the most Part, and comes to the South, usually there are three or four fair Days at first, and then the fourth or fifth Day comes Rain, or else the Wind turns North, and continues dry still.

5. If it returns to the South within a Day or two, without Rain, and turns Northward without Rain, and then returns to the South, the first or second Day, as before, two or three times together after this sort, then it is like to be in the South or South-West, two or three Months together, as it was in the North before. The Winds will finish these Turns in a Fortnight.

6. The South Wind brings Warmth in the Winter, and Heat in the Summer.

7. If it be fair Weather out of the South for a Week together (which is not usual) it is like to be a great Drought, when it has been a long Time of Rain out of the South before.

fore. Usually the Wind turns from the North to the South quietly without Rain, but comes back again into the North strong, and with Rain. The greatest Winds which blow down Houses and Trees, usually come from the turning of the Wind out of the South by the West into the North, which drives away Rain and clears the Air.

8. If two Clouds arise, with Thunder in them, the one on the one Side of you, and the other on the other, then beware and haste for Shelter. -

9. If you see a Cloud rise against the Wind, or Side Wind, when that Cloud comes up to you, the Wind will blow the same Way that the Cloud came; and the same Rule holds good of a clear Place, when all the other Part of the Sky is equally thick except one clear Edge near the Horizon.

10. When a Shower comes suddenly, 'tis like to be fair Weather again in the Space of Half an Hour, or an Hour; and when the Air grows thick by Degrees, and the Sun shines duller and duller, till it shines not at all, or the Moon or the Stars by Night, then it is like to rain six Hours usually.

11. If it begin to rain from the South, with a high Wind for two or three Hours, and the Wind falls, but the Rain continues, it is like to rain for twelve Hours or more, and does usually rain till a strong North Wind clears the Air. These long Rains seldom hold above twelve Hours, or happen above once a Year.

12. If it begins to rain an Hour or two before Sun-rising, it is like to be fair before Noon, and so continue that Day; but if the rain begins an Hour or two after Sun-rising, it is like to rain all that Day, except the Rain-bow be seen before it Rains.

6. By the SPRING and SUMMER.

If the last seven Days of *February*, and the first twenty Days of *March*, be for the most Part rainy, the Spring and Summer Quarters are like to be so too; and if the aforesaid Days should be dry, the Spring and Summer Quarters are like to be dry also.

7. By the WINTER.

1. If the latter End of *October* and Beginning of *November*, be for the most Part warm and rainy, then *January* and *February* are like to be frosty and cold, except after a very dry Summer.

2. If in *October* and *November* there be Snow and Frosts, then *January* and *February* are like to be open and mild.

ÆNIGMAS

Æ N I G M A S.

I.

I Am a Friend, and Enemy,
 A Blessing and a Curse;
 A Beauty and Deformity,
 I save Life, but what's worse,
 Take it away; am long and short
 Round, square, straight, crooked too,
 Smooth and uneven, hard and soft,
 Both hot and cold most true.
 In greatest Plenty, wanted most;
 Where useful, minded least;
 I to all Palates suit myself,
 Am sav'ry and want Taste:
 Of sweet and stinking Smell I am,
 Am strong and weak beside;
 Able to bear the greatest Weight,
 Yet can't a small Pin guide.
 I Matrimony can dissolve,
 At once please and displease;
 Absence and Presence, both implor'd,
 And give to Cook-maids Ease.
 Me Farmers curse, me Merchants use,
 I Want and Plenty bring;
 Both Antidote and Bane I prove,
 By me Men cry and sing.
 I kiss the fairest Ladies Lips,
 Assist them in their Dress;
 Am often their great Ornament,
 For which they my Name bless.
 One while I am subservient,
 At others I o'erbear;
 Both useful and destructive too,
 And I for nothing care.
 Death and a Med'cine I am both,
 Fluid and solid too;
 A Mountain high, a Valley deep
 And num'rous Offspring shew:
 Yet I to Children am a Foe;
 By me are Wonders wrought;
 A Plague to all Philosophers;
 A Theme for Poet's Thought.

The best of Music I improve,
Of Use in other Arts;
By me the best of Architects
Are valued for their Parts.

Solution.

'Tis only *Water* can do this,
Which useful and mischievous is. *Water*

II. T. D.

AS I once walk'd the *Essex* Road
Near to a charming Maid's Abode,
A Creature pass'd of such odd Look,
As none sees in Dame Nature's Book.
Three Heads, and twice as many Eyes
Although in Bulk of middling Size.
As many Eyes, so many Ears,
At once could have and not have Fears;
Could cry, and yet could shed no Tears. }
It had three Backs, distinct and right,
Could walk, and talk, and scold and fight,
Could reason, and yet nothing know
But these three small Words *Hey, Gee, Wo.*
Eight Legs of proper Form and good,
On th' right Side two, on th' left six stood:
Of such surprizing Frame and Make,
You might it into Piecemeals take;
And each Part be alive and sound,
Quite free from Pain, and free from Wound;
Then re-unite and make them one,
As in its pristine State was done:
Intirely of female Kind,
When sep'rate or together join'd.
Now Reader an Account me bring,
What was this three-back'd, six-eye'd, eight-legg'd thing

Solution.

Your monstrous *Beast* of middling Stature,
Not found in all the Book of Nature,
Is nothing else (nay, do not stare)
But two brisk *Girls* upon a *Mare*;
Which you might sep'rate without Pain,
And when so done, unite again.

I Hold

2 Girls upon a Mare

III. T. D.

I Hold the Good, I hold the Bad,
 Am never merry, never sad;
 One Mouth I have, oft, two or three,
 At which whole Hundreds enter me;
 And in my Bowels sometimes stay,
 Then out again they make their Way,
 And this repeat twice in the Day.
 When in my Body they are plac'd
 (Where, by the Way, I most am grac'd
 When greatest Numbers in me are,
 And enter me in Faith and Fear)
 There's sometimes Silence, often Noise,
 Like Men and Women, Girls and Boys;
 And now and then so very great,
 You'd think I'd burst at any Rate
 With very Pain, yet have no Grief,
 So stand in Need of no Relief.
 Now if you can to me declare
 What thing I am, and who they are
 That sometimes in my Bowels live,
 You shall a Sugar-plumb receive.

Solution.

Church. It is a *Church*, in which twice in the Day
 The People meet to hear God's Word and pray;
 At whose Doors, whensoever they enter in,
 Their Duty do and then come out again.

IV. T. D.

AH me! they little know my Weight
 Who're ign'rant of Affairs of State;
 But they alone who me do wear
 Can tell, I bring a deal of Care:
 'Tis true, my Make and Frame is such,
 As cause Mankind to 'dmire me much,
 Yet were I set on a weak Head,
 Small as I am, should crush it dead;
 And yet so light, howe'er renown'd,
 A Pin can bring me to the Ground.
 I am the Author of much Woe,
 Though nought at all I of it know.

I neither

I neither Sorrow feel, nor Joy;
 Nought can me please, nought can annoy.
 But I grant both; yet more of Pain
 Than Pleasure doth with me remain.
 Be that as 'twill, he knows it well,
 Whose own I am; and thence can tell,
 Who e'er's the Man that does me bear,
 Supports me with the utmost Care.

Solution.

Crown

When Kings are cloth'd in Robes of State,
 It is the *Crown* which makes them great;
 And whensoever they it wear,
 Are soon convinc'd 'tis lin'd with Care.

V.

WHEN living I the Living fed,
 I bear the Living now I'm dead;
 My Bulk is also very great:
 As is my Size, such is my Weight.
 Beside all this, I do declare
 Five Hundred Tons within me are,
 Of other Weight beside my own,
 Which is to many People known;
 To all which add the Rate I move,
 'Twill then a greater Wonder prove.
 I pass o'er Living with such Force,
 As will run down the swiftest Horse.
 Nay, more; two Hundred Miles a Day
 I often times do wing my Way,
 (For I have Wings to help me on),
 And yet, most strange to think upon,
 Great as my Weight is, and my Size
 (Which nobody I think denies)
 What me bears up's so very thin,
 It can't support the smallest Pin.

Solution.

Ship

A *Ship* in Bulk is very great,
 And consequently of great Weight;
 'Tis made of Oak, which once did yield
 Acorns for Swine before they're kill'd.
 Its Wings are *Sails*, with which't doth pass
 O'er Seas as clear as Chrystal Glass,
 Where living *Fishes* swim within,
 And where will sink the smallest Pin.

My

VI. T. D.

MY Head is one Way-very long,
And t'other very round ;
And when I speak, so strong's my Voice
'Twill drive you to the Ground.

My Tongue is longer of the two,
With which I sometimes sing ;
And when I do it in harsh Strains.
'Twill make your two Ears ring.

But when in softer pleasing Notes,
I do myself express,
I tickle then your pleased Ears,
And gently them address.

On one Side of my Head is plac'd,
Of swinging Size, an Ear ;
With a long Pendant fix'd thereto,
But yet I cannot hear.

And as at first I formed was,
So deaf I still remain ;
And what you say, nor know, nor care,
Tell (if you can) my Name.

Solution.

A Bell

Dear Jack, if you'd know,
'Tis the great *Bell* of *Bow*.

VII. T. D.

MY Head, which is round,
Oft runs on the Ground,
When I have got something to do ;
And tho' I've no Feet
(Yet I sometimes run fleet)
When I borrow two Legs to my two.

My Belly is square,
Wherein sometimes are
Such Things as many refuse ;
Yet tho' its oft empty,
It has often great Plenty
Of what Noblemen sometimes chuse.

But

But however it is,
 Mens Hands I oft kifs,
 When my kind Assistance they crave ;
 Yet when I've serv'd their Turn,
 At me they will spurn,
 Nor will from a Dunghill me save.

Solution.

A *Wheelbarrow* for many Ends conduces ;
 Sometimes for clean, but oft'ner dirty Uses.

*a Wheel-
barrow*

VIII.

WHoe'er, or what first gave me Birth,
 Or whether born upon the Earth,
 Or high in Air, it matters not,
 For I am born as soon as got ;
 And what's more strange (if you'll believe)
 As soon as e'er I Life receive,
 I'm then beginning to decay,
 And in five Seconds die away.
 So short's my Life, yet of such Force,
 I'm quicker than the swiftest Horse ;
 Yet neither Feet nor Wings have I,
 Wherewith to run, or help me fly ;
 And in my Passage I move on
 In various Lines till Life is gone :
 But in this quick and hasty Pace,
 At once I all the Compass trace,
 And fill the near surrounding Space,
 Go backward, forward, sideways too,
 And up and down, tho' not to View ;
 Strange to relate, but still 'tis true :
 And when I die, there's nothing found,
 Of me beneath or 'bove the Ground.
 Now tell my Name, I say no more,
 Whatever you of me explore.

}
}
}

Solution.

Sound, from what Place soe'er it moves,
 As from a Center moves in Lines direct ;
 Ten thousand times ten thousand told,
 It fills surrounding Space in this Respect.
 Is in its Passage very swift,
 And not unfrequently is very strong,
 Yet soon as 't's born begins to die ;
 Its Life is sometimes scarce five Seconds long.

Sound

I am

IX.

I Am the best of things below,
 Yet often tossed to and fro
 As nothing worth ; and yet declare
 (Tho' variously I do appear)
 To th' World the best Advice I give,
 And tell Mankind how they should live ;
 If they do well shall go to Heaven,
 Where ev'ry Sin shall be forgiven ;
 But if th' reverse, they then must dwell,
 O sad ! for evermore in Hell.
 Yet notwithstanding my Advice,
 Which some think not so wise as nice,
 I'm often kick'd by Boys, and cufft,
 And for my good Turns sometimes hufft.
 In many Places I am found,
 And always give Advice that's sound
 But what's remarkable in me,
 I know no Joy nor Misery :
 And tho' I never did amiss,
 Insensible of Happiness.
 I sometimes Limb from Limb am torn,
 Yet feel no Pain to make me mourn ;
 But ever to my greatest Foes,
 I do eternal Light disclose.

God's Word

Solution.

'Tis *God's* Word which does Sin oppose.

X.

WHEN Sol's bright Rays no more Men cheer
 In this their upper Hemisphere,
 Then I take Place, to let them see
 How useful I to them can be.
 By me assisted they are pleas'd,
 But taken from them, vex'd and teaz'd ;
 The Fair oft place me near their Eyes
 Without Reserve, without disguise,
 And thankful for my Service are,
 Which they'll at any Time declare.
 Whenever I am standing by,
 There's Joy in ev'ry Maiden's Eye,

But

But when removed out of Sight,
On ev'ry Eye sits dismal Night.

Solution.

A pleasing Sight
In Time of Night
Is *Candle-light*.

} *Candle-light.*

XI.

BAD Tenants seldom pay their Rent,
They're ticklish Chaps, on Mischief bent.
'Tis wanton Harlots Youth beguile,
And strive to kill whene'er they smile:
But they, who tread in Virtue's Ways,
Will ever meet with good Men's Praise.
Will not to Lewdness be confin'd;
But will in Wedlock's Charms be join'd:
From ev'ry Vice yourself withdraw,
And always keep the sacred Law.
Learn Modesty; be just to all;
Whether them Friends or Foes you call.
Let Goodness, in a Word, yours be,
You shall be blest'd eternally.

Now from these Lines, in artful Frame,
The Author begs you'd tell her Name:
Look narrowly, you'll see the better,
And then you'll quickly find each Letter.

Solution.

Hannah Snellway

Your Christian-Name is *Hannah*, I can tell.
Your Sur-Name's *Snellway* too, I know it well.
I gain'd them by strict Search, and found the Letters,
Tho' pretty strongly bound in Leaden Fetters.

XII.

WHatever others of me think,
concerning what I eat or drink,
Yet while they waste their Time and Store,
Tho' I've no Means, I am not poor;
Nay I am rich, for all is mine
On which the Sun or Moon does shine.
Truly I eat of Herbage green,
In Summer-time while it is seen;

And

And tho' I oft abroad do roam,
 Yet evermore I am at home.
 In Winter-time I am confin'd,
 And then my in-door Business mind;
 But soon as Summer comes again,
 Abroad I go, but still remain
 At home as I before observ'd,
 Where constantly my Health's preserv'd.
 Yet lest you should me disbelieve,
 Or think I want you to receive
 My Notions odd, this learn withal,
 That it is no Untruth at all,
 For me to go abroad, yet stay
 At home, the same Time all the Day.
 The Reason's plain, which if you'd know,
 I take my House where'er I go.

Solution.

Tho' *Snails* for Pasturage do roam,
 Yet they are evermore at home;
 And never from their Houses stray,
 But travel with them ev'ry Day.

Snails

XIII. T. D.

A Covering upon my Head I wear;
 No Part of Fish, nor Beast, nor Fowl, nor Hair;
 Nor yet of Reptile Kind I here declare. }
 Yet is the Produce of some living thing,
 As Witnesses great Number I can bring.
 Tho' when of it a Particle I see
 I call't a Hair, and with me all agree;
 How's this! when single we a Hair it call,
 But when compounded, something else cry all!
 With this a Cov'ring for my Pate is made,
 To guard 'gainst *Hym's* Cold, and from *Sol's* Heat to shade.

Solution.

In *India*, as sev'ral Trav'lers know,
 And *Turky* likewise, *Cotton Trees* do grow,
 Of these fine Cloth is made, call'd Callico.
 Of this too, *Caps* are made for you and me,
 To save our Pates from th' Weather's Injury.

} *Caps*

UPON

XIV.

UPON a Thing that hath no Ears,
 Nor Legs, nor Eyes, so never hears;
 Nor walks, nor fees, I sit astride,
 And fearless without Saddle ride;
 Where I two Friends do much befriend,
 And when they doubt their Doubts I end.
 The Sexes both alike me use,
 Nor do I e'er my Help refuse,
 But evermore their Call obey,
 Whether it be by Night or Day.
 The Aged my Assistance crave,
 To whom I always well behave.
 The Younger sometimes, I confess,
 And fair ones too, do me caress;
 And place me near their pretty Eyes,
 For whom, perhaps, some Lover dies.
 But they to me no Pleasure give,
 And yet in Pain I never live.

Solution.

Spectacles Ah! Jenny, on thy lovely Nose,
 Sits something, which I will suppose
 Suits well with those two Friends your Eyes,
 For which, though your dear Collin dies,
 It argues still a Sight that's bad,
 Or Spectacles you'd not have had.

XV. T. D.

COME tell me, Sinner, who am I?
 For with my Weapon you shall die.
 Prepare to give Account with Speed,
 What Sort of Life you late did lead.
 How much you Violence have us'd;
 And how your precious Time abus'd;
 How oft you had more Gods than one,
 When you should worship God alone:
 How often took his Name in vain,
 And did too oft his Day prophane.
 Your Parents too, have disobey'd,
 And their Hearts ake have often made,
 How often stole what wa'n't your own,
 And too too often Harlots known:

Against

Against your Neighbour Slanders born,
And from his Body his Soul torn ;
Or otherwise him us'd amiss,
And coveted all that was his.
I say prepare Account to give,
How you upon the Earth did live ;
If well, 'tis well ; if not 'tis bad ;
And then your Lot will be most sad.
Now let this single Stroke of mine,
Your Soul and Body quite disjoin,
'Tis done — and now the Soul must go,
To endless Bliss or endless Woe.

Solution.

Whoever lives here as he ought,
Shall dwell with *Christ*, who hath him bought ;
And he who lives a Life in vain,
Will meet with everlasting Pain :
In either Case, for Bliss or Wo,
By *Death* Man one of them shall know.

XVI.

WHate'er my Bowels do contain,
They clothe the Fair, 'tis very plain ;
With which they do appear each Day,
Delightful, pleasant, blithe, and gay,
And though in *England* I am fed,
In *Italy* I'm better bred ;
Because my Food's more plenty there,
And they of me more careful are :
My Diet is of Leaves of Trees,
Which me from Hunger daily frees ;
And when my Time of Eating's o'er,
I leave off quite, and ne'er eat more.
'Tis then I turn my Inside out
For Men to tug and pull about ;
This Way and that, as they see fit,
That they in shining Robes may sit.
When this is done, I change t'a Fly,
Increase my Species, and then die.

Solution.

The *Silk-worm*, though of creeping Kind,
Is in its Produce none behind.
Hence from the Reptile World, we see
How is deriv'd our Finery.

K

I Have

Silk Worm

XVII.

I Have two Bodies join'd in one,
 And stand still, when alone I run.
 Strange to relate, but yet 'tis true,
 At once to stand and run with me's not new:
 But if with philosophic Eye,
 You view me, then it is that I
 Declare Life's short, and you must die. }
 'Tis true, when I my Race have run,
 Directly 'tis again begun;
 And four and twenty times a Day.
 My Life begins, and wears away:
 Thus by successive Turns I live,
 And by the same my Death receive.
 But if through Carelessness I fall,
 'Tis then my Death comes once for all:
 And tho' I've often liv'd before,
 I then shall die ne'er to live more.

Solution.

How our frail Life is daily spun,
Hours-glass Time shews us as the *Hours* run
 In's brittle *Glass*; which if destroy'd,
 It's Life's extinct, and made quite void.

XVIII. T. D.

AH! what is that black thing I see;
 I hope it is not made for me.
 Hear what it says in silent Strains:
 ' Ye Mortals bring me your Remains:
 ' Go quit your Carcasses of Clay;
 ' And in my Bowels let them lay:
 ' In me most sweet Repose you'll find,
 ' Howe'er the World may prove unkind:
 ' Here th' injured Man is free from Strife;
 ' And all the vexing Cares of Life:
 ' The weary'd Traveller rests here,
 ' Secure from Pain, and from all Fear.
 ' My Aspect may some Dread create;
 ' It will, where Men repent too late:
 ' But whosoever here lives well,
 ' Hereafter shall in Heaven dwell.'
 Now Reader, if this thing you've seen,
 You sure can tell what 'tis I mean.

Solution.

Solution.

Whenever Men depart this Life,
 Their Souls directly go
 To Happiness, that knows no End;
 Or else to endless Woe.
 Each Body's in a *Coffin* laid,
 Devoid of Pain and Grief,
 And as it then can't be oppress'd,
 It cannot want Relief.

XIX.

WHEN first I in this World was seen,
 I was, as if I had not been.
 No Sign of Sense in me appear'd,
 Could make no Noise, so not be heard.
 To walk or stand could not abide,
 But ever lie upon my Side;
 Or roll about from Place to Place,
 Yet none my Path could ever trace.
 Strange it may seem, yet it is true,
 That I had Mothers, Number two:
 And both, when cloth'd in best Array,
 Not worth Five Shillings I dare say.
 Twice was I born, yet second Birth,
 Gave Date to all my seeming Mirth:
 Seeming indeed, for you must know,
 I all my Life in fear do go,
 And from the Hand that draws the Knife,
 Would gladly run to save my Life;
 But Fate decrees I must be kill'd,
 That her own Law may be fulfill'd:
 And tho' I never Sin did know,
 Yet to the Fire I must go.

Solution.

Your Riddle's nothing but an *Egg*,
 Which rolls because it wants a Leg.
 It had a first and second Mother;
 An Egg by the first, a Chicken t'other;
 And both together very dear
 Of two Half Crowns, I do declare:
 And when alive are good for Nought,
 But best when to the Fire brought.

XX.

NO Fault I ever did commit,
 Yet am severely beat;
 And whensoever I do good,
 Am treated like a Cheat.
 Whenever I upright do stand,
 'Tis then I sleep the best;
 And when in soundest Sleep I am,
 Then I am least at rest.
 In swiftest Motion when I'm put,
 I like a Stock stand still;
 Run when I stand, and standing run,
 To 'bey my Master's Will.
 And when I run, so swift I am,
 You cannot see me move;
 Strange to relate, but 'tis as true,
 As *Dick* sweet *Nell* does love.

Solution.

A *Scourge Top* when 'tis fast asleep,
 In swiftest Motion then does keep;
 And when with strongest *Thongs* 'tis bound,
 Runs constantly a certain Round,
 At once it *sleeps, runs* and *stands* still,
 And so obeys its Master's Will.

R E B U S S E S.

I.

WHAT's dreaded by a Man with Cares oppress'd,
 And where a Beast enjoys his Food and Rest;
 These join'd together, you must surely own,
 Will make the Name of an old *Engliss* Town.

Solution.

A *Barn* all Men distressed dread;
 And Beasts are to a *Stable* led:
 And when you these together take,
 They will the Word *Barn-stable* make.

II.

WHAT covers your Head, and produces your Corn,
 Is the Name of a Town where my *Chloe* was born.

Solution.

Solntion.

A *Hat* on my Head, and in my *Field Corn*,
Make *Hatfield*, the Town where your *Chloë* was born.

III.

BELOW my Mouth, and on my Face,
There something is which has a Place;
What it is call'd, I will not tell,
Because I'm sure you know it well:
This join'd with v turn'd upside down,
Denotes a Place of great Renown.

Solution.

It is CHIN-A, my Dear,
Where you came from last Year.

IV. T. D.

WHAT do you call it, Not to have
Life's Comforts? tell me, *Jack*, I crave.
Suppose to fourscore Years I live?
What's that? a just Account me give.
Now if you join these two aright,
At any Time before 'tis Night,
They'll shew the Place where I must dine
Next *Tuesday*, and get drunk with Wine.

Solution.

He who Life's Comforts don't enjoy,
Most surely lives in *Want*;
And who to fourscore Years arrives,
All must old *Age* it grant.
Now thus I these together join,
And tell where you'll get drunk with Wine,
At *Wantage* 'tis you filthy Swine. }

V. T. D.

WHenever you my Pate do view,
Quite free from any Hair,
You then me something call, 'tis true,
But what I'll not declare:
This join with something which you drink,
'Tis either red or white,
Then the last Letter quite expunge,
Now tell my Name at Sight.

K 3

Solution.

Solution.

The Man that is *Bald*, to be sure has no Hair ;
 And he, who drinks *Wine*, sits void of all Care :
 These two Words then join ; and then you will see,
 That *Baldwin* they make, by rejecting the e.

VI.

THERE is a Fowl, which I have seen,
 Were't here, 'twould tell where I have been,
 Because you then would know its Name,
 And so declare from whence I came.
 It's Male is often very proud,
 And then it chatters very loud :
 Tho' large, no Spirit has t' engage,
 A little Cock of Half its Age :
 But cowardly away does run,
 E'er it a Battle has begun.
 I think I've said enough to tell,
 Where once I formerly did dwell.

Solution.

A *Turkey* Cock is very proud !
 And Coward like, is very loud.

VII.

THERE nothing is, as I am told,
 But something is before 'tis old ;
 And many Things that have been lost,
 Have never to the Owner's Cost,
 Been — What d'ye call't ? and brought again,
 Which much increas'd the Owner's Pain.
 Sailors, when they are on the Main,
 And nothing them does entertain,
 But Water, and some threat'ning Clouds,
 Delight not in those rough Abodes ;
 But eagerly, and sometimes pant,
 Look out for what they wish and want.
 Now these together join and tell,
 Where live my Sisters, *Sue* and *Nell*.

Solution.

'Tis *New-found-land*, your Sisters *Nell*
 And *Sue* do live, I know it well.

Whatever

VIII.

WHatever's opposite to Light,
Is mostly seen at Ten at Night:
Then Participle's three last Letters
Of th' present Tense, though you have Fetters,
If duly join'd you'll then discover
Where lives *Susanna* my dear Lover.

Solution.

'Tis *Dark-ing* where my *Suke* does live,
I wish she would her Heart me give.

IX.

DEATH something has in's Hand depend on't,
Which has a sharp thing at the End on't,
With which, if once he does you strike,
You'll say, you never felt the like:
And on the Face 'tween Nose and Chin,
There's something to put something in:
Now if these two you rightly join,
You have the Place where's sold good Wine.

Solution.

'Tis *Dart-mouth* where good Wine is sold,
As I have more than once been told.

X. T. D.

WHAT is it grows like Wheat as high?
Come tell me now, or by and by:
And what d'ye call that five barr'd Thing,
That does in Fields on Hinges swing?
These two, when well together join'd,
Will make an inland Town you'll find.

Solution.

I think the Thing that grows as high
As Wheat, is nothing else but *Rye*:
And when in th' Fields a Gate does swing,
It tells me that's the other Thing:
And when I see these rightly join'd,
Of *Ryegate* then they me remind.

N. B. This is a Market Town in *Surry*, by some called
Ryegate.

XI. T. D.

A Maiden has another Name,
 While she, unmarried bears no blame.
 And the third Vowel, People say,
 Is — Oh! I dare not tell to Day:
 And the first Vowel is well known
 To be — I must not speak I own:
 But this I'll tell, nor be afraid,
 They'll shew where good Tobacco's made,
 If they're together rightly join'd,
 As you, by Art may quickly find.

Solution.

A *Virgin* is another Name,
 For Maidens while they're void of Blame.
 I's the third Vowel, *a* the first;
 And if they be but rightly nurst,
 They'll make *Virginia*, where you know,
 The choicest smoaking Herb does grow.

XII.

A Lion lodges somewhere, I know well,
 But what you call the Place, now I'll not tell.
 Archers (mind what I say) or miss or hit,
 But what it is, let this employ your Wit.
 Now if these two you join, as I am told,
 They'll shew a Place where th' Winter's very cold.

Solution.

A Lion lodges in a *Den*,
 Archers the *Mark* do hit;
 And *Denmark* is the Place you mean,
 Or I have lost my Wit.

XIII.

WHERE's Silver, Gold, and Copper bred?
 And where that Metal called Lead?
 And what do Mankind ever wear
 Upon their Shoulders? quick declare.
 These two join'd nicely, straight will shew,
 Where lives

Your Servant,

Richard Doe.

Solution.

Solution.

Gold, Silver, Copper, Iron, Lead,
Each in it's Mine, are ever bred ;
And when you see Dick Doe, beware
That your Head your own Shoulders bear.
Now these two put together tell,
At Minehead, Dick, all Things go well.

An Epitaph.

J. O.

Hnan DJ oAnLi ebu Ri Edh ERE

W. H. owH ENal Ive

T. H.

Oug Htth EYco UL Dth Rive

W. I.

Thno Ughtb Uthu Mmin Gbe Er.

This, and the following are design'd for the Learner to
put them into proper Words.

Matt. v. 29, 30.

I.

Fth yri gHte yeo ffe ndth eep lu ckit ou
tAN dCaS tiT fRO mth EE fO ri tisp

R O F I

taBL efo rth EE tha Ton Eoft hy

M. E. M.

Be Rssh Oul Dp eR IsHa NDh oTt
Hat Th Ywho Leb OdY Sho UL Dbec

Asti NtoH El L

A. N.

Dift hyr ighth an Doff endth EE cu titO
FFa nd ca sti tfro Mthe EF ori tisp RO

Fita BL efo Rth EE tha ton eoft HY

McMb ERss HouL D peri SHan Dno

ttha Tth Ywho Lebo Dysh Oul Dbeca

stin Tohe L. L.

The Character of a Christian in *Paradoxes*.

1. **A** Christian is one, who *believes* things, which his Reason cannot comprehend. Who hopes for that, which neither he nor any Man alive ever saw. And who *labours* for that, which he knows he can never attain.

Solution. A Christian believes the *Trinity in Unity*, and *Unity in Trinity*, which his Reason cannot comprehend. He hopes to be received into the Kingdom of *Heaven*, which he, nor any Man alive, ever saw. And he labours after *Perfection*, yet knows, at the same Time, that he can never attain to it.

2. He believes a Virgin to have been a Mother, and her own Son to be her Maker.

Solution. This is meant only of the Virgin *Mary*, of whom our Saviour was born: and as he was God; so also was he her *Maker*.

3. A Christian believes *him* to have been a weak Child, carried in Arms, who is the *Almighty*; and *him* to have died, who only hath Life and Immortality in himself.

Solution. Our Saviour, whilst he was in the Flesh, was that weak Child; and he, as *Man*, died upon the Cross; but as *God*, has only Life and Immortality in himself.

4. He believes the God of all Grace, to have been angry with one, who never offended him; and the God that hates all Sin, to be reconciled to himself, though sinning continually, and never making, or being able to make him Satisfaction.

Solution. The only begotten Son of *God* took upon him the Sins of the whole World, and endured that Wrath of *God* which was due to Mankind only for their Disobedience: And in this Sense it is to be understood that *God* was angry with his Son, who never offended him; and therefore *God* Almighty will always be reconciled to the repenting Sinner; though he is not able to make Satisfaction, since Christ did it for him.

5. He dares not justify himself, even in those things wherein he knows no Fault in himself, yet he believes *God* accepts those Services, wherein himself is able to find many Faults.

Solution. In the Sight of *God* no Flesh can be justified; and if he charges his Angels with Folly, who have no Sin, how much more Man, who is nothing else but Sin? But yet if a Man has these two great Articles, *Faith* and *Repentance*, he rests

rests satisfied that *God* will accept his weak Services, they being his best; though when he has offered them up, he can, by looking back, discover the Errors he committed at the Time that he offered them.

6. He is the most lowly minded, yet the greatest Aspirer; most contented, yet ever craving.

Solution. When a Christian compares himself with *God*, if I may use the Expression, he has great Reason to be lowly minded, because of the immense Difference between them; notwithstanding which he is the greatest Aspirer, because he aims at things which the Heart of Man is not able to conceive for their inestimable Value. And inasmuch as he puts his full Trust in *God*, joined with his own best Endeavours to live a good Life, he is contented let what will befall him in this World. He is ever *craving*, 'tis true; but it is *Pardon* for his past Offences, and *Grace* to lead a new and better Life for the Time to come; both which he will petition for with the strongest Desire all the Days of his Life.

7. He loses his Life and gains by it, and even while he loses it, he saves it.

Solution. When a true Christian departs this Life, whether it be by *Famine*, *Pestilence*, *Fire*, or *Sword*, a natural or violent Death, he goes into the Regions of Bliss, consequently he must gain by it, because the Happiness of the World to come, is superlatively greater than any this World can afford: Such a Christian may also very justly be said to *save his Life*, by *losing it*; since he only loses it in this World to *save it* from eternal Destruction, and find it in the Kingdom of Heaven. A happy Loss.

8. He denies himself often; yet no Man, that most pleases himself, loves himself so well.

Solution. A true Christian *fasts* as well as prays; and he who fasts denies himself; and herein he may be said to love himself, because he has Heaven in view; and not only love himself, but *better*, than he who pleases himself: For he, who pleases himself, looks no farther than this Life, not regarding how it shall fare with him in the World to come; while he, who denies himself here, does it to obtain a happy Eternity. And as the smallest Share of Happiness in Heaven is infinitely larger than the greatest upon Earth; so he who denies himself the Pleasures of this Life to gain a better, most certainly loves himself better than he who denies himself nothing that this World can afford, and takes no Care to save his Soul.

9. He

9. He is the most reproached of all Men living; and yet at the same Time, no Man is so highly honoured.

Solution. The best Christians are generally most reproached for their daring to be good; and this is the Work of the Devil, who endeavours to destroy all Goodness; but whenever they are thus reproached by Men, they are then most honoured by God for being so, which is the greatest Honour.

10. The more Injury his Enemies do to him, the more Advantage he gets by them.

Solution. Because, while he suffers for Christ's Sake, he is sure to gain *Heaven* by it, which is the greatest of all *Blessings*.

11. He is a Peace-Maker; yet continually fighting, and an irreconcilable Enemy.

Solution. When Men are at Variance, he will endeavour to make up the Difference, and set them at Unity: but he himself is continually fighting against his three grand Enemies, the *Devil*, the *World*, and the *Flesh*; and is an irreconcilable Enemy to them, lest they should overcome him and bring him to eternal Destruction.

12. He believes the Angels to be more excellent Creatures than himself, and yet counts them his Servants. He believes he receives many good Turns by their Means, yet he never prays their Assistance, nor craves their Prayers, nor offers them Thanks, which yet he doth not disdain to do to the meanest Christian.

Solution. The Angels are not only more excellent Creatures than Men, but minister also to their spiritual Wants; hence they are our Servants. And although we do receive many good Turns, by their Means, they being our constant Attendants, yet it is not lawful to pray to them, nor crave their Prayers; neither may we thank them for their good Offices, because they are commanded of God, to whom alone our Thanks are due.

13. He knows he shall not be saved by his Works, and yet doth all the good Works that he can, and believes he shall not be saved without them.

Solution. Good Works alone will never save a Man; and it is as certain that without them he cannot be saved. *Faith* therefore must be joined with *Works*, and by them both, a Christian stands a fair Chance of being made an Inheritor of the Kingdom of Heaven.

14. He prays with all his Heart not to be led into Temptation, yet rejoices when he is fallen into it.

Solution.

Solution. A Christian prays that he may not be led into *Temptation*, for fear he should fall therein; but when he is *tempted* and falls not by the *Temptation*, he has great Reason to rejoice and be thankful to God for supporting him under it.

15. He believes his Prayers to be heard, even when they are denied, and gives Thanks for that which he prayed against.

Solution. The best of Christians are but short-sighted Creatures, and therefore cannot so well tell what is good for them, as he, who knows all things can; Hence allowing God to know better than themselves, they are contented if they are denied the thing which they prayed for; imagining, if they had it, it would be worse for them. And as Men pray against Afflictions of all Kinds, yet when they are sent for our good, we ought to be thankful, and say with *David*, *It is good for me to be afflicted, that I may learn thy Commandments.*

16. He is a *Serpent* and a *Dove*; a *Lamb* and a *Lion*; a *Reed* and a *Cedar*.

Solution. He is as wise as a *Serpent* to be hurt by nobody, and as harmless as a *Dove* to hurt nobody himself: In his suffering for Sin, or for the Cause of *Christ*, he is as patient as a *Lamb*, but in opposing *Sin*, he has the Courage of a *Lion*. In the common Calamities of Life, he is like a *Reed*, frequently shaken, and often born almost quite down; but against the Storms and Tempests of *Satan* and his wicked Suggestions, he stands firm like the *Cedar*, which is not easily shaken.

17. He lives invisibly to those that see him; and those who know him best, do but guess at him: Yet they sometimes see farther into him, and judge more truly of him than he doth of himself.

Solution. A true Christian retires frequently into himself, and thence too often finds just Reason to accuse and condemn himself, but then it puts him upon his Guard, and makes him more watchful for the Time to come, and thus he lives *invisibly* to all others. Hence as he declares nothing of all this to the World, they who know him best do but *guess* at him; and as the good Christian has always a mean Opinion of himself, knowing he is not so good as he ought to be, and is rather inclined to condemn than acquit himself: So they who are best acquainted with him, and know that he has led as good a Life as human Frailty would admit of, always and with good Reason acquit him; and hence it may very
justly

justly be said, that *they sometimes see further into him, and judge more truly of him, than he doth of himself.*

18. He believes in one *Nature three Persons*, and in one *Person two Natures.*

Solution. God the *Father*, God the *Son*, and God the *Holy Ghost*, though three distinct Persons, make but one God, who is an eternal Spirit, therefore of one *Nature*; yet the second Person in the sacred *Trinity*, taking *Flesh* upon him, may very justly be said to have two *Natures*, *viz.* those of *God* and *Man*.

19. He believes the most just God to have punished a most innocent Person, and to have justified himself though a most ungodly Sinner.

Solution. The whole Race of *Adam* being involved in Sin, deserved, most justly, the Wrath of God; but as the second Person in the most divine Trinity purposed from all Eternity to redeem Mankind; so by dying for them, he is said to have been *punished*: And as the best Christian, by Birth and also by Action is continually sinning; yet by true Repentance, and Faith in *Christ*, he is *justified* by God, though he confesses himself the worst of Sinners.

20. He is the most temperate of all Men, yet fares most deliciously.

Solution. For while he is indifferent about, and sits loose to all earthly Comforts, in which his Temperance consists, he enjoys *Peace of Mind* and a good *Conscience*, which give him more real Pleasures than all that this World can afford.

Promiscuous

Promiscuous Questions, both Arithmetical and of Pleasantry.

1. **F**ULL three times Ten, and four times Nine,
Twice five times Eight and Seven;
What do they make, with nine times Six,
Thrice eight times Twelve and Leven? *Ans. 506.*

2. The Account of a certain Cathedral is as follows, *viz.*
As many Days as in one Year there be,
So many Windows in one Church we see:
As many Marble Pillars there appear,
As there are Hours throughout the fleeting Year:
As many Gates as Moons one Year doth view:
Strange Tale to tell, yet not more strange than true.
What Church is it? How many Windows, Pillars and
Gates had it? And give the Sum of them all together.

Solution.

Windows	365	=	as many Days	} <i>Salisbury Cathedral.</i>
Pillars	8760	=	Hours	
Gates	13	=	Moons	

9143

3. Suppose ten Half-pence to be placed in a right Line;
I demand how they may be doubled, when any one single
Half-penny, shall cover the third distant from it?

Solution.

1	2	3	4	5	6	7	8	9	10	<i>Indices.</i>
o	o	o	o	o	o	o	o	o	o	<i>Half-pence.</i>

1st, Thus,

1	2	3	4	5	6	7	8	9	10	
o	o	o	o	o	o		o	o	8	<i>7th covereth 10th.</i>

2d Thus,

1	2	3	4	5	6	7	8	9	10	
o	8	o	o		o		o	o	8	<i>5th covereth 2d.</i>

3d, Thus,

1	2	3	4	5	6	7	8	9	10	
o	8		o		o		8	o	8	<i>3d covereth 8th.</i>

4th, Thus,

1	2	3	4	5	6	7	8	9	10	
	8		o		8		8	o	8	<i>1st covereth 6th.</i>

5th, Thus,

1	2	3	4	5	6	7	8	9	10	
	8		8		8		8		8	<i>9th covereth 4th.</i>

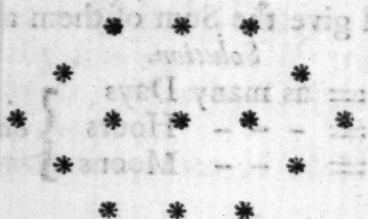
4. My

14. My Water-Tub holds 80 Gallons, when full; but being faulty at the Bottom, is continually dropping; now admit that it drops once in a Second of Time, and that 100 such Drops would fill Half a Quarter of a Pint; in what Time would it be empty?

Solution. In 80 Gallons are 5120 Half Quarters of Pints, and those multiplied by 100 give so many Drops, equal to as many Seconds; which reduced into higher Terms, give 5 Days, 22 Hours, 13 Minutes, 20 Seconds; and so long would the Water in the said Tub be dropping out.

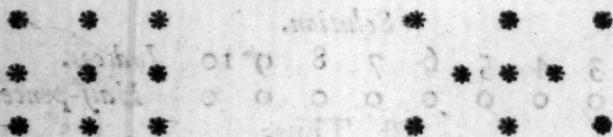
5. Place 15 Trees in such Manner, that there may be 15 Rows, containing 3 Trees in a Row; and 1 Row more, consisting of 5 Trees, without destroying the Order of the other 15 Rows.

Solution.

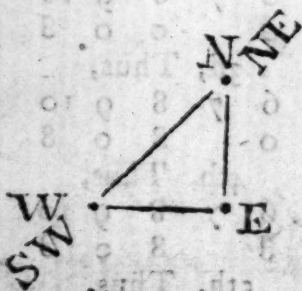


6. Place 9 Trees in such Manner that they may make 8 Rows, at 3 Trees in each Row.

Solution.



7. Let 3 Points be placed in such Sort, that 2 may stand East and West; 2 North and South, and 2 North-East and South-West.



8. I have seen a Torrent of Water run down the Kennel in *Tower-street* with some Rapidity : Now admit a Cork, put in at a certain Place, should move a Yard and Half in Half a Second of Time, how far would it run in an Hour, supposing its Motion to be continued with the same Force ;

$$\frac{1}{2} \text{ Sec. } \frac{1}{2} \text{ Ft. } \frac{1}{2} \text{ Sec.}$$

$$1 : 9 :: 7200 : 6 \text{ Miles, } 1 \text{ Furlong, } 20 \text{ Yds.}$$

9. A Ship is freighted for *London* with 30540 Pipe-Staves, and 6780 Hoghead-Staves, at 7*l.* 5*s.* per Thousand Pipe-Staves : I demand what the Freight comes to, accounting 3 Hoghead-Staves to be equal to 2 Pipe-Staves ?

$$\text{hhd.St. P.St. hhd.St. P.St.}$$

$$3 : 2 :: 6780 : 4520$$

$$30540 + 4520 = 35060 \text{ Pi. St.}$$

$$1000 : 7\text{l. } 5\text{s.} :: 35060 : 254\text{l. } 2\text{s. } 3\text{d.}$$

10. *B*, according to the Currency of his Country, lets *A*, who lives in another Country, know that he owes him 93*l.* 5*s.* 6*d.* and *A* in return, according to the Currency of his Place, pays him 66*l.* 12*s.* 6*d.* by which Means the Debt is discharged without any Abatement : The Question is, what is 100*l.* of *A*'s Mony worth in *B*'s Currency ?

A			B			A			B		
<i>l.</i>	<i>s.</i>	<i>d.</i>	<i>l.</i>	<i>s.</i>	<i>d.</i>	<i>l.</i>	<i>s.</i>	<i>d.</i>	<i>l.</i>	<i>s.</i>	<i>d.</i>
66	12	6	:	93	5	6	:	100	:	140	

11. If 100*l.* in one Place are equal to 140*l.* in another, what is the Proportion in its lowest Terms ?

$$2) \frac{100}{140} (\frac{5}{7} \text{ Answ. } \frac{5}{7})$$

$$\text{For as } 100 : 140 \text{ or as } 10 : 14 :: 5 : 7$$

Hence appears the short Way, that Merchants have of computing how much Mony of one Country is equal to that of another, provided the Rate *per Cent.* is first known. Now let it be granted, that

12. *A* and *B* are Merchants residing at distant Places, and 100*l.* of *A*'s Currency are equal to 140*l.* of *B*'s Currency ; what must *A* pay to *B* to clear a Debt of 1000*l.* 19*s.* 4*d.* ?

B		A		B		A	
<i>l.</i>	<i>l.</i>	<i>l.</i>	<i>s.</i>	<i>d.</i>	<i>l.</i>	<i>s.</i>	<i>d.</i>
140	:	100	:	:	1000	19	4

$$714 \text{ } 19 \text{ } 6 \text{ } 1 \frac{48}{336} = \frac{1}{7}$$

Thus abbreviated.

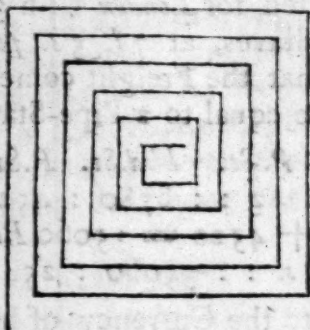
$$7 : 5 :: 1000 \text{ } 19 \text{ } 4 : 714 \text{ } 19 \text{ } 6 \text{ } 1 \frac{1}{7}$$

And

And this Proportion of 7 to 5 one Way, or of 5 to 7 the other Way, being once known, a Multiplier and Divisor are always ready for the speedy reducing the Mony of one Country into the Mony of another.

13. There is a Piece of Paper, which is just 12 Inches square; I would have 12 Yards taken from it, all in one Piece, whose Width shall be a Quarter of an Inch.

Solution. It must be cut Spiral-wise as hereunder.



14. A Man went to *Billingsgate*, and bought a Pack of *Miton* Oyfters, for 3 Shillings: When he came Home, he told them out, and found their Number to be 199, which were, one with another, about eleven for Two-pence: Now admit these Oyfters were divided into three Sorts, *viz.* large 48, middling 66, and small 85, and the largest to be sold at 3 for Two-pence, the middling at a Halfpenny a piece, and the small at 3 for a Penny, what would be the Gain? *Ans.* 4s. 9d. and an Oyfter over.

15. Some Fishermen having been a fishing, and caught nothing, sat down to louse themselves: A Man coming by, asked them what Success they had; to which they answered, What they caught they left behind them; and what they could not catch, they took away with them.

Solution. The Fishermen, as they could catch no Fish, meant Lice; which when they had taken and kill'd, they left behind them, by throwing them away; and what they could not catch they took away with them in their Clothes.

16. It is said by experienced Bankers and Gardeners, that a Bank of 7 Feet in Height, perpendicularly so, will require its Base or Bottom to be 10 Feet in Width: Now a Gardener having such a Bank, and being willing to save so much Ground, and have it planted, would, instead thereof, have a Row of Pales or Pallisadoes; but he is willing, first of all, to state the Expense one Way, and the Gain the other. The Length

Length of the Ground that was to be enclosed or paled was 160 Feet, and the Paling 7 Feet high; all which a Carpenter would do, and find the Materials, for 5 Shillings *per* Yard square, and level the Bank into the Bargain. Again, he considered the Quantity of Ground, thus saved, was not only 160 Feet long, as aforesaid, but 10 Feet broad; and that every square Foot would produce 5 Carrots, and those Carrots be sold at 2 for three Farthings: Now admitting all this; and that the Paling would stand 10 Years without Repair; what would he gain or lose at the End of the said Time?

1. $160 \times 7 = 1120 \text{ sq. Ft.} = 124 \frac{4}{9} \text{ sq. Yds.}$
2. $124 \frac{4}{9} \text{ at } 5s. = 31l. 0s. 6d. \frac{1}{2}$
3. $160 \times 10 \times 5 = 8000 \text{ Carrots}$
4. $2 \text{ Ca.} : 3 \text{ qrs.} :: 8000 \text{ Ca.} : 12l. 10s.$
5. $12l. 10s. \times 10 = 125l.$
6. $125 - 31 \text{ } 0 \text{ } 6\frac{1}{2} = 93l. 19s. 5d. \frac{1}{2} \text{ Gain.}$

17. A Butcher went to Market, and bought 20 Beasts for 20*l.* he had Oxen at 4*l.* a-piece, Calves at 1*s.* a-piece, and Sheep at 5*s.* a-piece: How many of each had he?

18. In the Parish-Church of *Tiverton* in *Devonshire*, lie buried *Edward Courtney* Earl of *Devonshire*, and his Countess, under their Effigies in Alabaster, with this Epitaph;

Ho, ho, who lies here?
 'Tis I the good Earl of *Devonshire*,
 With *Kate* my Wife, to me full dear.
 We lived together Fifty-five Year.
 That we spent, we had;
 That we left, we lost:
 That we gave, we have.

Solution. What Money the Earl and his Countess spent, they had something for it; thus they had what they spent. — What they left behind them when they died, was lost to them, because not disposed of to a good End. — What they gave, or disposed of to charitable Uses, was so much laid up in Store, to be received in the Kingdom of Heaven, which, 'tis hoped, fell to their Lot; thus what they gave, they have.

19. I have a Water-Tub, which contains 126 Wine Gallons: Now it happen'd on a rainy Day, that the Spout over it ran with so fine a Thread, that a Wine Pint could not be filled in less than 15 Minutes; I demand the Length of Time that

that the same Thread (supposing it to be continually running) would take up to fill the said Water-Tub? *Answ.* 1 Day, 12 Hours.

20. Says *Jack* to his Sisters, *Sue*, *Mary* and *Nan*,
You pretend to be Scholars; now tell if you can;
How many Plumbs have I? Some Help I will give,
But 'tis only what follows, nought else as I live:

I've the Half of Five Hundred; the Third of nine Score;
The Fourth of one Million; twelve Hundred and four;
With ten times nine Thousand; six Dozen and five;
And ninety-two Half Scores as I am alive.
Now if you can give me the Number with Speed,
You shall be rewarded, dear Sisters indeed.

Answ. 342509 Plumbs.

21. The new River, from its Beginning at *Ware*, to the great Reservoir or Basen at *Islington*, is judged to be about 60 Miles; and its Stream moves in such an equable Manner, that any thing cast into it, which will not sink, will move about 10 Feet in 6 Seconds of Time: How long will a Cork be in moving from the Beginning to the End of the said River, supposing that it had a free Passage all the Way, and no Grates or Locks to check or hinder its Course? Also at what Hour would it arrive there, admitting it to be cast in on *Monday* at Ten in the Morning? *Answ.* 2 Days, 4 Hours, 48 Minutes, or 48 Minutes past Two on *Wednesday* in the Afternoon.

<i>F.</i>	<i>Sec.</i>	<i>Miles.</i>	<i>Sec.</i>
10	:	6	:
:	:	:	:
60	:	1900	80

22. *Nancy*, one Day, playing with her Cat, by Accident broke a prodigious large China Punch-Bowl, which held nine Gallons and a Half, and had in it three Setts of the finest China, that could be procured, or that ever was seen, which were broke also, and which cost I know not how much. Her Mama was extremely angry with her, and chid her very severely for her great Carelessness; at which she fell upon her Knees, and with Tears said, Dear Mama, I will pay you for all the Damage, if you will not be angry with me. *Nancy*, says her Mama, because you did not break the China for the Purpose, though I gave a great many Pieces of Money for it, yet, after telling you how many and what those Pieces were, if you can tell me how much the Bowl cost, I will forgive you: If not, you must pay for it all. The several Pieces and their Number were as follows, viz.

14 Moidores

14 Moidores	100 Groats
12 Six and thirty Pieces	500 Sixpences
22 Five Pound Pieces	1000 Threepences
15 Three Pound Twelve Pieces	4000 Twopences
13 Two Guinea Pieces	10000 Silver Pennies
17 Guineas	10 Queen <i>Ann's</i> Farthings
19 Half Guineas	which cost me 40 Shillings and Six-pence a piece.
73 Crowns	How much did all the China cost?
107 Half Crowns	
419 Shillings	

Ans. 434*l.* 2*s.* 2*d.*

23. A thrifty Roper, once much Wealth did save,
And to his Daughter fair this Portion gave :
Fifty new Ropes, each Rope thrice twenty Foot ;
At each Yard's Distance was a firm ti'd knot ;
By ev'ry Knot hung thirty Purfes fixt ;
In ev'ry Purse were Crowns and Guineas mixt ;
To three bright Crowns, two Pieces of pure Gold :
What is her Fortune when together told ? *Ans.* 130500*l.*

24. How are four ones to be placed that they may make just 12 ?

25 I have a Hog, a Goat, a Cow,
With one fat Calf, two Pigs and Sow ;
All which, with one Ram and two Sheep,
Are full as much as I can keep.
'Tis true, they do afford to me,
My Wife, and all my Family,
Some Nourishment ; but that wont do,
For they must all to Market go,
And something get for all my Pain,
Or I shall bring them Home again.
The Profit I intend to make
(And nothing less for them I'll take)
Is, for my Hog three Shillings clear ;
And twice three for my Goat (not dear)
My Cow must gain one Pound and Crown ;
My Calf the same, or I'm undone.
And what I gain for my Dun Cow,
Two thirds must be for Pigs and Sow :
Then for my Ram and two good Sheep,
Five Crowns they clear, or I not sleep.
Now as they cost me forty Pounds,
When I them bought, with twice three Crowns,

What

What must I sell each for again,
The 'foresaid Profit to be ta'en?

Solution.

As the whole clear Gain
Is to the first Cost and Gain together;
So is the Gain made by each of the Beasts,
To the Sum which they must be sold for.

26. A Man bought 100 Oranges at 2 for a Penny, and 100 at 3 for a Penny, and sold them again at 5 for Two-pence: What was the Gain or Loss by the Sale thereof? *Answ* $3\frac{1}{3}d.$ Loss.

27. Divide 20 Shillings in such Manner that *A* may have $\frac{1}{3}$, *C* $\frac{1}{4}$, *D* $\frac{1}{5}$, and *E* $\frac{1}{6}$.

Note, In Questions of this Nature, when the several Parts are not equivalent to the whole Sum, whether they be more or less, the several Parts required must bear such Proportion to the given Parts, as the Sum of the given Parts does to the given Sum.

	s.	d.	qr.	
A	7	0	0	$\frac{192}{228}$
C	5	3	0	$\frac{144}{228}$
D	4	2	2	$\frac{24}{228}$
E	3	6	0	$\frac{96}{228}$
	20	0	0	

28. What Sum of Money is that, which being divided by 5, will give the Quotient in such Manner that the Pounds, Shillings and Pence shall be in arithmetical Progression whose common Difference is 1, and the Sum of those Numbers 18?

Note, There is nothing more in this Question, than to find three such Numbers in Pounds, Shillings and Pence, as make 18, which is very easy, and then multiply them by 5; the rest is purposely omitted.

29. What Sum of Money is that, which being divided by 2, the Pounds in the Quotient will be equal to the Shillings in the Dividend; and the Shillings in the Quotient, will be equal to the Pounds in the Dividend? *Answ.* 13l. 6s.

30. How many Heads, Legs, Eyes and Claws,
Has nineteen Score and ten Jack-Daws. *Answ.* 5070.

31. How many Deals of 12 Feet long, and 1 Inch and a Half thick, are equal to 500 Deals each 19 Feet long, and 2 Inches and three Quarters thick?

Solution.

Solution.

$$2\frac{3}{4} = .229 \text{ of a Foot.}$$

$$.229 \times 19 \times 500 = 2175.5 \text{ Feet solid}$$

$$1.5 = .125 \text{ of a Foot}$$

$$.125 \times 12 = 1.5 \text{ Foot solid in 1 Deal}$$

1.5) 2175.5 (1450 Deals of 12 Feet long, and 1 Inch and a Half thick, are equal to 500 Deals of 19 Feet long, and 2 Inches $\frac{3}{4}$ thick.

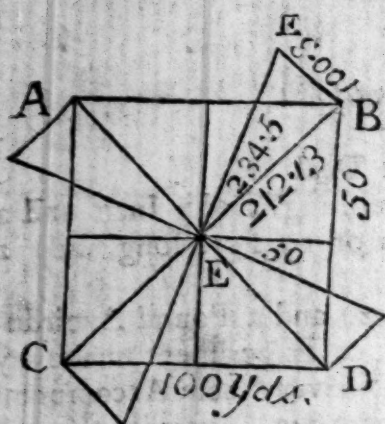
32. A Pound Troy contains 12 oz. and a Pound Avoirdupoise 16 oz. Now from a very nice Experiment made by the late Mr. John Ward, who was a very able Accomptant and Mathematician, it appears that 16 oz. Avoirdupoise are equal to 14 oz. 11 dwts. 15 grs. and $\frac{1}{2}$ Troy; what Weight Avoirdupoise is equal to 12 oz. Troy?

oz. dwts. gr. oz. oz. oz. dr. grs.

$$14 \quad 11 \quad 15\frac{1}{2} : 16 :: 12 : 13 \quad 2 \quad 2 \quad \frac{2322}{13099}$$

33. Says Jack to his Brother Ned, my Uncle William Greybeard has paid Nature's last Debt, and has left me his fine House and Garden: Now, Brother Ned! as the Garden is Quadrangular, I intend to build 4 Towers at the four Angles or Corners, each of which shall be 100 Feet high: The Distance between each Tower's Center, you know, will be 100 Yards. But (says Jack) because I would do something, that never was done yet, I intend to have 4 Ladders, all of a Length, that shall reach from the Center of the Garden to the Top of the Tower: Now, as I know very little of Arithmetic, and you are a very good Accomptant, Brother Ned, tell me what must be the Length of each Ladder.

Solution. Every large Square (as A B C D) is composed of four small Squares, each Side being just half of the Side of the given Square, viz. 50 Yards. The Center of the given Square (as E) is the angular Point to the 4 lesser Squares joined together. Now a Line running from the Center to any of the Angles of the given Square or Garden, will divide that lesser Square into two Triangles (as E B) and is the Hypothenufe to either of them: This Hypothenufe is found by common Numbers according to the Method of calculating Triangles, viz. by finding the Square Root of the Sum of the Squares of the Base and Perpendicular of any one of the lesser Squares (as they are all alike) and this square Root is the Base of another new Triangle, of which the intended Ladder (as E F) is the Hypothenufe, and the Tower F B (= 100 Feet, or a third Part of the Side of the Garden) is the Perpendicular.



$$50 \times 50 = 2500$$

$$50 \times 50 = 2500$$

Yds.

$$5000. (70.71 \div = EB$$

49

$$1407 \overline{) 10000}$$

9849

$$14141 \overline{) 15100}$$

14141

959

$$70.71 \times 3 = 212.13 \text{ Feet} = EB$$

Or EB in Feet may be thus found.

$$50 \text{ Yds. are} = 150 \text{ Feet}$$

$$150 \times 150 = 22500$$

$$150 \times 150 = 22500$$

$$45000. (212.13 = EB \text{ in Feet.}$$

4

$$41 \overline{) 50}$$

41

$$422 \overline{) 900}$$

844

$$4241 \overline{) 5600}$$

4241

$$42423 \overline{) 135900}$$

127269

$$8631 = 959 \times 9, \text{ because the Yards}$$

being multiplied by 3 to bring them into Feet, occasions this last Remainder to be 9 times greater than the other, the Square of 3 being 9.

$$212.13 \times 212.13 = 44999.1369$$

$$100 \times 100 - - = 10000.$$

54999.1369 (234.518 Feet, = EF, the
4 Length of each of the several Ladders.

$$\begin{array}{r} 43 \overline{)149} \\ 129 \end{array}$$

$$\begin{array}{r} 464 \overline{)2099} \\ 1856 \end{array}$$

$$\begin{array}{r} 4685 \overline{)24313} \\ 23425 \end{array}$$

$$\begin{array}{r} 46901 \overline{)88869} \\ 46901 \end{array}$$

$$\begin{array}{r} 469028 \overline{)4196800} \\ 3752224 \end{array}$$

$$\underline{444576}$$

34. Out of the following Figures, viz. 1113335557779991 it is required to find five of them that will make 20?

$$11 + 3 + 3 + 3 = 20$$

or

$$11 + 5 + 3 + 1 = 20$$

Note, The Difficulty in answering this Question arises from the Use of two ones, not as 1 and 1, which make two, but as 10 and 1, which make 11. It can be answered in no other Manner than the two foregoing Ways.

35. Change a Guinea into 20 Pieces, but let there be no Crowns, Half-Crowns, Shillings nor Six-pences.

3	2r. Guineas	0	15	0
12	Groats	0	4	0
5	Three-pences	0	1	3

Pieces 20

1 1 0

36. It is said, Gen. vi. 15, that Noah's Ark was 300 Cubits long, 50 Cubits broad, and 30 Cubits high; what was the Length, Breadth and Height in English Measure?

Note, A Cubit is = 1.824 Foot.

Feet.

Answ. $\left\{ \begin{array}{l} 547.2 \text{ long.} \\ 91.2 \text{ broad.} \\ 54.72 \text{ high.} \end{array} \right.$

37. Place the Alphabet in such Manner that A and Z may be as near together as K and L, without transgressing the commonly received Order of it.

Solution. *Make a Circle, and divide it into 26 equal Parts; on the Outside or Inside of which write the Alphabet; so will A and Z be as near as K and L.*

38. The Globe of the Earth being 360 Degrees, and each Degree upon its greatest Circle equal to 69 Miles and an Half; in what Time might a Man travel quite round on such a Circle (admitting there were Conveniencies for it) at the Rate of 20 Miles per Day? *Answ. 3 Years, 5 Months, 16 Days, allowing 28 Days to a Month.*

$$360 \times 69.5 = 25020 \text{ Miles.}$$

M. D. M. Y. M. D.

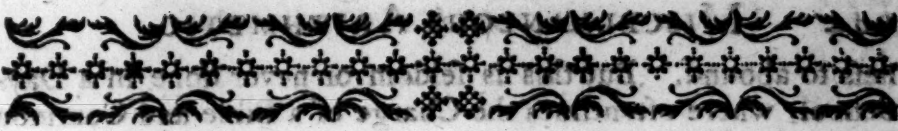
$$20 : 1 :: 25020 : 3 \quad 5 \quad 16$$

39. Admit the Sun to be on the Line; and at his setting, to be, by a good Observation, just 1 Degree above the Horizon; admit also a Man to be travelling on the Line full West, with the Sun right before him; how many Miles must he travel per Hour, to keep the Sun in the same Position? *Answ. 1042.5 Miles per Hour, allowing 69.5 Miles to a Degree.*

H. Deg. H. H.

$$24 :: 360 :: 1 : 1042.5 \text{ Miles.}$$

Miscellaneous



Miscellaneous Arithmetic :

OR A FULL

ACCOUNT of the NEW CALENDAR, &c.

PART VII.

OF THE EDUCATION of CHILDREN,

So far as relates to the several

SCIENCES which they are to learn at School.

Of Reading.

AMONG the several Branches of Literature commonly taught in Schools, there is not one, perhaps, more difficult, or less regarded, than that of Reading. I don't mean the bare Pronunciation of the Words, for that is not the Case; but the Reading with a proper Tone and Cadence; laying a just Stress or Emphasis on such Words as require it; whereby the Sentence, whatever it is, will appear according to the Mind of the Author: Without this, an Expression is often misunderstood; and what is really an Interrogation, may, by laying a Stress or Emphasis on wrong Words, be changed into a determinate Sentence. And it is no unusual Thing to meet with an Expression that is capable of bearing a double Construction, which by an undue reading, will have the Reverse of what was primarily intended. Now one Way (and perhaps the only one) to remedy this Inconvenience, is, to let the Scholar be furnished with such Books as will (with due Care in the Tutor) oblige him to fall into this Way, such as the *Spectators*, *Guardian*, *Tatlers*, *Milton's Paradise Lost*, *Young's Night Thoughts*, and many others, with which we have the Happiness

ness to abound. But this is seldom or never done in a Day-School, where oftentimes the Charge of a Bible and Common Prayer Book only, are thought much of. And yet it is expected those Children should read as well as the best, though they are not furnished with such Helps as are necessary for the Purpose; and without which, no Master, how capable and diligent soever he be, can forward his Pupils. And it is certain, that Boys of Ability and Inclination, whose Parents are happy in Circumstances, and are not afraid of the Expense, must make the desired Improvement.

Of Writing.

The Usefulness of the Pen, in all its Varieties, but especially in the Round-Hand, is so very great and extensive, that very little need be said concerning it, especially since most People are now very industrious to have their Children acquire the free Use thereof. Within the last Century, very great Improvements have been made in Writing; and perhaps it is at this Time arrived to that Perfection as not to be much exceeded. And as no Business can be well carried on without setting Pen to Paper; it must certainly look extremely pleasing to the Eye, to see Books of Accompts well and orderly wrote; while, on the contrary, to see Books ill wrote, blotted, and in which is bad Spelling, must give as large a Share of Pain.

Amidst the several Sorts of Writing, that particular Part of it called *Short Hand*, is of late Years, become none of the least; and its great Usefulness in taking down Speeches made *Extempore* in the two Houses of Parliament, Trials, &c. by which Means many very valuable Expressions are preserved, which otherwise would be lost, declare it to be so. In every Court of Judicature, the Judges thereof know the Advantages which arise from it, because they are thereby enabled to take down the several Depositions of the Evidences, and then sum them up, and from thence deliver their Opinions to the Jury, who give the final Sentence. In other more ordinary Cases, its Use is found in the quick Dispatch it makes of committing a Man's Thoughts to Paper, and likewise in the Secrecy thereof (if he is minded to have it so) inasmuch as it is not easy for any one to read it, but only such as use the same Alphabet, and other Marks of Abbreviation.

The Variety of Hands serve very well for Ornament in Books of Accompts, where there is any Leisure for the same: and indeed, all Books of Accompts should not only be regularly

larly kept, but well wrote likewise, that in case of any Examination on the Score of Bankruptcy, Decease, or any other Occasion whatsoever, they can be easily looked over and examined; and if any thing happens amiss, it is thereby sooner set right, to the Satisfaction of every Party concerned therein.

Of the Want of School Necessaries, beside Books to read in.

The Want of common Necessaries at School, such as Writing-Books, Pens, Ink, Paper, Pencils, &c. is another Impediment in the Way of a School-Boy's Progress in his Learning.

All People would have their Children improve in Writing, but many of them are put to great Pain at the Charge of Writing-Books. Some think they write too much, others, that they tare their Books to Pieces too fast, forgetting how it was with them when they were Children themselves; or if they happened to be of the careful Sort, think their own Children must be so too. Now the Want of School-Necessaries is a prodigious Hindrance: And as Parents would have their Children improve; so they must not deny them such things as tend to their Improvement; and without which they can't improve at all. Hence it follows, that People of mean Abilities can't reasonably expect that their Children should improve so fast as those whose Circumstances are better, and whose Childrene njoy all the Necessaries that are requisite.

And here, such Schools have the Advantage, the Masters of which have every thing that is proper for their Pupils Improvement by them, without the Parents furnishing them with every thing they want (which is generally of the worst Kind) and this, though attended with some Expense, yet the Scholars find the Advantage by it, and the Parents the Satisfaction of seeing their Children improve in an easy and regular Manner.

Of changing Masters.

Parents when they have found a Master that they can confide in, should, even religiously, conform to his Directions; and when it happens that their Children don't make so good an Improvement as is expected by their Parents, it should rather be imputed to the Pupil's Carelessness, or want of Ability. than the Master's Negligence: Since it is attended with a great deal of Danger, after having made Choice of a proper Master, to lay the Blame of the Scholar's Non-improvement on him. See *An Essay on the Education of Charity-Children*, p. 7.

Of

Of Method in a School.

Every Schoolmaster must (like all other Men of different Occupations) have a Method; out of which, if he suffers himself to be put, all is disjointed; and instead of Harmony, his whole School will be put into the utmost Confusion, and himself in the greatest Perplexity. Hence all Parents should be very far from giving Directions to the Schoolmaster how he should manage their Children in Point of Instruction in Literature: For if the Master pulls one Way, and the Parents another, it is certain that the Children will make very little Improvement. Some People are mighty fond of recommending the Method themselves were taught by: But should a Schoolmaster attempt to teach every Child by the Method his Parents shall prescribe, he would not be able to teach six of them aright, occasioned by such a Diversity of Methods: Nay, if he has one general Method, and that Method not very just, those six Boys, if they have any Spirits, and regard their own Improvement, will press so hard upon him as to make him run almost beside himself, for want of Employment, because they can do Business faster than their Master can find it for them to do. And this I shall make appear in the following Manner.

Suppose, for Example, a Master should always rule his Scholars Writing-Books; it is now well known that this will rob him of a great deal of his Time, which will be more profitably spent in Instruction: and if he be the most expert Ruler, the just Distances of the Lines, this Way, can never be come at: For what with Haste, and perhaps, Impatience, the Ruler will sometimes slip; or if it be made the least tapering, will of itself run uneven, and as it were, twist about, and make the Lines run wide from a Parallel. Now the best Remedy for this Inconvenience, is black Lines; those, which I have contrived for my School, are after this Manner, *viz.* a double Line for the Body of the Letter, a Line for the Top of the Letter, and another below for the Tail, with a sloping Line for the Position. Now as nothing of this Kind can be done with a Ruler and Plummets; so Copper-Plate-Lines of this Kind are the most useful Contrivance for the Improvement of Writing, that can be; and if they be made for various Sizes (four being enough) it will still further that Improvement. By this Means all that Time is saved, that is spent in ruling Writing-Books. Again,

Suppose

Suppose he has a competent Number of Cypherers, and should set all their Cyphering-Books; this will rob him of more Time than the ruling the Writing-Books. Nor is this the Worst: For if to ease himself, and to bring this Kind of Business into a narrow Compass, he sets but a few Sums, his Scholars will stand still for want of Employment, and harass him most sadly that Way: And, if to keep them full employed, he sets them a sufficient Quantity, so much of his Time, by this Means will be engross'd, that he will scarce have any left for Instruction; especially if he adds to this the ornamental Part, which some Writing-Masters, to shew their Skill, are very fond of. For this Inconvenience also, I have provided a Remedy, called *The Schoolmasters Assistant*, with another, called the *Young Book-keepers Assistant* (both pretty well known now) where there is always Business enough in Arithmetic and Book-keeping, ready cut out. By these Means a young Gentleman intended for Business in the *Mercantile* Way, when he comes to School, has his Business always ready prepared to his Hand, and without any Fatigue to his Tutor. Hence (if the Parents would not spare their Pockets) many other useful Parts of Literature might be taught, such as *Grammar*, *French*, *Geography*, and the several Branches of the *Mathematics*, most of which are in many Schools intirely omitted, for want of such a speedy Method as this is. Now Children placed out in Schools where the foregoing Methods are used, have all the Advantages that can be practised or even desired. As to such Masters of Schools, as, for the sake of getting a Number of Scholars, do it at so mean a Price, that they can scarce make a Livelihood of it, very little need be said about them, because I think they say enough for themselves. Beside, when Parents, as it were, hawk about for the cheapest Schools, and would have a great deal of Learning for a little Money, if they happen to be baulk'd, can blame nobody for it but themselves. Not to say, according to the common Way of Trading, if the best things cost the most Money, the worst Sort should not cost so much; and therefore, if Parents stand resolved to give but a little Money for their Children's Education; Reason will direct that they must not expect it in so ample a Manner as where a larger Price is given.

Of the Modern Languages.

These are serviceable to all trading Persons, especially such as send Goods to, or receive them from any foreign Kingdom. And here, whatever particular Sort of Trade, any
young

young Gentleman is designed for, whether it be to *France, Spain, Portugal, Italy*, or any other Kingdom, it would not be amiss to learn the Language of that Country. However, as the *French* Language is universally known in all Parts of *Europe*, it may be worth the while for the young Merchant to be acquainted with that, since he will in all Probability, often find Occasion to understand it, by writing himself, or receiving Letters in that Language.

Of Mathematics.

By these I mean Geometry, Trigonometry, Dialling, Astronomy, Navigation, Surveying, Gauging, and the like, all which Studies are to some profitable, but to every one most pleasant and delightful. And no Time (except in the immediate Acts of Religion) can be better spent with less Repentance, than in such Speculations as these. 'Tis owing to Studies of this Kind, that so many surprising Conclusions, numerical, optical and mechanical, have taken their Rise: consequently where there are both Time and Abilities, they ought not to be omitted: I shall only observe here, that *Geography*, which is a Science that consists in the Knowledge of the several Parts of the Globe, the Situation of distant Lands, Cities, Towns, &c. together with a Knowledge of the Manners and Customs of the several Inhabitants, is very useful and very easily attained, is nevertheless almost as much neglected as it is useful. And it is very surprizing to me, that a Science which comes within the Compass of every Pupil's Understanding, should be so much condemn'd even by Parents, as to forbid their Children learning it, because they think it will be of no Service to them.

Of Book-Keeping.

As a great deal has been said already in my *Young Bookkeepers Assistant*, both by Preface and Notes, very little may be said here. I shall therefore only observe, that it is the Art or Mystery of keeping an Account of all Transactions of Trade; the Incomes and Expenses of Estates; and the Charges and Profits of a Prince's, Nobleman's and Gentleman's Revenue; so that at one View, the Advantage or Disadvantage of the Whole, or any particular Part may be readily seen and discovered; for which Purpose, that most excellent Method, called *Double Entry*, or the *Italian* Manner, has been invented, and now generally practised by all regular Accomptants, especially Merchants.

Of the English Language.

Whatever may be said in Commendation of foreign Languages, it is certain an *Englishman* should understand the *English* Tongue; and, if it be possible, in all its Elegancies. And here, Parents happy in Circumstances, and good Inclinations, and their Children happy in Abilities, are most likely to succeed. It is no small Commendation for a young Gentleman or Lady to write a Piece of good *English*; and to be defective herein, is to be defective in an Essential: And therefore, as he who writes a bad Hand, or is ignorant of Figures, is very unfit to be a Book-Keeper; so he who is not Master of his own Language, at least in some tolerable Degree, is equally unfit for that Employment. Besides, the writing of a Letter well, and couching it in proper and pertinent Terms, must needs be very agreeable, even to the Writer of it; while another, who labours at it, for want of proper Diction, and a thorough Acquaintance with his Mother-Tongue (which will always produce unjust and lame Expressions, and oftentimes Misunderstandings) cannot, on a Survey of it, after it is wrote, but lament the want of that useful Share of Knowledge.

Writing Exercises.

By these are meant the Employment of the Time at Home, after School-Hours are over, in writing out, and then getting, *memoriter*, some useful Lesson, either in Spelling, or what else the Tutor, in his Judgment, shall think most convenient for the Improvement of his Pupil; and herein the Learner will undoubtedly find his Advantage, by being employed in some Part of Literature, which has a Tendency to his future Good. Parents therefore do wrong to their Children, when they forbid this useful Employment: And it is a sad Truth, that when Parents run counter to the Rules of the School, in which their Children are instructed, they do in Effect, teach those Children to do the same thing. Hence, as Children are naturally prone to do wrong, it is impossible (by such a Proceeding from the Parents) for them to make any tolerable Share of Improvement. For as they perceive the Wings of their Tutor's Authority to be clipped, and his Power over them lessened, they of course, will undervalue, despise and deride him; and from being forbid to do what they ought, they will most certainly do what they ought not; the bad Consequence of which is but too often seen, whenever Occurrences of this Kind happen. Let the Parents then look to it,
if

if by with-holding their Children from obeying their Tutor's Directions, they, instead of being obedient Children, pick out their Parents Eyes, and turn reprobate.

Of the Method of examining Children at Home, and therein of the want of a becoming Presence of Mind in them.

It is no uncommon Thing for Parents, when they have a Mind to try their Children's Capacities, to put very idle Questions to them, such as the multiplying $2s. 6d.$ by $2s. 6d.$ and the like, which, in no Shape, will hold good, except in the Rule of Three, as before taught, and then, if a Failure happens, to ridicule either the Person so tried, or his Tutor, or both. But, that this is a very unfair way of dealing with young Heads, is manifest from the Trial itself, because it is impossible to *set old Heads upon young Shoulders*; it happening that good and able Men, Men of Capacity and Genius, have sometimes been confused and overcome, by such sudden but idle Propositions; and it is then no Wonder if a Boy should be put to his *Ne plus ultra* by a like way of Proceeding. It must indeed be confessed, that whoever enjoys a good Presence of Mind, is possessed of a very valuable Blessing; but how this is to be obtained, perhaps belongs more to the *Parents* than to the *Schoolmaster*; it being certain (however great the Tutor's Care is in forwarding his Pupils) that many Boys can perform very commendably at School, who out of it can do nothing that is acceptable, nay sometimes are scarce able to speak; and the very fear of doing wrong before their Parents, has made them do so: Hence some Parents, not knowing rightly how to put the Question to their Children, first quarrel with them, and next with their Tutors, when the Fault lies in neither of them. It was the Case once (as I have been credibly inform'd) of a Father, who, though he could not read himself, would take upon him to examine his Son; the Child being sensible of his Father's Inabilities, and hot Temper, and fearful, right or wrong, that his Father would correct him, stood quite mute, for which, the good Father, in the Height of his Passion, had like to have cut out his Eyes with a Horse-Whip.

The whole Care and Management of Children, as I have elsewhere observed, in an *Essay on the Education of Charity-Children*, p. 7, does not lie on the Teacher altogether: There is something to be done at Home, which (if Parents would learn to know themselves) they might soon perceive what Part they are to act out of School-Hours. It is in short the

the setting them a good Example both in Speech and Action; never to be guilty of that Fault for which they reprove their Children; and by no Means to brow-beat them, except for Enormities; but at other Times, and for less Faults, to argue with them, and shew them their Errors, with such Calmness and Evenness of Temper, as will make it appear to them, that such Parents rather chuse their Childrens Amendment than gratify a Passion in themselves: Among other things, they should be careful now and then to introduce them into good Company, where the Rules of good Manners should be strictly observed. Without this Way of Proceeding, it will be in vain for Parents to examin their Children about their Improvement, since they will very rarely be found to stand the Trial.

Of Drawing.

Amidst the several beautiful and entertaining Arts, it must be confess'd, that Drawing has its Share of Admirers, as well as the rest, and perhaps not the least in Number. And if to behold the Resemblances of things (if those Resemblances are accurately done) be a Pleasure, it must be more so, to be able to make such a Resemblance one's-self. Drawing, strictly speaking, signifies no more than the describing the Outlines of any Subject to be imitated; but more commonly it includes Limning or Colouring, which is also called Painting: by the Help of which, a Flower, Bird, or any other Thing, may be imitated so nearly, as that it shall appear to be the Thing itself. And indeed this is the Perfection of the Art, to copy after Nature so closely, as that Art may be taken for Nature. Hence to be able to perform acceptably, and to excel in this Art, must not only give Pleasure, but in many Cases may be found necessary. The Story of *Parrhasius* and *Zeuxis* is very entertaining, which runs thus.

Parrhasius and *Zeuxis* were eminent Painters, and contended for Superiority. Each painted according to his Fancy; *Parrhasius* painted a *Curtain*, and *Zeuxis* a Bunch of *Grapes*. As *Zeuxis* was carrying his Performance, it appeared so natural to the Birds, that they flew to it for the sake of the imaginary Fruit, but were deceived. When *Zeuxis* came to *Parrhasius's* House, and produced his Work, it was acknowledged to be very good, and so much the better as it had deceived the Birds. *Zeuxis* then desired to see *Parrhasius's* Performance, and accordingly was led into the Room where the *Curtain* was; but he taking it for a real one, imagined *Parrhasius's*

sius's Work was within it, and order'd the *Curtain* to be drawn, that he might behold it, which decided the Controversy at once in favour of *Parrhasius*; for though *Zeuxis*, by his Performance had deceived the Birds, yet *Parrhasius* had carried the Point a great Way farther, by deceiving a Master of the Profession.

Of Music.

From the first Inventor of this Art, down to the present Time, *Music* has ever been in the greatest Esteem; and the great Majority of Mankind have all along so strongly declared in its Favour, that it is no Wonder its Number of Votaries are now become very great. Such is the Efficacy of *Music* (sacred *Music* I mean) that it strangely works upon the Passions of Men, and softens their rugged Tempers and Dispositions: Several Instances we have in sacred Writ of this dissolving and melting Quality, which so wrought upon *Saul*, by *David's* playing on the Harp before him, when he was troubled with an Evil Spirit, as to make him well, *i. e.* easy in his Mind, who before labour'd under some very uneasy and painful Sensations. Well may it then be called the Handmaid to Divinity, when its Influences are so surprizing. At this present Time, *Music* in some Cases is carried too far, contrary to the Intention of the first Promoters of it; and to the Shame of such Composers of it, be it spoken, that there is no Sett of Words, whether in Prose or Verse, how bad soever, but some loose-principled Men will set them to Music. And the great Number of filthy and lewd Songs are now become so common, that it is hard to escape them. The *Music* therefore that I would recommend (and which yet stands recommended by much better Pens, and seems to gain Ground of late Years) is such as is set to Words either sacred, or at least such as runs not counter to it, and the Instruments are the *Spinnet*, *Harpsichord* or *Organ*, which are noble, and therefore very entertaining. Good Performances on these Instruments, carry with them irresistible Charms, not only to the Hearers, but even the Performers. Hence Persons of happy Circumstances should by no Means let their Children remain ignorant of an Art that *Solomon* calls *the Delight of the Sons of Men*, but cause them, among other Branches of a polite Education, to imbibe the Principles of this.

Of Dancing.

Dancing is an agreeable Motion of the Body, adjusted by Art to the Measures of a musical Instrument, or to the Voice:
and

and though it is perhaps the least useful of any thing taught in Schools, it has, however, some that speak in its Praise, both antient and modern: Though it must be confess'd, that while it has been held in Esteem by some, it has been look'd on in a very contemptable Light by others. But however that may be, it certainly gives a Grace to such as have been exercis'd that Way; and when us'd as it ought to be, has, in all Ages, more or less, been esteem'd a very genteel Accomplishment: I say, when us'd as it ought to be; for if it be carried to an undue Length, it is preductive of something that is tainting, and the Youth of both Sexes have sometimes suffer'd very severely by such Indulgences. There was a Time when Dancing was made an Act of Religion; and no less a Man than *David*, the second King over *Israel* did so, when he *danced* before the *Ark* to honour God, and express his Excess of Joy for its Return into the City of *Zion*: However, nothing of this Kind is admitted of now; and the Art of *Dancing* is learned for nothing more than either to give a graceful Carriage, or for Pleasure and the Benefit of Exercise. Hence we may conclude, that Dancing, of itself, is harmless; and when kept within due Bounds, is conducive to *Health*, by promoting Perspiration, and throwing off such superfluous Matter as would otherwise, in Time, become destructive of it.

Of learning Latin.

However fond the major Part of Parents may be of their Children's learning the dead Languages, it is very certain, that many are put to this Task, which Nature forbids: And the pernicious Consequences that follow from such an ill concerted Proceeding, are such, as some have all the Reason in the World to lament as long as they live. It is owing to this heavy Drudgery (and I can call it no otherwise, where Children are oblig'd to learn what they have no Abilities for) that many are spoil'd from becoming both good Penmen, and good Accomptants, and consequently good Merchants or Traders.

The learning *Latin* (for Example) is become so common, that in the Opinion of many People, their Children must be taught it, because it makes them spell well; whereas nothing is more unlikely: And to say the best of it, it is such a round-about Way to learn the *English* Language, as is by no Means warrantable; for the *English* may be taught grammatically, as well as the *Latin*, or any other Language; and the Time that is spent in going over the Rules in *Lilly's*
M Grammar,

Grammar, cannot be adequate to the Loss of Knowledge in other Sciences, occasioned thereby; especially in such, whose Abilities, or Circumstances, or both, require them to be acquainted with such things that more naturally fall in with Trade and Commerce, with which *Latin* has no Share at all. "There are many excellent Tempers which are worthy to be nourished and cultivated with all possible Diligence and Care, that were never designed to be acquainted with *Aristotle, Tully, or Virgil.*" Spectator, Vol. 2, p. 278. Let it then be the Care of all Parents, when they have found a Teacher of Probity, to abide by his Determinations, and permit their Children to be instructed in such Branches of Learning as they have an Inclination for, and will acquire with Pleasure, but never force them to learn such things as they have no Abilities for, or cannot come at, but with the Loss of something more beneficial.

Of the Circumstances of Parents.

It is much to be wished, that all Parents whose Care for their Children's Improvement in Learning, were happy in *Circumstances*, in Proportion to the Expectations they have of their Children's Performances; the want of which, occasions many Children, whose natural Abilities are exceeding good, to leave their Schools without being able to receive such a Share of Education, as those whose *Circumstances* are really very affluent; and yet, strange as it is, Parents of but low *Circumstances*, expect their Children to make an Improvement in Learning (though it be only at the Writing School) equal to those, whose Fortunes are ample enough to grant their Children all the Necessaries requisite thereto. The Expense of Pens, Ink and Paper only, as has been before observed, (without which it is impossible to write a good Hand, or become an able Accomptant) are thought so much of by some narrow Spirits, that the Teacher is sure to meet with a Reprimand for charging them in his Bill: What must be the Case then, where higher Attainments are expected? And yet higher Attainments will be attended with their respective Charges. But it is really very bad for Parents, whose *Circumstances* are such, as every one would wish to enjoy, to dispute the Point with the Tutor, for such necessary Articles as they can by no Means do without. This is like *Pharaoh's* requiring the Children of *Israel* to make Bricks without Straw; and how hard their Case was, every one can determine very easily.

Of Decency and Good Manners.

I have heard it reported, that *William of Wickham*, once Bishop of *Winchester*, when he taught School, caused to be wrote there, in large Characters, this Motto, MANNERS MAKE A MAN: So sensible was he of the Force of good Manners; intimating thereby, that where young Persons could be brought to conform to the Rules of Decency and good Behaviour, they were likely to reap the Benefit of them, by thriving in the World, and becoming useful Members of the Commonwealth; and such as good *Manners* could take no Hold of, were as likely to prove bad Parents, bad Masters of Families, and become the very Pest of the Community. Now this Rule in Life must be taught by the Parents, at least in a great Measure so, because at the ordinary Day-Schools, Children are no longer under the Master's Inspection than while they are at School; and when they are gone from thence, the Master cannot be accountable for their Misbehaviour. And though it is very common for the Parents to charge the Master with Neglect, where good *Manners* are wanting in their Children, yet the same Parents take it very ill, if their Master should correct their Children for being rude, and roundly tell him, he has nothing to do with their Children out of School-Hours. But in Truth, the School-master, in this Case, has a hard Task of it, as it is like the Mariner's steering between the Rock *Scilla* and the Gulf *Charybdis*, where, if he avoids the one, 'tis great odds but he is split to Pieces or cast away upon the other.

Of School and Family Prayers.

How indifferently soever some may think of this, yet I beg Leave to assure my Reader, that it is of too great Consequence to be neglected. We commonly say, If a Favour is not worth asking for, it is not worth having: But if God Almighty should deny his Favours to all those that refuse to ask for them, their Condition must be very bad indeed, who do not receive them. Nor only so, but for want of this Christian Armor, we lie open to the Arrows and Battery of our Spiritual Enemies, viz. the Devil and his Angels, whom *St. Paul* styles *Principalities, and Powers, and the Rulers of Spiritual Wickedness in high Places*; implying that these are no small Foes, which we have to contend with; but those of the most powerful Kind. Wicked Spirits see us when we do not see them, and therefore it behooves us to be so much the more upon our Guard, that we be not overcome by them. And if it be true (as most certainly it is)

That it is good to draw near to God :

That if we seek God, he will be found of us :

That such as are far from God shall perish : And

That if we forsake God he will cast us off for ever :

these ought to be strong Motives to induce us to *pray without ceasing* ; that is, always to be in a praying Frame of Temper, and to lay hold of any Opportunity of praying when it offers. *Abraham and Joshua, Cornelius and Aquila,* stand renowned upon sacred Record, for the Piety of their Households : And surely, if the Faith and Zeal of a good Householder, and I hope I shall be pardoned, if I say a good Schoolmaster, be duly vigorous and stedfast, he cannot but delight to call the little Assembly of his Family, or School, together, to worship their infinitely good and gracious God, in whose Hands their Breath is, and *from whom cometh every good and perfect Gift.* And, to the End, that the right ordering the Morals of Youth be not neglected, there is no better Way (in a School) to do it, than by beginning and ending each Day's Study with Addresses to the great Creator and Preserver of the Universe (which for Honour and Distinction's sake, should be that Pupil's Province, who stands first in the School) a very momentous Affair ; too much neglected by many Teachers, but should be omitted by none. And as the main End of Education is, or should be with a View to Religion, in order to secure a happy Eternity, besides its being made subservient to the Affairs of this Life, it is a Matter of the last Importance, to take Care that young Minds be well seasoned therein, the better to enable them to guard against the Superstitions, Heresies and Idolatries of the Church of *Rome*, which of late Years, prevail very much in *England*. Jesuits and Romish Missionaries therefore, as they swarm (in Disguise) in and about *London*, to make Profelytes, and broach their pernicious Doctrines ; this should oblige all Protestants to use their utmost Endeavours to fortify their Children against every Attempt to seduce them to that wicked Church. Hence if Children are timely and properly armed, in order to make a suitable Resistance, Decency and good Manners will naturally follow, or be the more easy inculcated. Hence also (as Parents and Schoolmasters should always begin and end their Business with God) we may observe, where Children see their Parents and Masters use this Method of praying to and praising their great Creator, that they themselves will be naturally led to do the like afterwards, which not only tend to the Glory of God in this Life, but the Salvation also, of their own immortal Souls in the Life to come.

N. B. The following Lines should have been inserted in p. 92, but as they were then omitted, it was thought advisable to place them here, rather than wholly omit them.

Whatever has been said with regard to the exquisite Workmanship of the Tabernacle, and all its Appendages; may without the least Diminution, be applied to the Workmanship done by our Saviour, while he was in the Flesh, and wrought in the Occupation of a Carpenter. For if the curious and admirable Mechanism of the Tabernacle, &c. was owing to the several Workmen's being inspired, and taught by the immediate Direction of God Almighty himself, nothing less can be said of the Saviour of the World (*who had all the Fulness of the Godhead dwelling in him, and had Wisdom without Measure*) when he took an Instrument in Hand, whether Saw, Plane, or any other Implement of that Trade.

The Square and Compass mark'd out justest Lines,
That what was most superfluous might first
Be taken off by th' Weight of th' sharper Ax:
The Saw made nicest Kerf, and splinter'd not:
The lab'ring Plane, o'er ev'ry Piece it pass'd,
Made roughest Wood, superlatively smooth:
Th' uplifted Mallet with due Force came down;
Nor err'd the Chizzel in its finest Cut:
And th' Joint, where join'd, so curiously was wrought,
By Mortise, Tenon, Pin, exactly fram'd,
That it all human Art exceeded far.

Such was the Skill of him, who long e'er that,
Taught Wisdom to the wisest of meer Men;
And longer still, e'er Man was made, made Earth,
Sun, Moon, and all those glorious Orbs of Light:
Then Motion circular and central due
To each gave, as it suited his great Will;
That Angels wonder'd at the Work divine,
And all th' Hierarchy, all the Heavenly Host
In sweetest Notes, and most ecstatic Strains,
To th' Eternal sounded 'ternal Praise;
And sung such rapt'rous Songs as never reach'd,
But once, since *Adam* err'd, the human Ear.

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